

# Using LS-DYNA To Model Hot Stamping

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**A. Shapiro, “Finite Element Modeling of Hot Stamping”, Steel research International, p. 658, Vol. 80, September 2009.**

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# Katana: how to make a Japanese sword

LSTC

The sword smiths of China during the Tang Dynasty (618-907) are often credited with the forging technologies that the Japanese used in later centuries. These technologies include folding, inserted alloys, and quenching of the edge. Okazaki-san is recognized as Japan's greatest sword smith creating such weapons as the katana (14<sup>th</sup> century).



**Heat** the steel to the color of the moon in February



**Transfer** the blank to the anvil



**Form** the blank with a hammer and lots of muscle



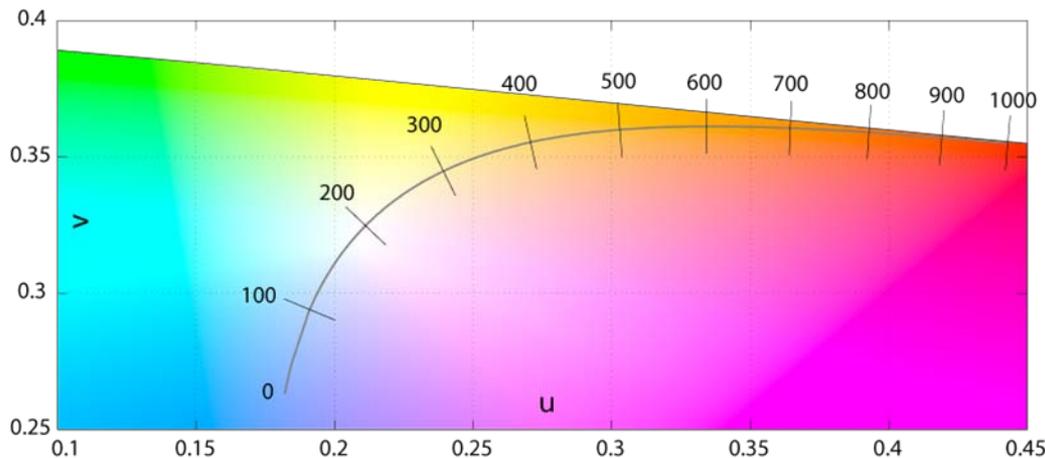
**Quench** the blade.

# Katana: how to make a Japanese sword

## Temperature of the Moon in February

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A color triangle is an arrangement of colors within a triangle, based on the additive combination of 3 primary colors (RGB) at its corners. The correlated color temperature is the temperature of the Planckian radiator whose perceived color most closely resembles that of a given stimulus. Shown is the Planckian locus (in mired) overlaid on the color triangle.



NASA 2/23/09

$$T_{moon} = \frac{1 * 10^6}{M} \approx \frac{1 * 10^6}{900} = 1111 K = 838 C$$

# B-pillar: how to make Car parts

Courtesy of Mercedes Car Group, Sindelfingen , Germany

LSTC

## 1. Heat



## 2. Transfer



## 3. Form

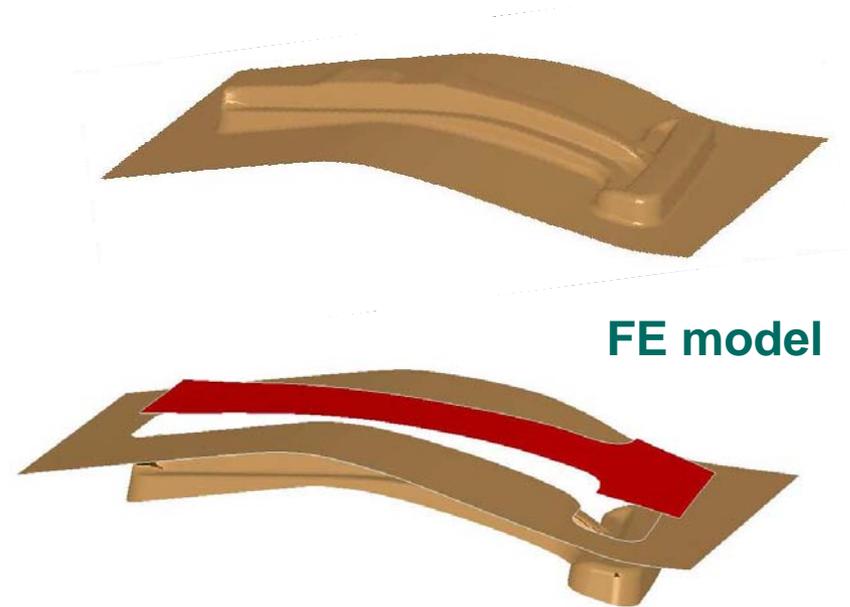
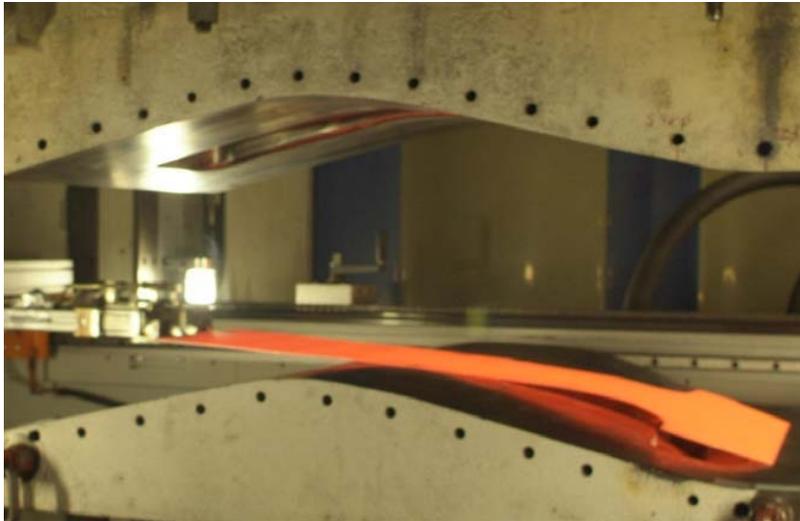


## 4. Quench

# Numisheet 2008 Benchmark BM03

proposed by Audi

LSTC



## Benchmark process specification

1. Heating of the blank to 940C.
2. Transport from the oven into the tool 6.5 sec.
3. Temperature of the blank at the beginning of the die movement 810C.
4. Forming process time 1.6 sec.
5. Quench hold time in the tool 20 sec.
6. Cool down to room temperature 25C

# Symbols and values

## metal

<b>Blank</b>	
material	22MnB5
dimensions	
<i>l</i> , thickness	0.00195 m
length	1m
width	0.25 m
properties	
$\rho$ , density kg/m <sup>3</sup>	7830.
C <sub>p</sub> , heat capacity J/kgK	650.
k, thermal conductivity W/mK	32.
$\lambda$ , latent heat, kJ/kg	58.5
$\alpha$ , linear expansion, 1/C	1.3e-05
E, Young's modulus, Gpa	100.
$\mu$ , Poisson's ratio	0.30

# Symbols and values

## air at 483C

LSTC

$$T_{film} = \frac{940 + 25}{2} = 483.$$

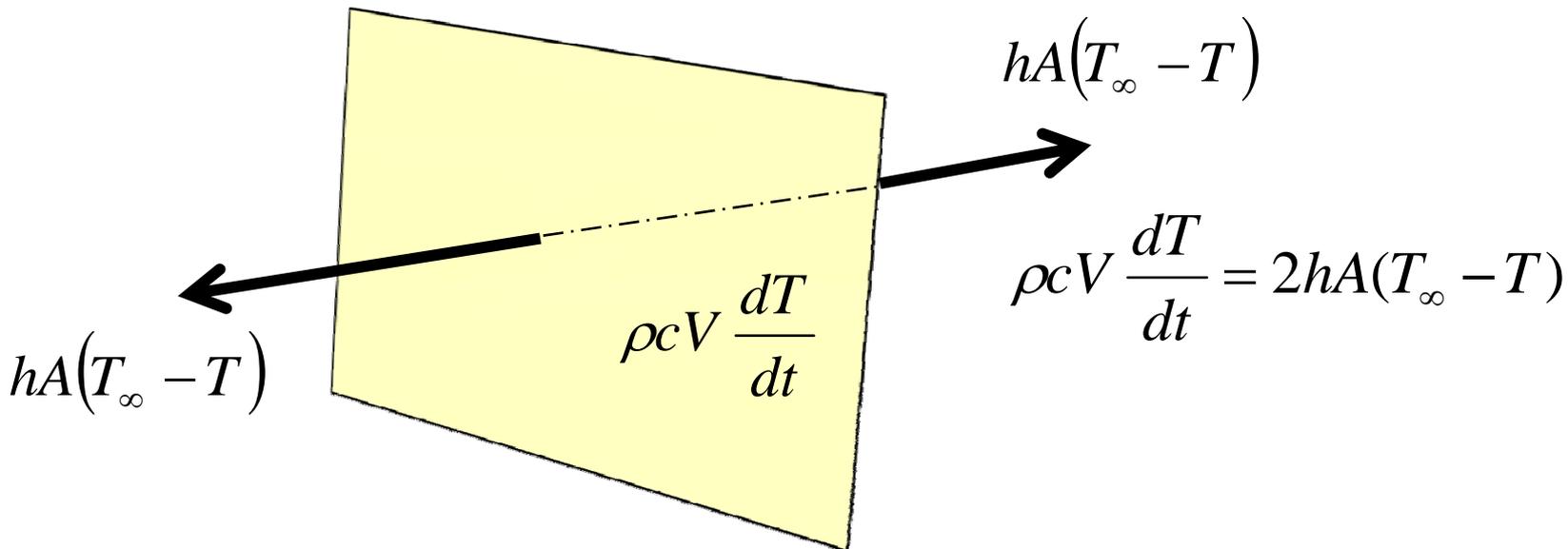
Air properties at 483 C	
$\rho$ , density, kg/m <sup>3</sup>	0.471
C <sub>p</sub> , heat capacity, J/kg C	1087.
k, thermal conductivity, W/m C	0.055
$\mu$ , viscosity, kg/m s	3.48e-05
$\beta$ , volumetric expansion, 1/C	1.32e-03

# Newtonian heating or cooling

## convection lumped parameter model

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Consider an object being heated from some uniform initial temperature,  $T_i$ . If the object is of high thermal conductivity, then its internal resistance can be ignored, and we can regard the heat transfer process as being controlled solely by surface convection.



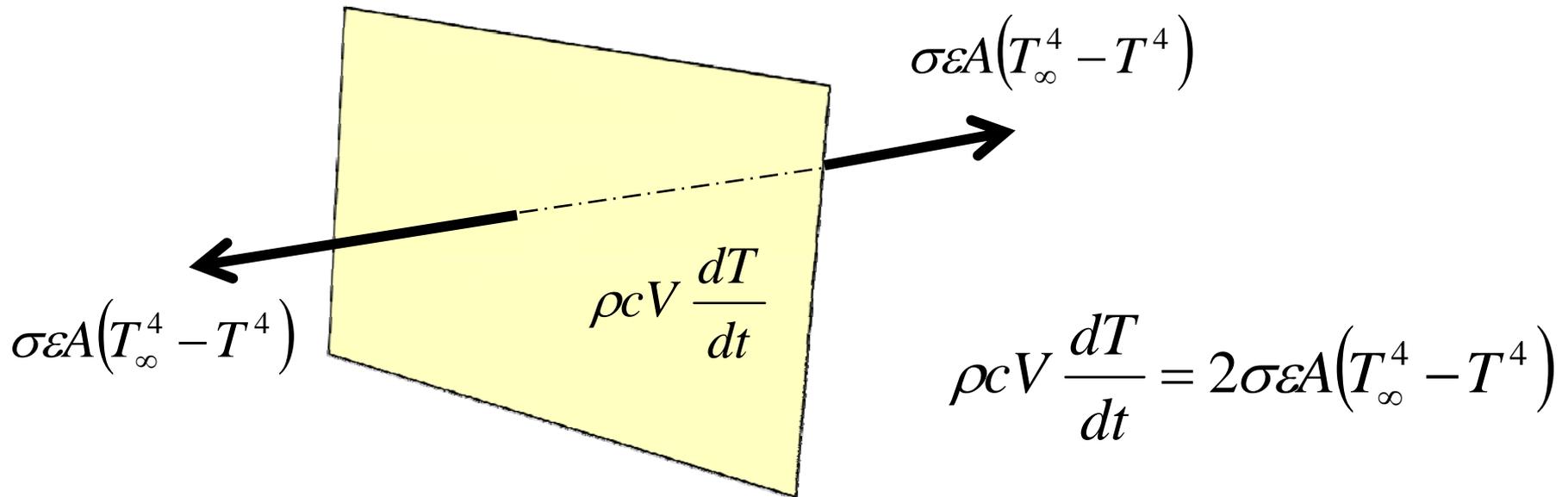
The solution is

$$\frac{T - T_\infty}{T_i - T_\infty} = e^{-\left(\frac{2hA}{\rho c V}\right)t}$$

# Newtonian heating or cooling

## radiation lumped parameter model

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The solution to this differential equation between the limits ( $T=T_i$  @  $t=0$ ) and ( $T=T_f$  at  $t$ ), is

$$t = \frac{\rho c V}{2A \sigma \varepsilon} \left[ \frac{1}{4T_{\infty}^3} \ln \frac{(T_f + T_{\infty}) / (T_f - T_{\infty})}{(T_i + T_{\infty}) / (T_i - T_{\infty})} + \frac{1}{2T_{\infty}^3} \left( \tan^{-1} \frac{T_f}{T_{\infty}} - \tan^{-1} \frac{T_i}{T_{\infty}} \right) \right]$$

# Blank heating and transport into tools

Our starting point for the FE analysis was Process Step Specification 3. However, we performed a hand calculation to verify steps 1 and 2.

The following analytical equation can be used to calculate the time for the blank to cool by radiation from  $T_f=940\text{C}$  to  $T_i=810\text{C}$  during the transport operation from the oven into the tool. The surroundings are at  $T_\infty=25\text{C}$ .

$$time = \frac{\rho C_p l}{2\sigma\varepsilon} \left[ \frac{1}{4T_\infty^3} \ln \frac{(T_f + T_\infty)/(T_f - T_\infty)}{(T_i + T_\infty)/(T_i - T_\infty)} + \frac{1}{2T_\infty^3} \left( \tan^{-1} \frac{T_f}{T_\infty} - \tan^{-1} \frac{T_i}{T_\infty} \right) \right]$$

$$time = 6.68$$

The calculated time is in agreement with the benchmark specification of 6.5 sec.

$$\sigma = 5.67\text{e-}08 \text{ W/m}^2 \text{ K}^4$$

$$\rho = 7870 \text{ kg/m}^3$$

$$l = 1.95 \text{ mm}$$

$$\varepsilon = 1.$$

$$C_p = 650 \text{ J/kg C}$$

Use degrees Kelvin in  
above equation

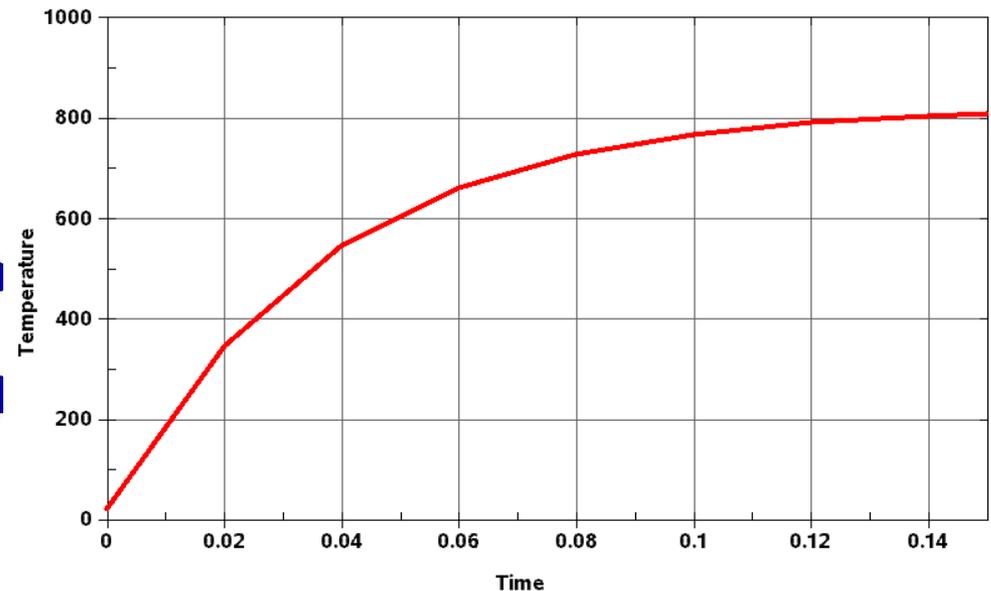
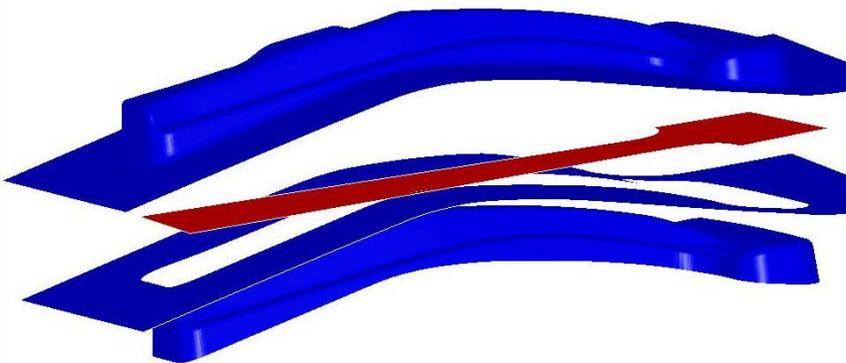
# Blank heating and transport into tools

## Blank $T=810\text{C}$ at beginning of die movement

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The easiest modeling technique is to define the initial temperature of the blank to be  $810\text{C}$ . However, doing this will not calculate the thermal expansion of the blank between  $25\text{C}$  and  $810\text{C}$ . Therefore, the blank is heated in the FE model resulting in a thickness increase from  $1.95\text{mm}$  to  $1.97\text{mm}$ .

The time to heat the blank is not a critical parameter for this analysis. All we want is the blank to be at  $810\text{C}$  and have the correct thickness at the beginning of the die movement.



# Blank heating and transport into tools

## How do you chose an h for heating the blank LSTC

It takes 0.4 sec for the upper tool to touch the blank according to the specified tool displacement curve. Therefore, select 0.15 seconds for heating.

$$h = -\frac{\rho C_p l}{t} \ln\left(\frac{T - T_\infty}{T_i - T_\infty}\right) = -\frac{(7830)(486)(0.00195)}{(0.15)} \ln\left(\frac{809.9 - 810}{25 - 810}\right) = 444,000 \frac{W}{m^2 C}$$

**h=444,000** is a ridiculously high number and is not physically possible. But, remember that the time to heat the blank is not a critical parameter for this analysis. All we want is the blank to be at 810C and have the correct thickness at the beginning of the die movement.

# Radiation & convection heat loss during transfer and forming

LSTC

After heating the blank, it is transferred to the tools. The blank cools by convection and radiation to the environment.



1. Heat



2. Transfer

The heat loss is calculated by:  $\dot{q}'' = h_{eff} A (T_s - T_\infty)$

How do you determine  $h_{eff} = h_{conv} + h_{rad}$

# Radiation & convection heat loss

## How to calculate coefficients

LSTC

### Convection

$$T_{film} = \frac{T_{surf} + T_{\infty}}{2} = \frac{940 + 25}{2} = 483 \text{ C}$$

$$L = \frac{2(\text{length} * \text{width})}{\text{length} + \text{width}} = \frac{2(1 * 0.25)}{1 + 0.25} = 0.4 \text{ m}$$

$$Gr = \frac{g\beta\rho^2 L^3 (T_{surf} - T_{\infty})}{\mu^2} = \frac{(9.8)(1.32 * 10^{-3})(0.471)^2 (.4)^3 (940 - 25)}{(3.48 * 10^{-5})^2} = 1.39 * 10^8$$

$$Pr = \frac{C_p \mu}{k} = \frac{(1087)(3.48 * 10^{-5})}{0.055} = 0.687$$

$$h_{conv} = 0.14 \frac{k}{L} (Gr * Pr)^{0.33} = .14 \frac{0.055}{.4} (1.39 * 10^8 * 0.687)^{0.33} = 8.3 \frac{W}{m^2 C}$$

### Radiation

$$940\text{C} + 273\text{C} = 1213\text{K}$$

$$h_{rad} = \frac{\sigma \varepsilon (T_{surf}^4 - T_{\infty}^4)}{(T_{surf} - T_{\infty})} = \frac{(5.67 * 10^{-8})(0.8)(1213^4 - 298)}{(1213 - 298)} = 107 \frac{W}{m^2 K}$$

# Radiation & convection heat transfer coefficients

LSTC

$$h_{\text{conv}} + h_{\text{rad}} = h_{\text{eff}}$$

T [C]	$h_{\text{conv}}$	$h_{\text{rad}}$	$h_{\text{eff}}$ [W/m <sup>2</sup> C]
50	5.68	5.31	11.0
100	6.80	6.8	13.6
200	7.80	10.8	18.6
300	8.23	16.3	24.5
400	8.43	23.6	32.0
500	8.51	33.0	41.5
600	8.52	44.8	53.3
700	8.50	59.3	67.8
800	8.46	76.6	85.1
900	8.39	97.2	106.
1000	8.32	121.	129.

**Note:**

- a)  $h_{\text{rad}}$  dominates
- b)  $h_{\text{conv}}$  @ T>400 uncertain

# Temperature of the blank at tool contact

LSTC

After the blank is positioned within the tools, it continues to lose heat by convection and radiation to the environment. The benchmark specifies a heat transfer coefficient of  $h_{\text{air}}=160 \text{ W/m}^2\text{K}$ . We feel that this value is too high and  $h_{\text{air}}=115$  is more appropriate. However, a hand calculation reveals that the blank only drops by 10C before the tools make contact. Therefore, knowing  $h_{\text{air}}$  precisely is not important. We ignored modeling this energy loss (i.e., temperature and thickness change) in our FE model.

$$T = T_{\infty} + (T_i - T_{\infty})e^{-\left(\frac{2ht}{\rho C_p l}\right)}$$

t = time until top tool contacts blank

$$800 = 25 + (810 - 25)e^{-\left(\frac{2(160)(0.4)}{(7870)(650)(0.00195)}\right)}$$

# Heat transfer to air and to dies



## Top blank surface

Convection + radiation heat loss to the environment, use:

- \***BOUNDARY\_CONVECTION**
- \***BOUNDARY\_RADIATION**

## Bottom blank surface

Turn off thermal boundary conditions when parts are in contact.

- \***CONTACT\_(option)\_THERMAL**  
parameter **BC\_FLAG = 1**

There will be a through thickness temperature gradient in the blank caused by the different heat loss rates from the surfaces.

## \***CONTROL\_SHELL**

**ISTUPD = 1** → calculate shell thickness change

**TSHELL= 1** → 12 node thick thermal shell, **T gradient through thickness**

# Heat transfer to air and to dies



The **top surface** loses heat to the environment by convection and radiation.

The **bottom surface** loses heat to the tool. The contact heat transfer to the tool is **10x** greater than conv. + rad. loss.

There will be a through thickness temperature gradient in the blank due to the large difference in heat loss rates from the top and bottom surfaces. This is calculated using the 12 node thick thermal shell formulation developed by G. Bergman & M. Oldenburg at Lulea University.

What is  $h$  contact ?

# Contact parameters

(1) Friction function of T (2) heat transfer function of P

LSTC

\*CONTACT\_(option)\_THERMAL\_FRICITION

lcfst lcfdt formula a b c d lch

## Mechanical friction coefficients vs. temperature

Static →  $\mu_s = \mu_s * \text{lcfst}(T)$

Dynamic →  $\mu_d = \mu_d * \text{lcfdt}(T)$

1	$h(P)$ is defined by load curve “a”	such as GE data
2	$h(P) = a + bP + cP^2 + dP^3$	polynomial curve fit
3	$h(P) = \frac{\pi k_{gas}}{4\lambda} \left[ 1 + 85 \left( \frac{P}{\sigma} \right)^{0.8} \right] = \frac{a}{b} \left[ 1 + 85 \left( \frac{P}{c} \right)^{0.8} \right]$	I.T. Shvets, “Contact Heat Transfer between Plane Metal Surfaces”, Int. Chem. Eng., Vol4, No. 4, p621, 1964.
4	$h(P) = a \left[ 1 - \exp\left(-b \frac{P}{c}\right) \right]^d$	Li & Sellers, Proc. Of 2 <sup>nd</sup> Int. Conf. Modeling of Metals Rolling Processes, The Institute of Materials, London, 1996.

# Contact parameters

## In-line FORTRAN function

LSTC

<b>LCH</b>	<b>= 0</b>	not defined
	<b>&lt; 0</b>	h(temperature)
	<b>&gt; 0</b>	h(time)
	<b>&gt; nlcur</b>	function(time, Tavg, Tslv, Tmsr, pres, gap)

```
*DEFINE_FUNCTION
```

```
101
```

```
h101(pres)=25.+25.e-07*pres+25.e-14*pres**2+25.e-21*pres**3
```

# Contact parameters

## In-line FORTRAN function with load curve

LSTC

```
*DEFINE_FUNCTION_TABULATED
$#      fid      definition
        100      acoef(tavg)

$# title
acoef
$#              tavg              acoef
              0.              25.
              1000.             25.

*DEFINE_FUNCTION
101
h101(pres,tavg)=acoef(tavg)+25.e-07*pres+25.e-14*pres**2
+25.e-21*pres**3
```

# Contact parameters

## Function specified by C program

LSTC

```
*DEFINE_FUNCTION
$#      fid      defintion
      101      h a function of pressure
float contact(float tslv, float tmsr, float pres)
{
  float tmean, acoef, h ;
  tmean=(tslv+tmsr)/2. ;
  acoef=.125*tmean ;
  h=acoef+25.e-07*pres+25.e-14*pres**2+25.e-21*pres**3 ;
  printf ("tmean= %f      acoef= %f      h= %f \n",tmean,acoef,h);
  return (h) ;
}
```

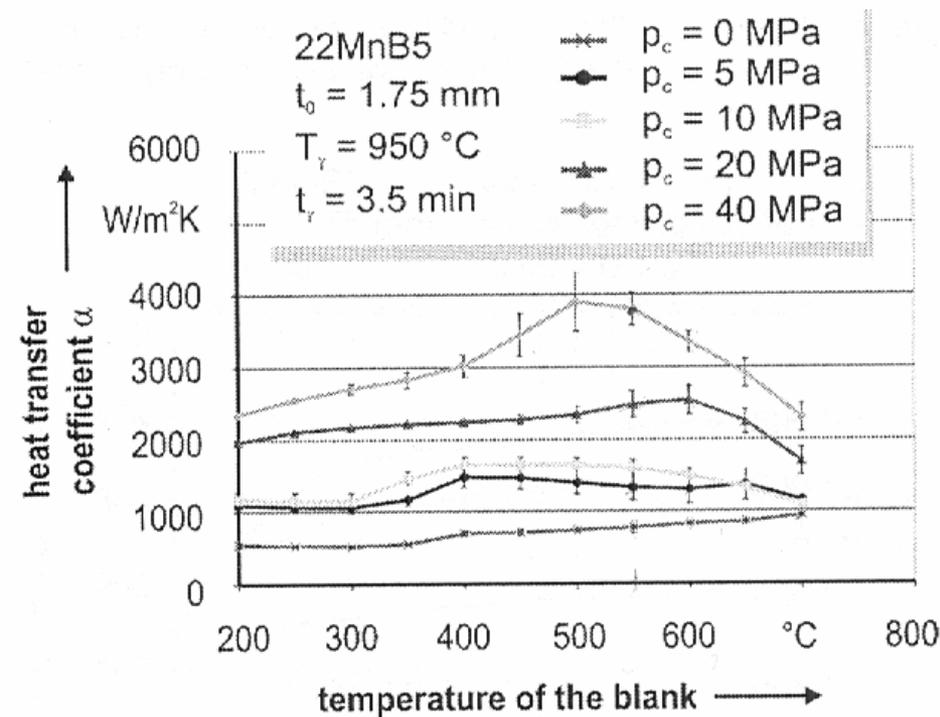
# Contact parameters

## Contact conductance function of pressure

LSTC

M. Merklein and J. Lechler, “Determination of Material and process Characteristics for Hot Stamping Processes of Quenchable Ultra High Strength Steels with Respect to a FE\_based Process design”, SAE Technical Paper 2008-01-0853, April, 2008.

### Numisheet BM03 data

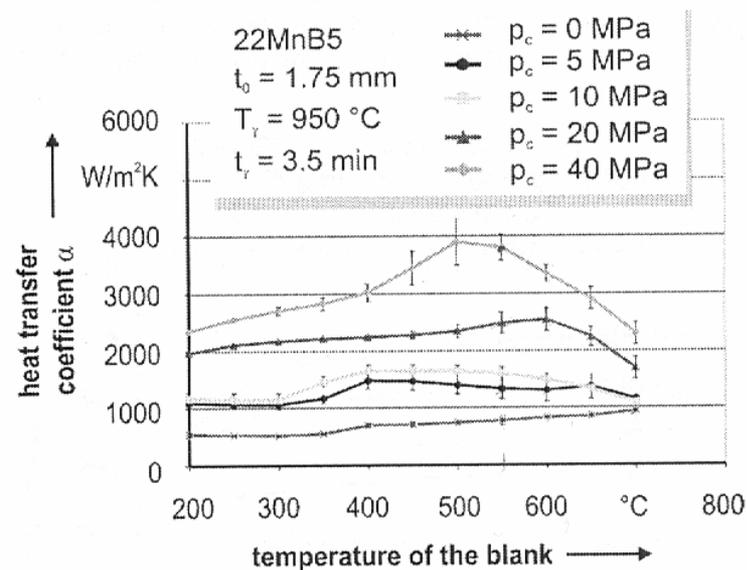


P [MPa]	h [W/m <sup>2</sup> K]
0	1300
20	4000
35	4500

# Contact parameters

## How do you calculate $h(P)$ at the interface

LSTC



P	h @ 550C (curve)	h calculated
0	750	750
5	1330	1330
10	1750	1770
20	2500	2520
40	3830	3830

$$h = \frac{k\pi}{4\lambda} \left[ 1 + 85 \left( \frac{P}{\sigma_r} \right)^{0.8} \right]$$

$h$  = contact conductance [W/m<sup>2</sup>C]

$k$  = air thermal conductivity

0.059 W/mC at 550 C

$\lambda$  = surface roughness [m]

$P$  = interface pressure [MPa]

$\sigma_r$  = rupture stress [MPa]

M. Merklein and J. Lechler, "Determination of Material and process Characteristics for Hot Stamping Processes of Quenched Ultra High Strength Steels with Respect to a FE-based Process design", SAE Technical Paper 2008-01-0853, April, 2008.

I.T. Shvets, "Contact Heat Transfer Between Plane Metal Surfaces", Int. Chem. Eng, Vol 4, No 4, p621, 1964.

# Contact parameters

## How do you calculate $h(P)$ at the interface

LSTC

1. Using curve data, solve the equation for  $\lambda$  at  $(P, h) = (0, 750)$ .

$$750 = \frac{(0.059)\pi}{4\lambda} \left[ 1 + 85 \left( \frac{0}{\sigma_r} \right)^{0.8} \right] \quad \lambda = 61.8e-05$$

2. Using curve data and the above value for  $\lambda$ , solve the equation for  $\sigma_r$  at  $(P, h) = (40, 3830)$ .

$$3830 = \frac{(0.059)\pi}{4(6.18 * 10^{-5})} \left[ 1 + 85 \left( \frac{40}{\sigma_r} \right)^{0.8} \right] \quad \sigma_r = 1765$$

3. Now use the equation to calculate  $h(P)$

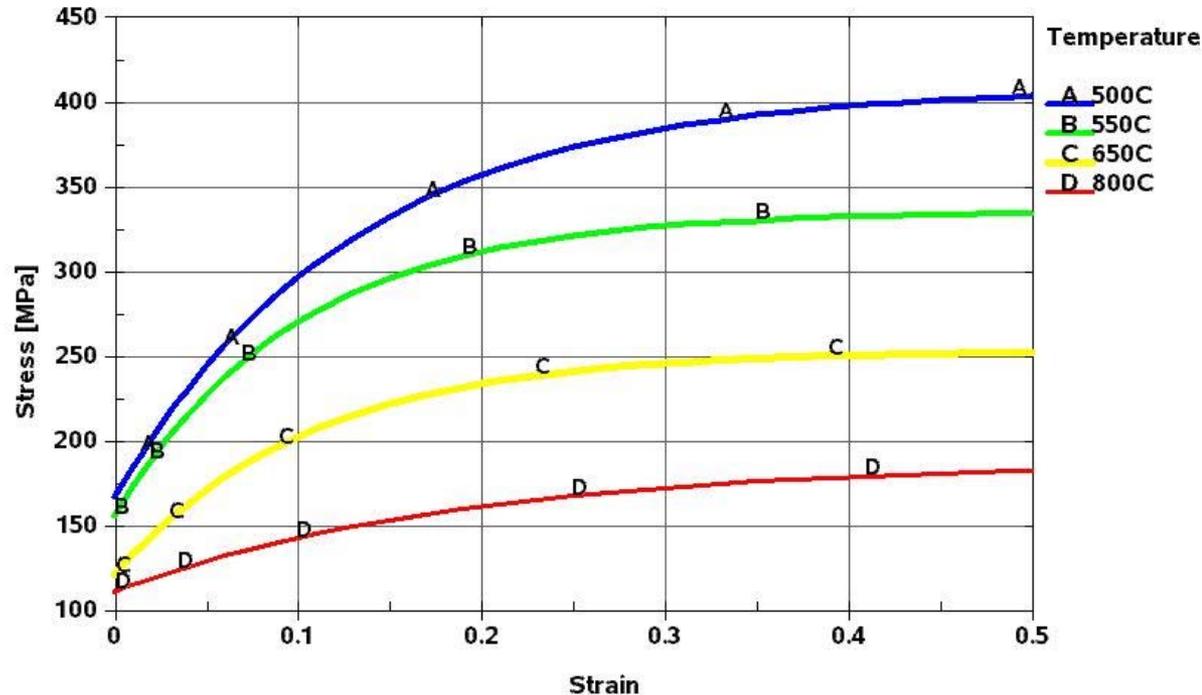
$$h = \frac{(0.059)\pi}{4(6.18 * 10^{-5})} \left[ 1 + 85 \left( \frac{p}{1765} \right)^{0.8} \right]$$

# Numisheet 2008 data for 22MnB5

LSTC

de/dt [s <sup>-1</sup> ]	T [°C]				
	500	550	650	700	800
0.01					
0.1					
1.0					

A material model (MAT\_106) was used that allowed interpolation of the  $\sigma$  vs.  $\epsilon$  data as a function of temperature at a specified strain rate.



# MAT\_106 : Elastic Viscoplastic Thermal

LSTC

1	2	3	4	5	6	7	8
MID	RO	E	PR	SIGY	ALPHA	LCSS	
C	P	LCE	LCPR	LCSIGY			LCALPH
LCC	LCP						

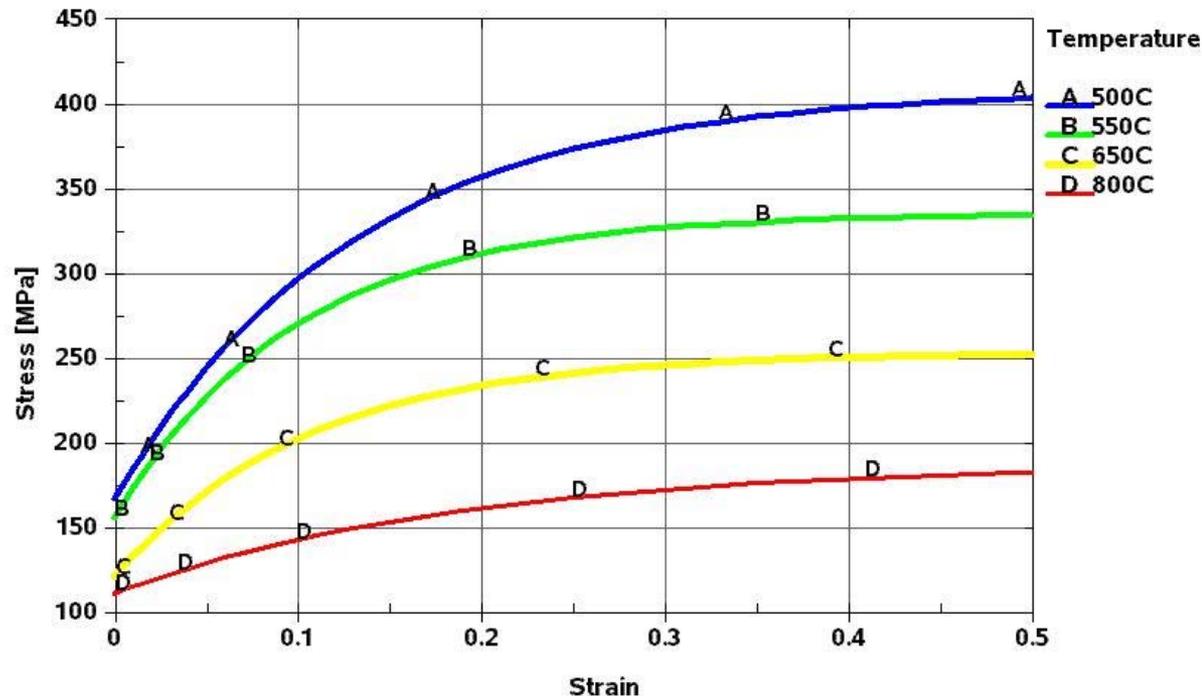
# MAT\_106 : Elastic Viscoplastic Thermal

## How to enter $\sigma$ vs. $\varepsilon$ vs. T

LSTC

```
*DEFINE_TABLE
500
550
650
800
*DEFINE_CURVE
(stress,strain) at T=500
.
*DEFINE_CURVE
(stress,strain) at T=550
.
*DEFINE_CURVE
(stress,strain) at T=650
.
*DEFINE_CURVE
(stress,strain) at T=800
.
```

Material: 22MnB5 ( $d\varepsilon/dt=0.1 \text{ s}^{-1}$ )  
Data from University of Erlangen



# MAT\_106 : Elastic Viscoplastic Thermal

## Cowper and Symonds model

LSTC

Viscous effects are accounted for using the Cowper and Symonds model, which scales the yield stress with the factor

$$1 + \left( \frac{\dot{\epsilon}_{eff}^P}{C} \right)^{1/P}$$

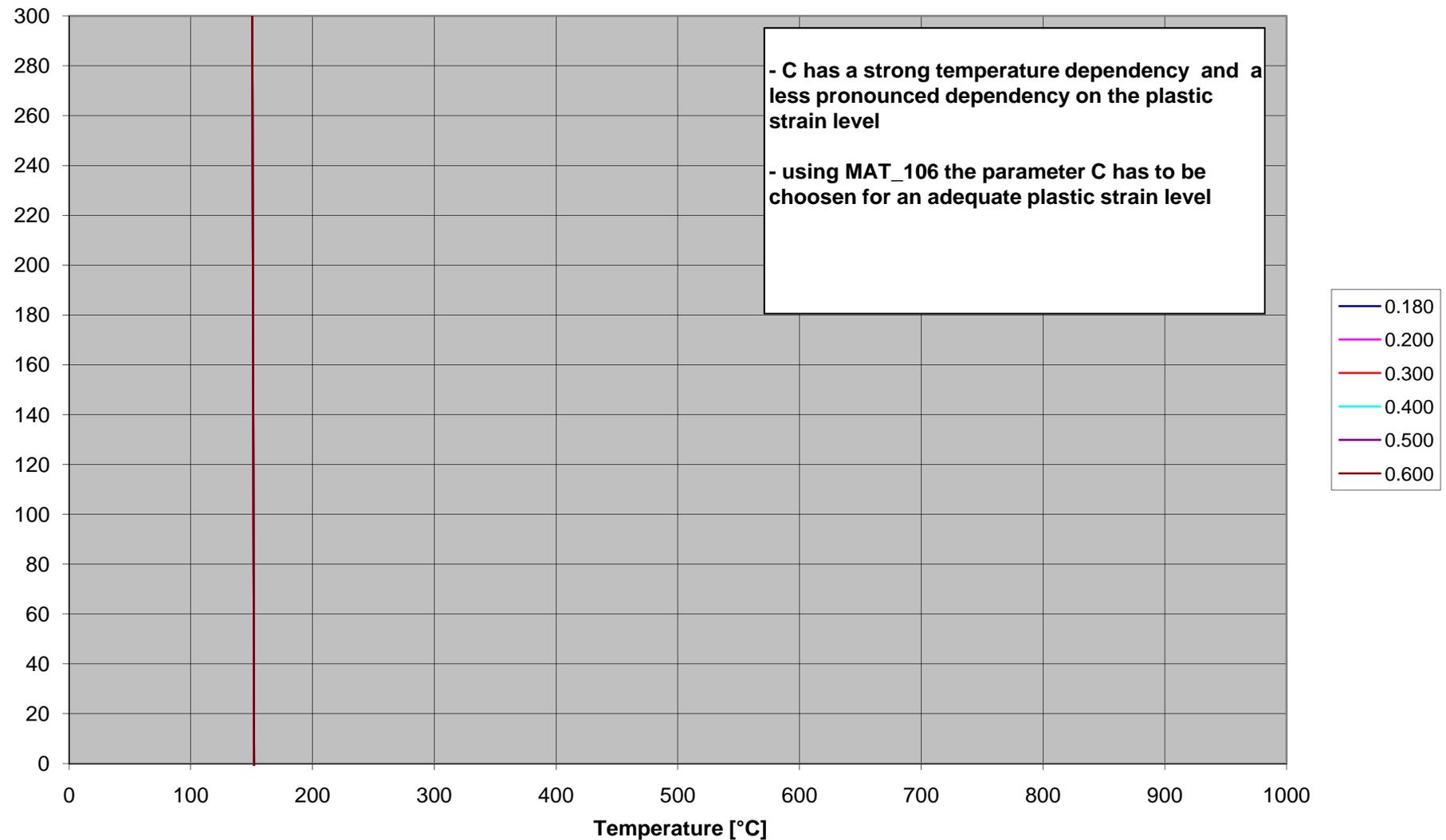
Temp [C]	20	100	200	300	400	500	600	700	800	900	1000
E [MPa]	212	207	199	193	166	158	150	142	134	126	118
v	0.284	0.286	0.289	0.293	0.298	0.303	0.310	0.317	0.325	0.334	0.343
p	4.28	4.21	4.10	3.97	3.83	3.69	3.53	3.37	3.21	3.04	2.87
c	6.2e9	8.4e5	1.5e4	1.4e3	258.	78.4	35.4	23.3	22.2	30.3	55.2

Courtesy of David Lorenz, Dynamore, Stuttgart, Germany.

# MAT\_106 : Elastic Viscoplastic Thermal

## Parameter C vs. T at different plastic strains

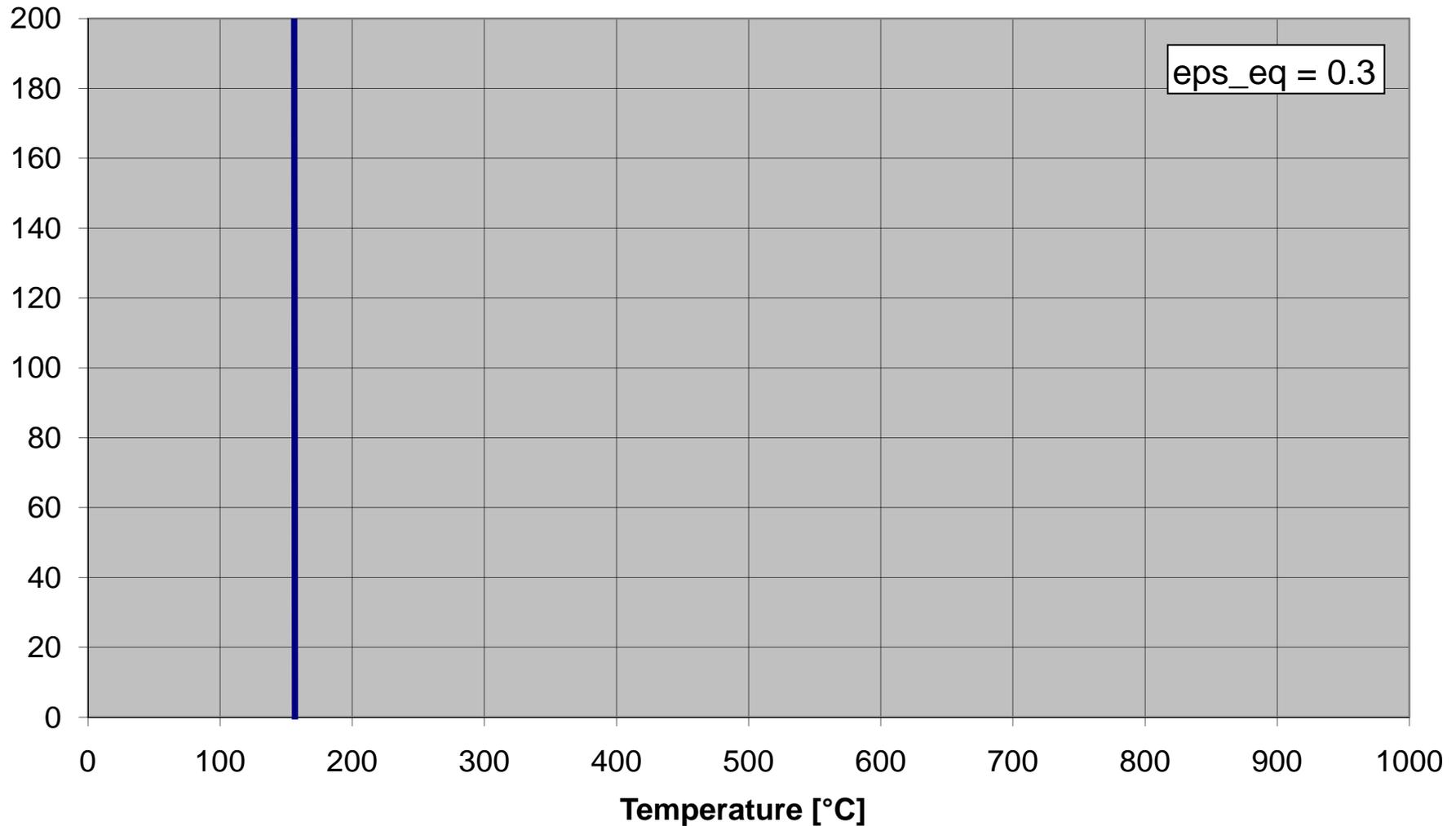
LSTC



# MAT\_106 : Elastic Viscoplastic Thermal

## Parameter C at $\epsilon = 0.3$

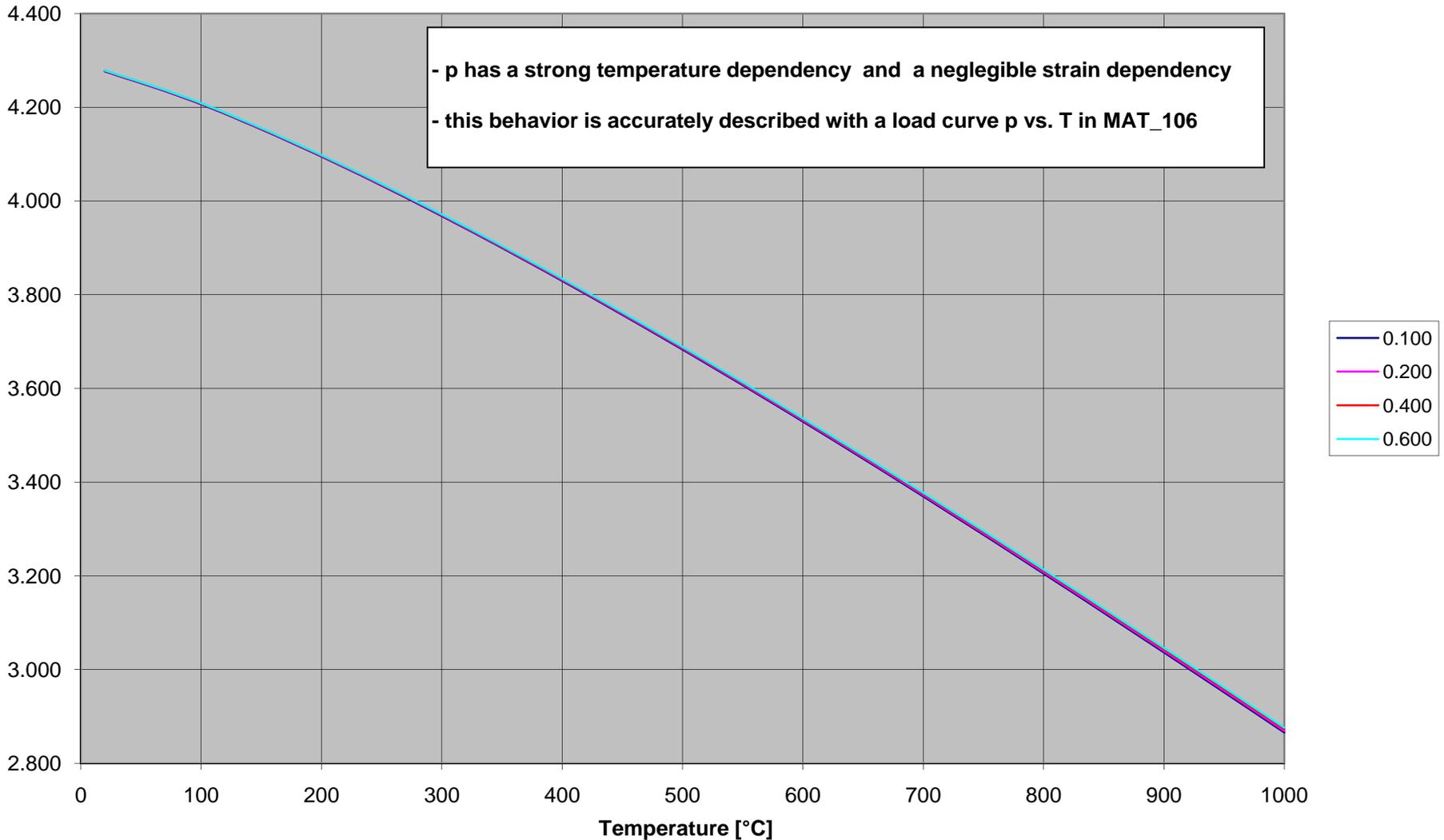
LSTC



# MAT\_106 : Elastic Viscoplastic Thermal

## Parameter p vs. T @ different plastic strains

LSTC



# MAT\_244 : Ultra High Strength Steel

**MAT\_244**  
**MAT\_UHS\_STEEL**

This material model is based on the Ph.D thesis by Paul Akerstrom and implemented by Tobias Olsson (ERAB)

## Input includes:

1. 15 element constituents
2. Latent heat
3. Expansion coefficients
4. Phase hardening curves
5. Phase kinetic parameters
6. Cowper-Symonds parameters

## Output includes:

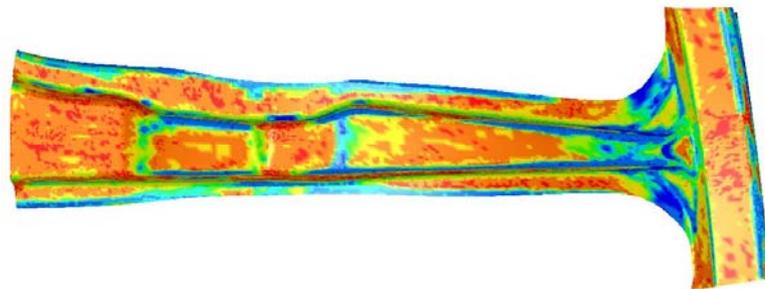
1. Austenite phase fraction
2. Ferrite phase fraction
3. Pearlite phase fraction
4. Bainite phase fraction
5. Martensite phase fraction
6. Vicker's hardness distribution
7. Yield stress distribution

Paul Akerstrom, "Modelling and Simulation of Hot Stamping", Lulea University of Technology, 2006.

# MAT\_244 : Ultra High Strength Steel

Material model predicts phase fractions and hardness.

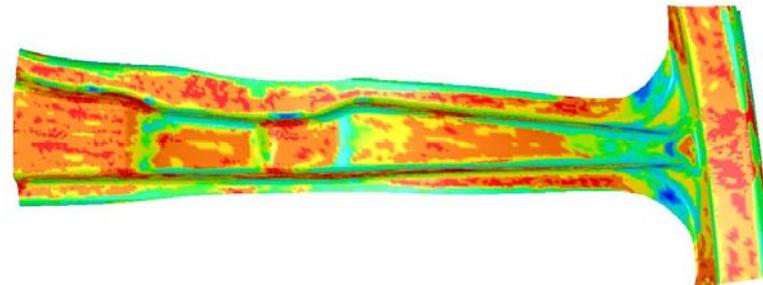
% martensite



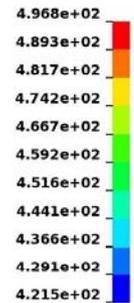
Fringe Levels



Vickers hardness



Fringe Levels



# MAT\_244 : Ultra High Strength Steel

## Boron steel composition, wt%

LSTC

	HAZ	Akerstrom	Naderi	ThyssenKrupp Max. values
B		0.003	0.003	0.005
C	0.168	0.23	0.230	0.250
Co				
Mo	0.036			0.250
Cr	0.255	0.211	0.160	0.250
Ni	0.015			
Mn	1.497	1.25	1.18	1.40
Si	0.473	0.29	0.220	0.400
V	0.026			
W				
Cu	0.025			
P	0.012	0.013	0.015	0.025
Al	0.020			
As				
Ti			0.040	0.05
S		0.003	0.001	0.010

# MAT\_244 : Ultra High Strength Steel

## Phase start temperatures

LSTC

### Start temperature calculation algorithm

$$T_{\text{ferrite}} = A_{e3} = 273 + 912 - 203C^{1/2} - 15.2\text{Ni} + 44.6\text{Si} + 104\text{Va} + 31.5\text{Mo} - 30\text{Mn} - 11\text{Cr} - 20\text{Cu} + 700\text{P} + 400\text{Al} + 120\text{As} + 400\text{Ti}$$

$$T_{\text{pearlite}} = A_{e1} = 273 + 723 - 10.7\text{Mn} - 16.9\text{Ni} + 29\text{Si} + 16.9\text{Cr} + 290\text{As} + 6.4\text{W}$$

$$T_{\text{bainite}} = 273 + 656 - 58\text{C} - 35\text{Mn} - 75\text{Si} - 15\text{Ni} - 34\text{Cr} - 41\text{Mo}$$

$$T_{\text{martensite}} = 273 + 561 - 474\text{C} - 35\text{Mn} - 17\text{Ni} - 17\text{Cr} - 21\text{Mo}$$

Element wt%

Temperature initial condition must be greater than  $T_{\text{ferrite}}$

### Data printed to D3HSP file and messag file

Ferrite	start temperature	= 1.06986E+03
Pearlite	start temperature	= 9.94761E+02
Bainite	start temperature	= 8.43146E+02
Martensite	start temperature	= 6.80303E+02

# MAT\_244 : Ultra High Strength Steel

## Phase change kinetics

LSTC

### austenite to ferrite

$$\frac{dX_f}{dt} = \frac{\exp\left(-\frac{Q_f}{RT}\right)}{C_f} 2^{(G-1)/2} (\Delta T)^3 X_f^{2(1-X_f)/3} (1-X_f)^{2X_f/3}$$

$$C_f = 59.6\text{Mn} + 1.45\text{Ni} + 67.7\text{Cr} + 24.4\text{Mo} + K_f\text{B}$$

### austenite to pearlite

$$\frac{dX_p}{dt} = \frac{\exp\left(-\frac{Q_p}{RT}\right)}{C_p} 2^{(G-1)/2} (\Delta T)^3 DX_p^{2(1-X_p)/3} (1-X_p)^{2X_p/3}$$

$$C_p = 1.79 + 5.42(\text{Cr} + \text{Mo} + 4\text{MoNi}) + K_p\text{B}$$

#### Input parameters

$Q_f$  = activation energy

$Q_p$  = activation energy

$Q_b$  = activation energy

$G$  = grain size

$\alpha$  = material constant

$K_f$  = boron factor

$K_p$  = boron factor

# MAT\_244 : Ultra High Strength Steel

## Phase change kinetics

LSTC

### austenite to bainite

$$\frac{dX_b}{dt} = \frac{\exp\left(-\frac{Q_b}{RT}\right)}{C_b} 2^{(G-1)/2} (\Delta T)^2 DX_b^{2(1-X_b)/3} (1-X_b)^{2X_b/3}$$

$$C_b = 10^{-4}(2.34 + 10.1C + 3.8Cr + 19Mo)Z$$

### austenite to martensite

$$X_m = X_a \left[ 1 - e^{-\alpha(T_{ms} - T)} \right]$$

Empirical equation with  
 $\alpha = 0.011$

A.J. Fletcher, Thermal Stress and Strain Generation in Heat Treatment, 1989, ISBN 1-85166-245-6.

# MAT\_244 : Ultra High Strength Steel

## Hardness calculation is empirically based

LSTC

$$H = (x_f + x_p)H_{f-p} + x_b H_b + x_a H_a$$

$$H_{f-p} = 42 + 223C + 53Si + 30Mn + 12.6Ni + 7Cr + 19Mo \\ + (10 - 19Si + 4Ni + 8Cr + 130V) \ln(dT/dt)_{973}$$

$$H_b = -323 + 185C + 330Si + 153Mn + 65Ni + 144Cr + 191Mo \\ + (89 + 53C - 55Si - 22Mn - 10Ni - 20Cr - 33Mo) \ln(dT/dt)_{973}$$

$$H_a = 127 + 949C + 27Si + 11Mn + 8Ni + 16Cr + 12 \ln(dT/dt)_{973}$$

# MAT\_244 : Ultra High Strength Steel

## Mechanical & Plasticity Material Model

LSTC

Since the material has 5 phases, the yield stress is represented by a mixture law

$$\sigma_y = x_1 \sigma_1 (\bar{\varepsilon}_1^P) + x_2 \sigma_2 (\bar{\varepsilon}_2^P) + x_3 \sigma_3 (\bar{\varepsilon}_3^P) + x_4 \sigma_4 (\bar{\varepsilon}_4^P) + x_5 \sigma_5 (\bar{\varepsilon}_5^P)$$

LC1  
LC2  
LC3  
LC4  
LC5

Where  $\sigma_i (\bar{\varepsilon}_i^P)$  is the yield stress for phase i at the effective plastic strain for that phase.

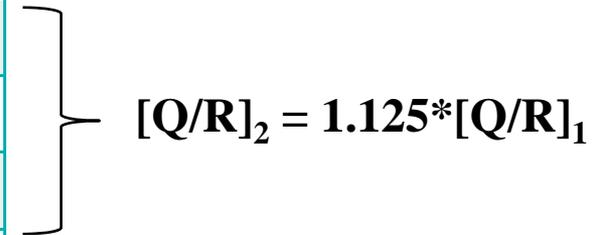
### References

1. T. Olsson, "An LS-DYNA Material Model for Simulations of Hot Stamping Processes of Ultra High Strength Steels", ERAB, April 2009, [tobias.olsson@erab.se](mailto:tobias.olsson@erab.se)
2. P. Akerstrom, Modeling and Simulation of Hot Stamping, Doctoral Thesis, Lulea University of Technology, Lulea, Sweden, 2006.

# MAT\_244 QA parameter study

LSTC

	1	2
$Q_1/R$	11575	13022
$Q_2/R$	13839	15569
$Q_3/R$	13588	15287
$K_f$	1.9e+05	0.
$K_p$	3.1e+03	0.
a	0.011	0.011
G	8	8



$[Q/R]_2 = 1.125*[Q/R]_1$

# MAT\_244 QA parameter study

1

Cooling rate [C/sec]	Vickers Hardness	Ferrite wt%	Pearlite wt%	Bainite wt%	Martensite wt%
200	428	0.0001	0.0010	0.3978	0.5840
100	336	0.0001	0.0031	0.9825	0.0139
40	310	0.0001	0.0188	0.9810	0.0001
20	283	0.0002	0.1193	0.8804	0.0001
10	176	0.0006	0.9993	0.0001	0.0000
5	174	0.0023	0.9976	0.0001	0.0000
2.5	172	0.0125	0.9874	0.0001	0.0000

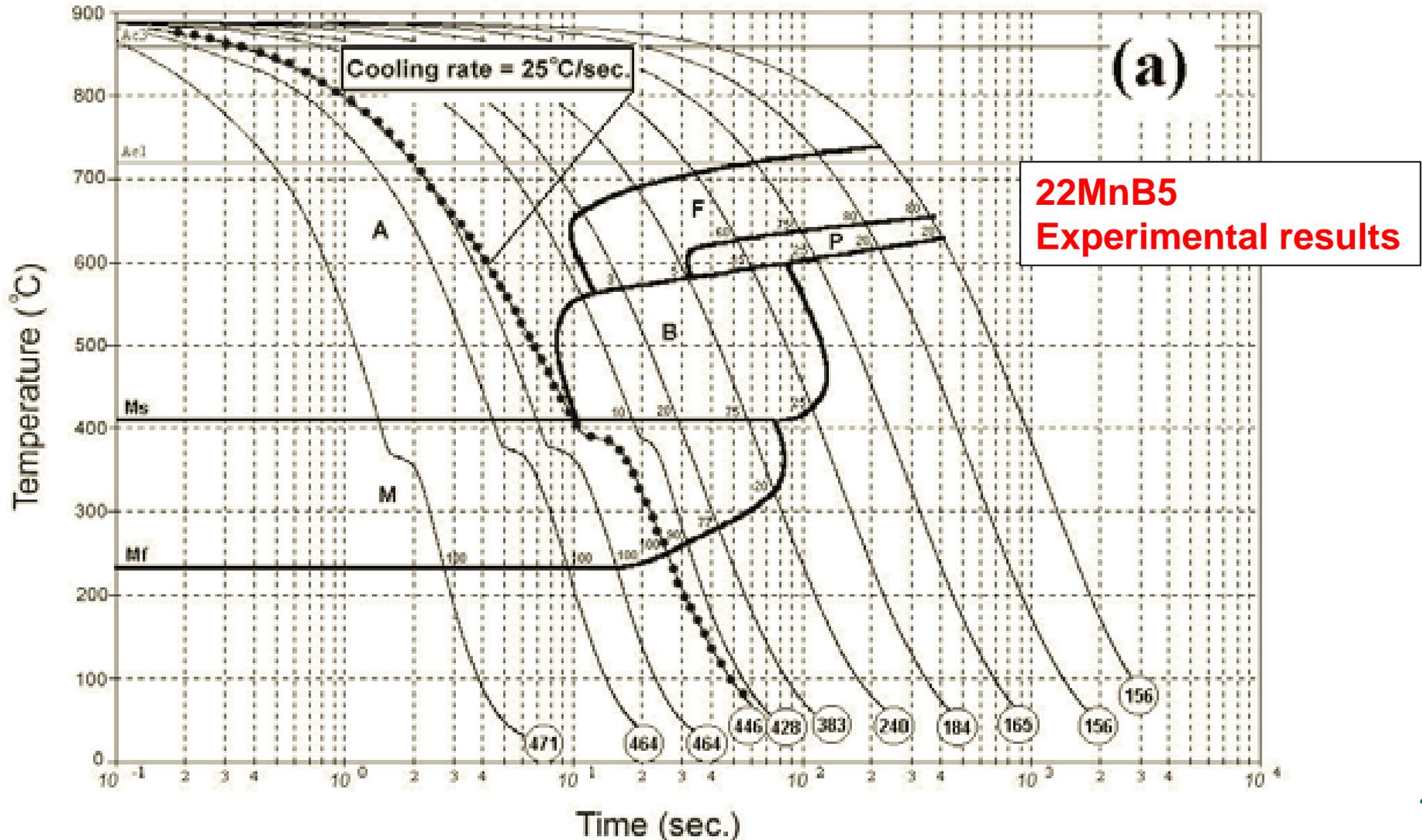
2

Cooling rate [C/sec]	Vickers Hardness	Ferrite wt%	Pearlite wt%	Bainite wt%	Martensite wt%
200	478	0.0001	0.0004	0.0008	0.9692
100	472	0.0001	0.0009	0.0028	0.9668
40	459	0.0002	0.0040	0.0256	0.9416
20	376	0.0005	0.0154	0.4819	0.4880
10	273	0.0018	0.0852	0.9015	0.0111
5	174	0.0093	0.9906	0.0001	0.0000
2.5	172	0.7023	0.2976	0.0000	0.0000

# MAT\_244 QA parameter study

M. Naderi, Thesis 11/2007, Dept. Ferrous Metallurgy, RWTH Aachen University, Germany

LSTC

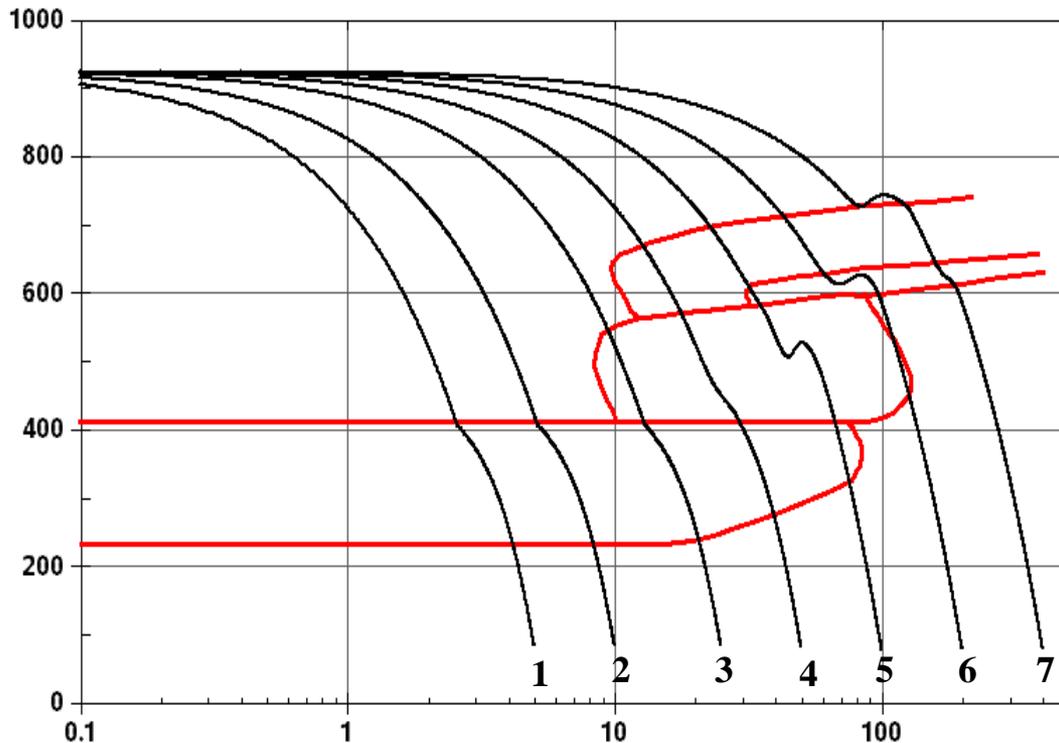


# MAT\_244 QA parameter study

## Using data set 2

LSTC

CCT Diagram for 22MnB5 overlaid with LS-DYNA calculated cooling curves and Vickers hardness using MAT\_UHS\_STEEL

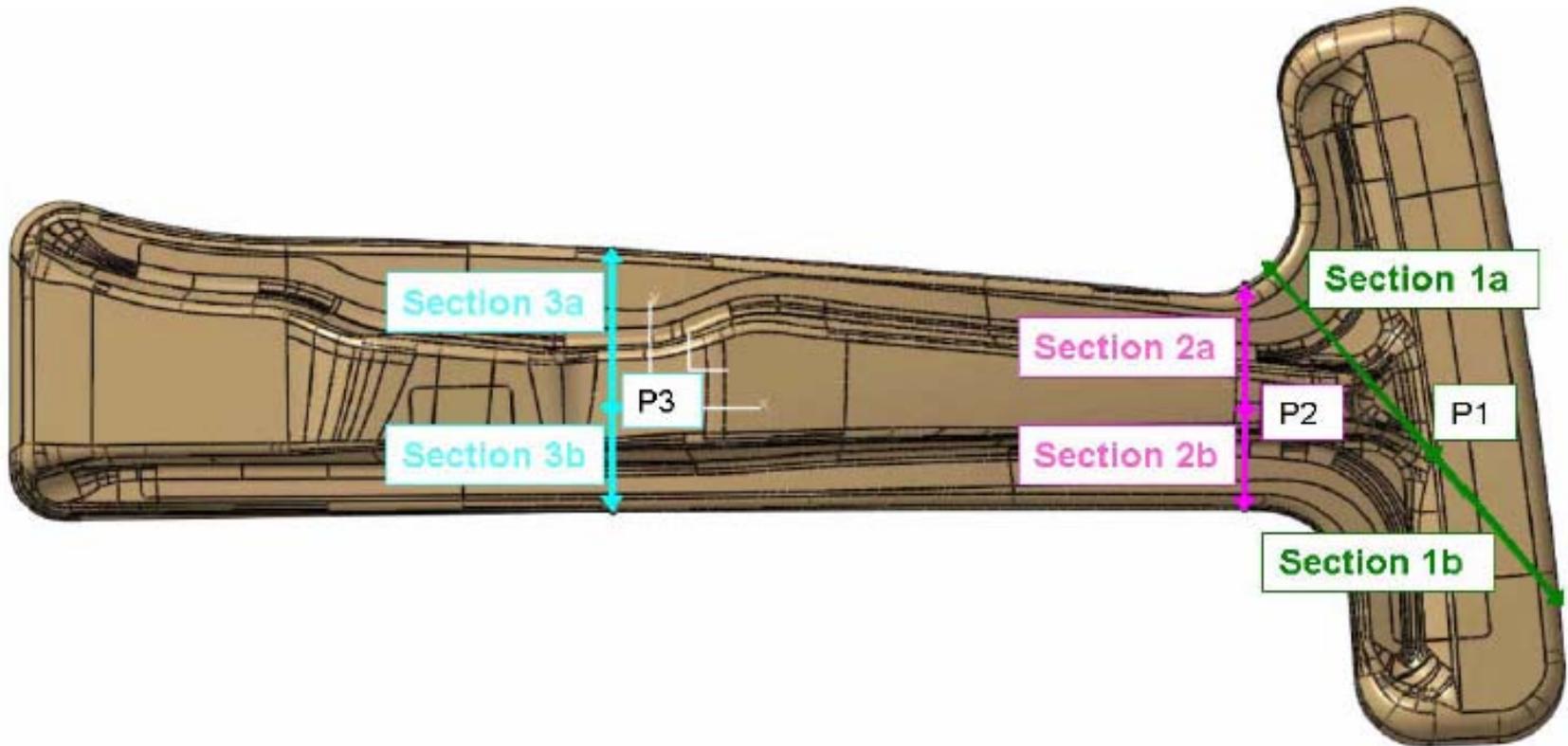


	Rate C/sec	Vickers Hardness	Exp. Naderi
1	200	478	-----
2	100	472	471
3	40	459	428
4	20	376	383
5	10	273	240
6	5	174	175
7	2.5	172	165

# MAT\_244 QA parameter study

## Numisheet Benchmark BM03

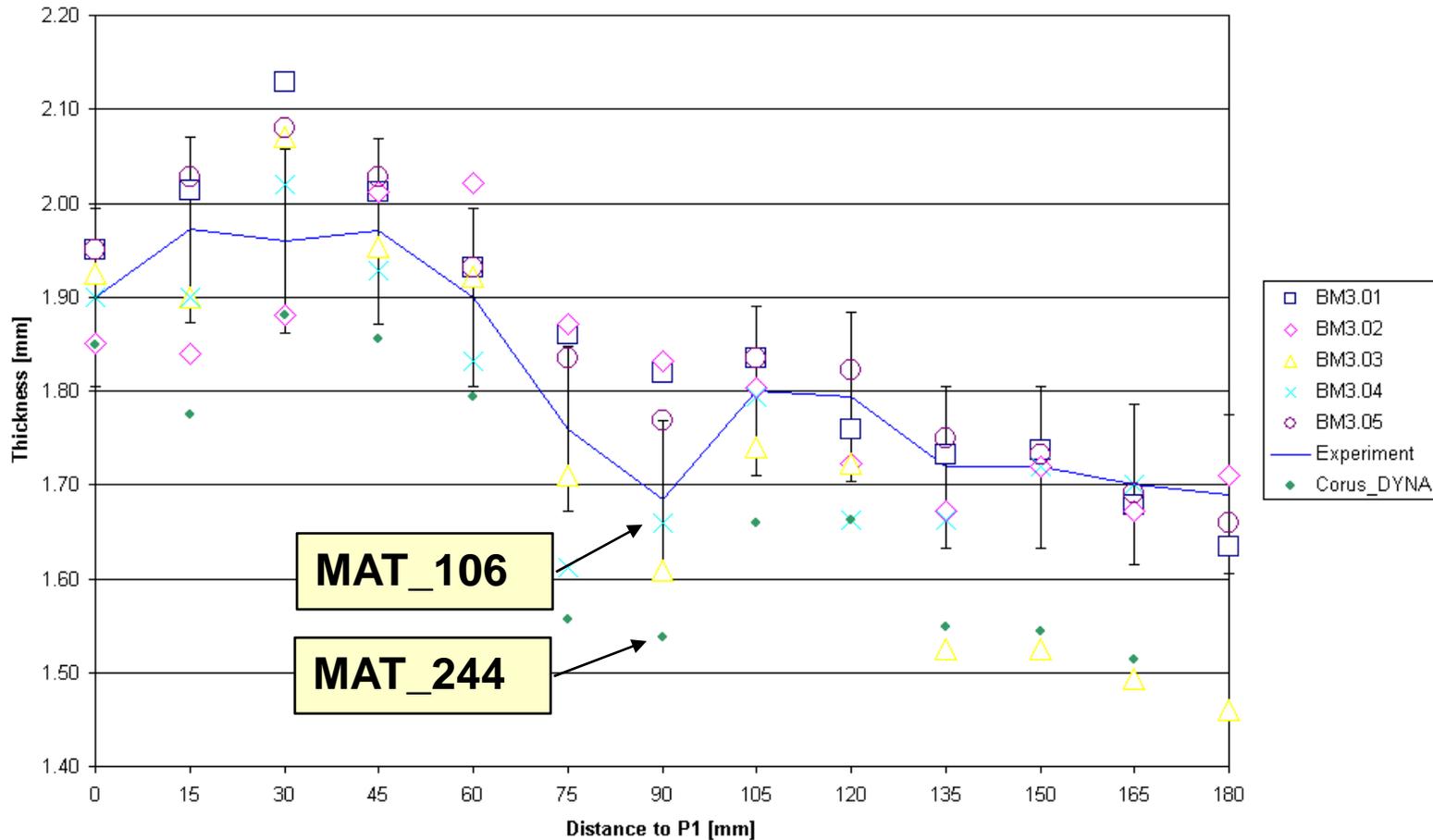
LSTC



# MAT\_244 QA parameter study

## Numisheet Benchmark BM03 section 1a

LSTC



By: Sander van der Hoorn, Corus, The Netherlands

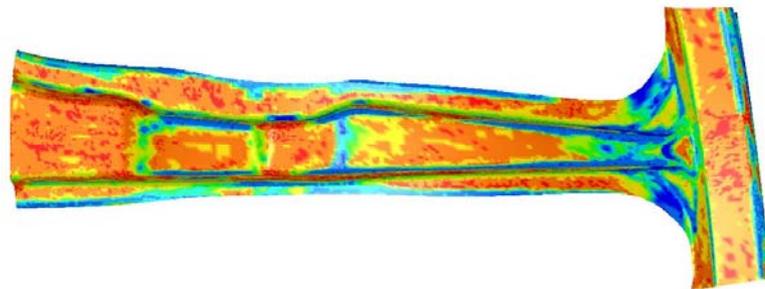
# MAT\_244 QA parameter study

## Numisheet BM03 benchmark problem

LSTC

Material model predicts phase fractions and hardness.

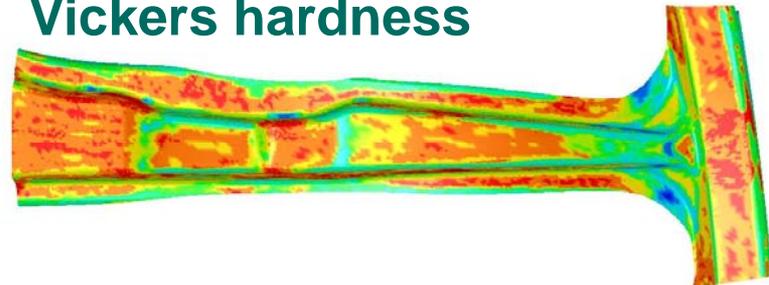
% martensite



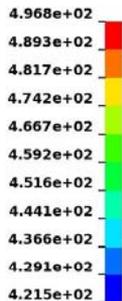
Fringe Levels



Vickers hardness

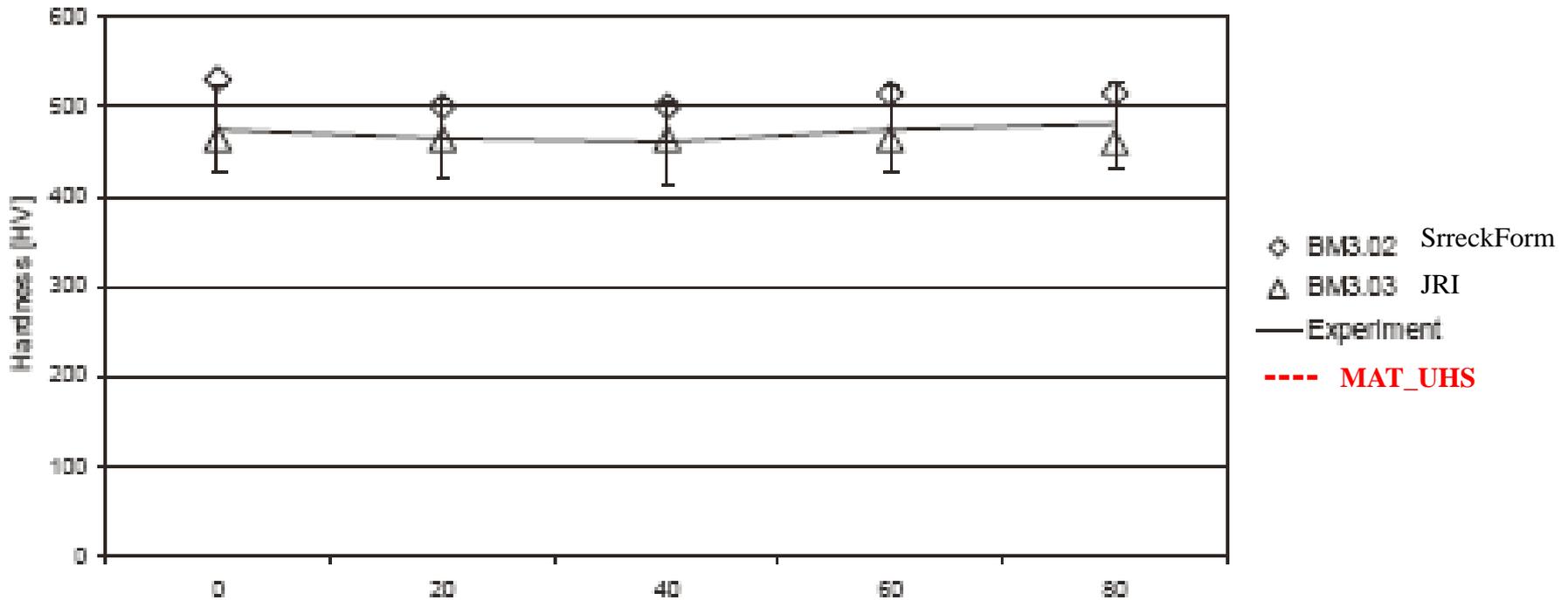


Fringe Levels



# MAT\_244 QA parameter study

## Vickers hardness for section 2b



# Numisheet 2008 BM03 Model & Simulation

## Forming process

LSTC

### FE model

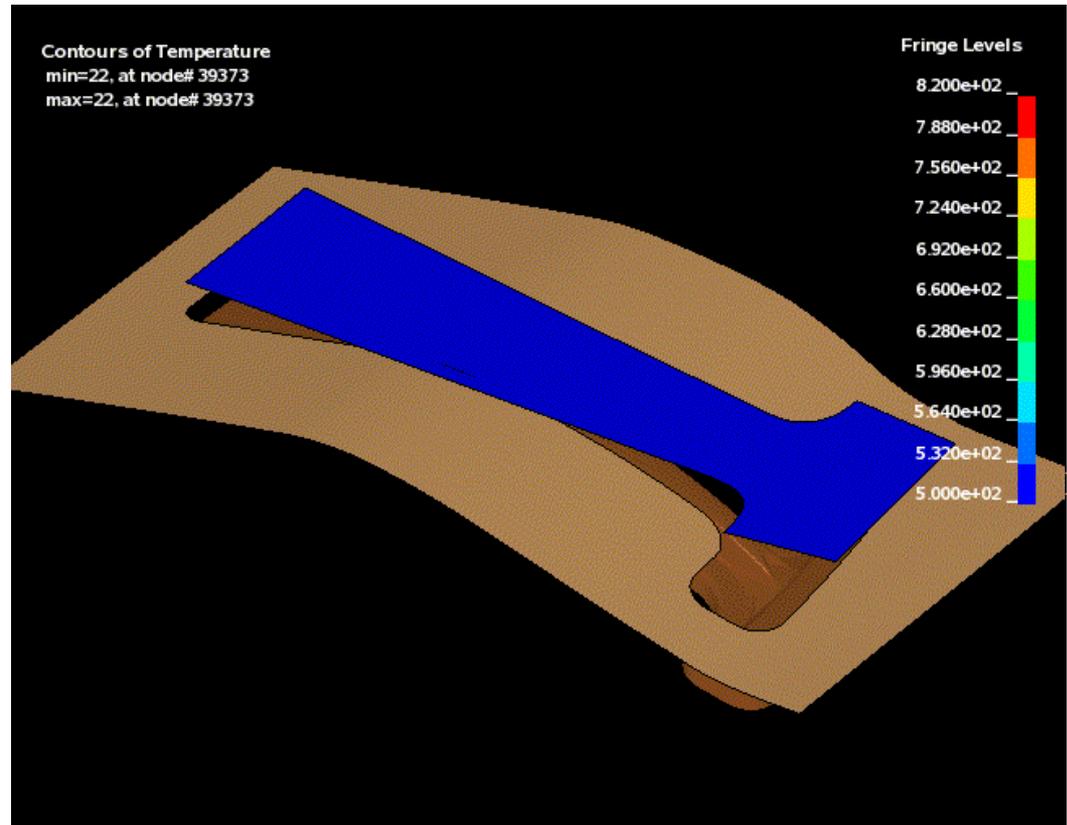
**Tools:** 68,268 rigid shells  
**Blank:** 3,096 deformable shells  
increasing to 11,682 after  
adaptivity

**Run time:**  
INTEL Core Quad CPU @ 2.40GHz

1 cpu → 5.10 hr  
2 cpu → 3.96 hr  
4 cpu → 2.65 hr

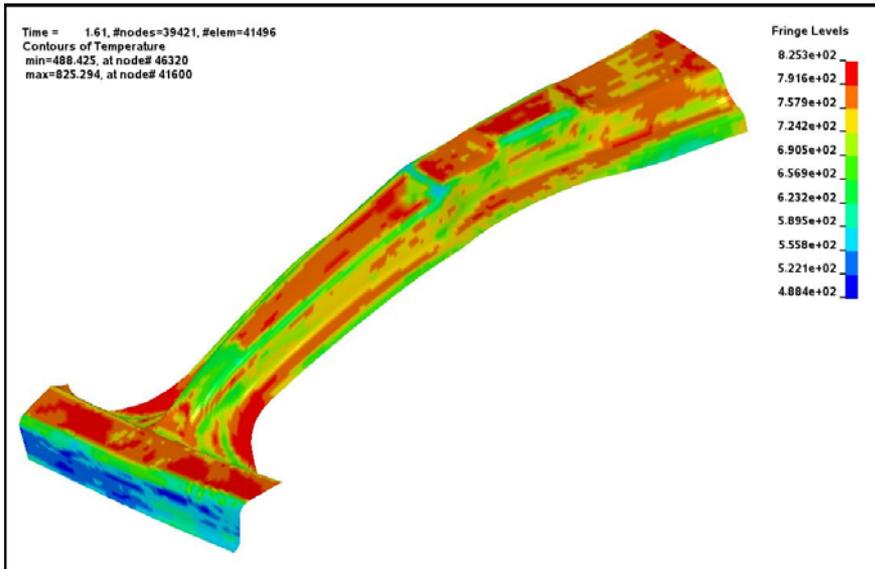
### Time step

- mechanical 1.e-05
- thermal 1.e-03

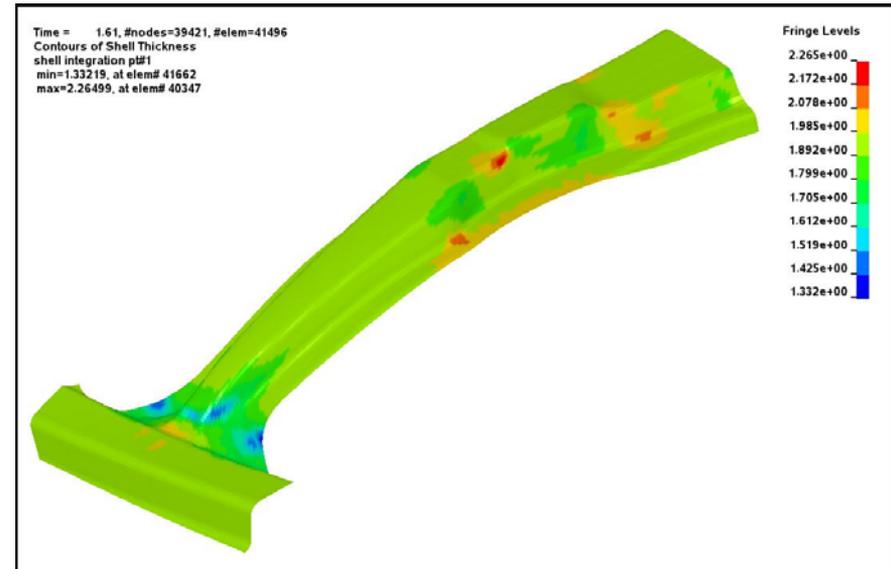


# Numisheet 2008 BM03 Simulation

## Results after forming



**Temperature**  
min = 488C  
max = 825C



**Thickness**  
min = 1.33mm  
max = 2.26mm

# Numisheet 2008 BM03 Simulation

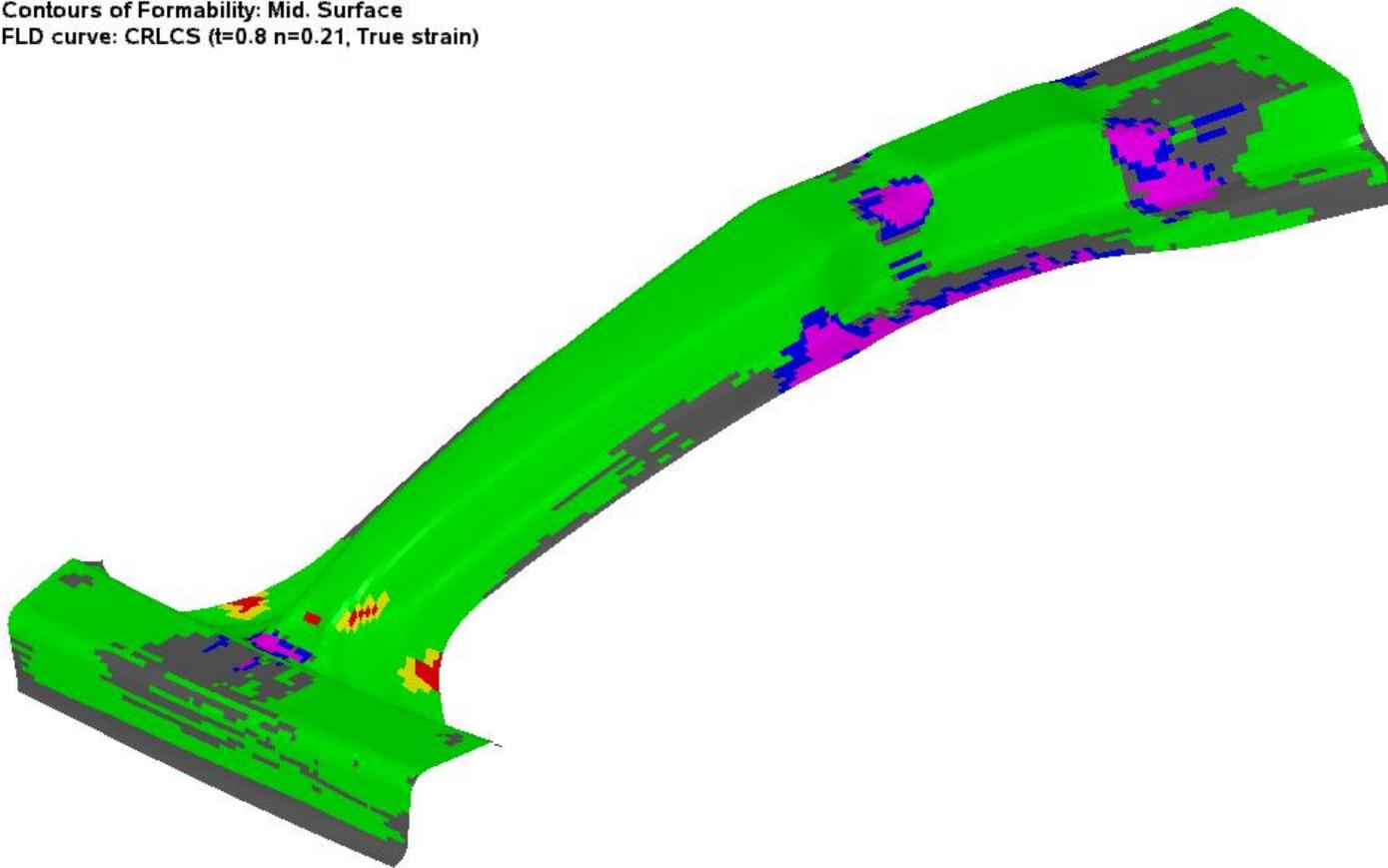
## FLD

LSTC

Time = 1.61, #nodes=39421, #elem=41496  
Contours of Formability: Mid. Surface  
FLD curve: CRLCS (t=0.8 n=0.21, True strain)

Formability key

Cracks	Red
Risk of cracks	Yellow
Severe thinning	Orange
Good	Green
Inadequate stretch	Grey
Wrinkling tendency	Blue
Wrinkles	Purple

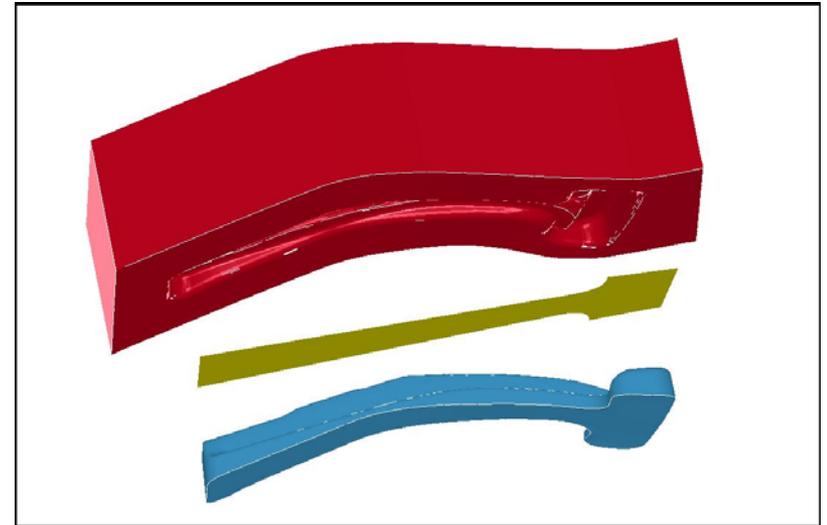
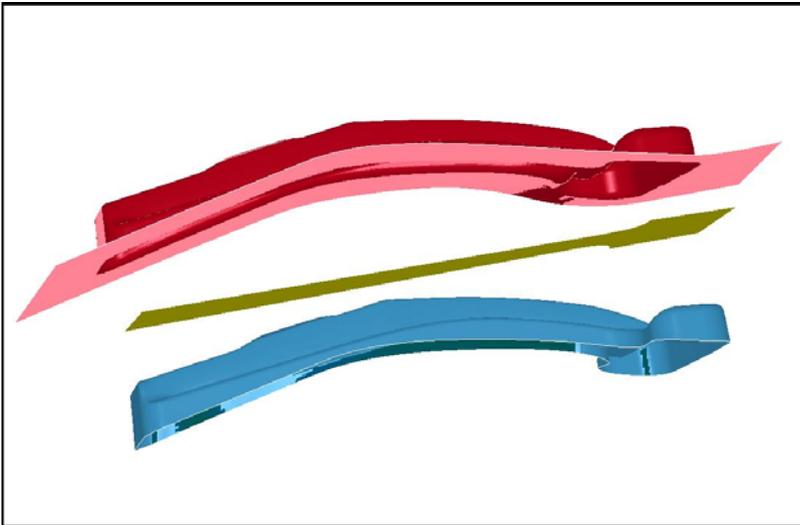


# Numisheet 2008 BM03 Simulation

## Quench: hold time in the tool 20 sec

LSTC

Modeling the **cooling rate** correctly is critical in determining the material phase composition and the material hardness. The local cooling rate is affected by the heat transfer between the blank and tools. The tools must be modeled using solid elements as shown in the figure below for an accurate calculation. We did not do this for the benchmark. Our FE model used shells for the tools fixed at the specified tool temperature of 75C.



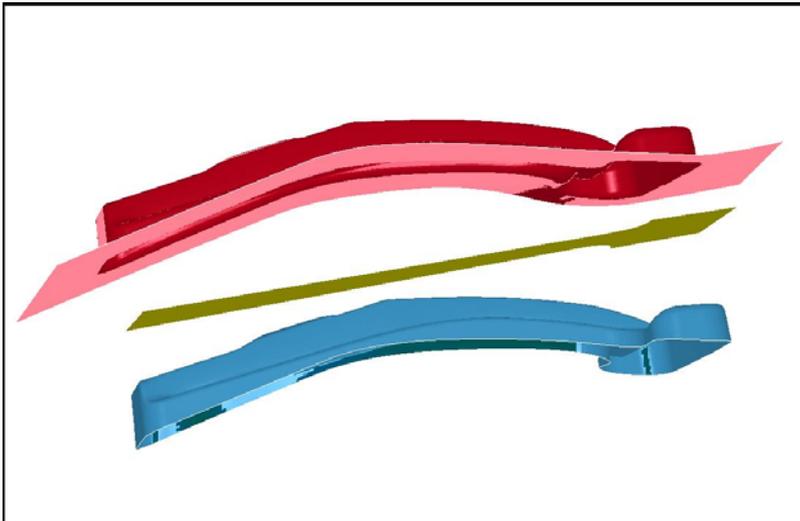
**shell model  $dT/dt > \text{solid model } dT/dt$**

# Numisheet 2008 BM03 Simulation

LSTC

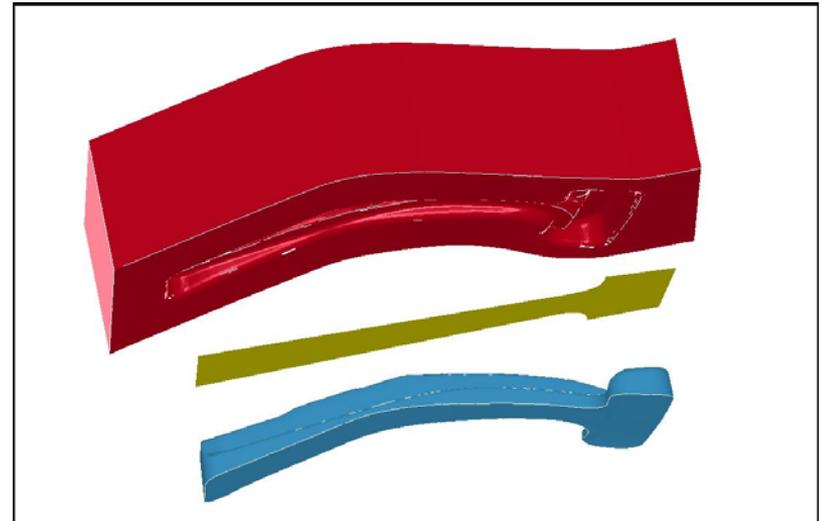
## Shell geometry (5.0hr run time)

- 68,268 rigid shells
- 3,096 deformable shells
- 11,682 shells after adaptivity



## Solid geometry (5.9hr run time)

- 532,927 solids (punch & die)
- 6,692 shells (holder)
- 3,096 deformable shells (blank)
- 11,682 shells after adaptivity

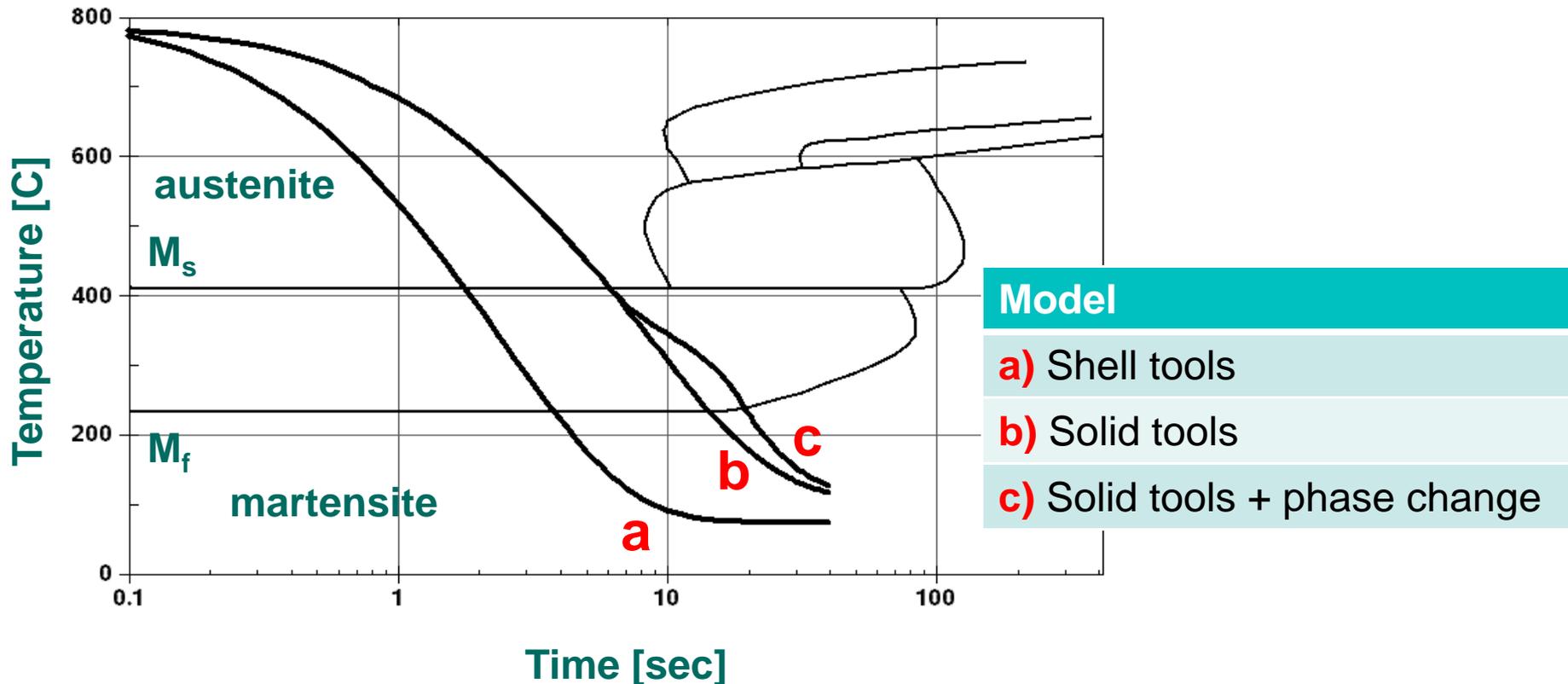


# Numisheet 2008 BM03 Simulation

## Cool down to room temperature

LSTC

CCT diagram for 22MnB5 steel

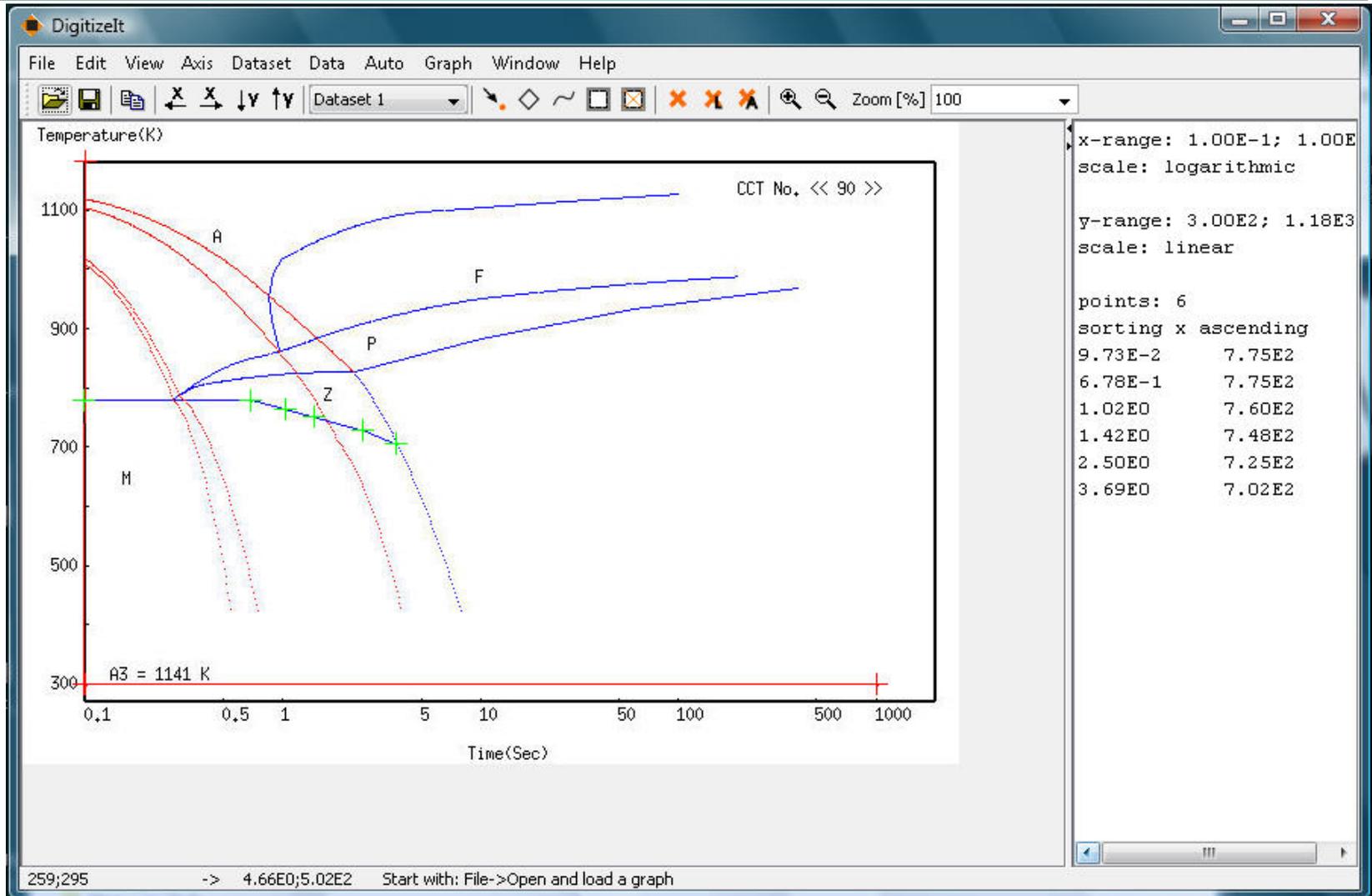


Our benchmark results are depicted by curve (a). Subsequently, we looked at the affect when using solid tools (b) and including phase change (c). The cooling rate is much slower.

# Creating a CCT diagram

Digitzelt, <http://www.digitizeit.de/>

LSTC



# Creating a CCT diagram

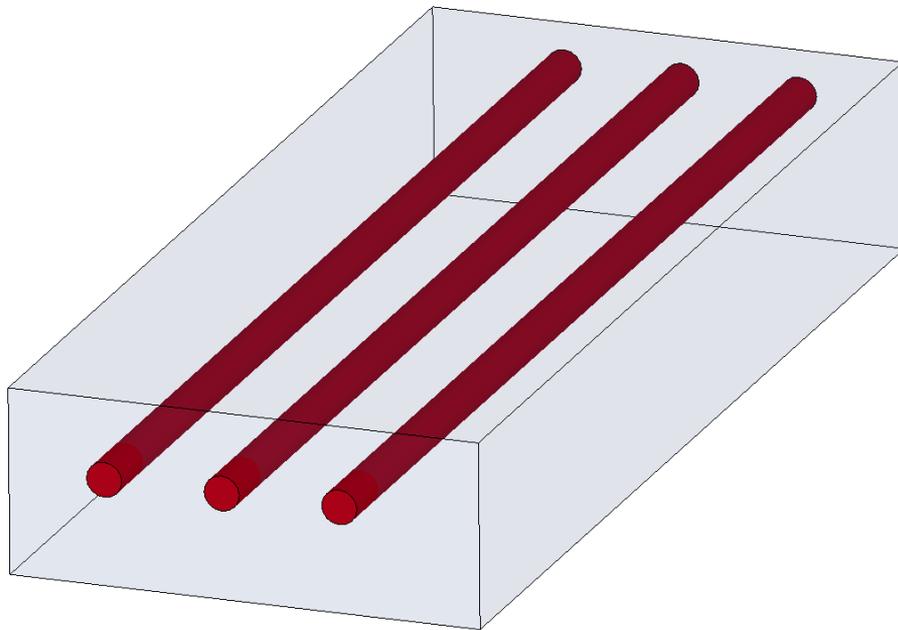
1. Obtain an image of a CCT diagram (e.g., from <https://inaba.nims.go.jp/Weld/cct/>)
2. Use software to digitize curves (e.g, Digitizeit, <http://www.digitizeit.de/> ) and save as xy-data
3. Using LS-PrePost, plot temperature history of one or more nodes and save as xy-data
4. Import xy-data into LS-PrePost and display curves on a single plot

# Modeling tool cooling

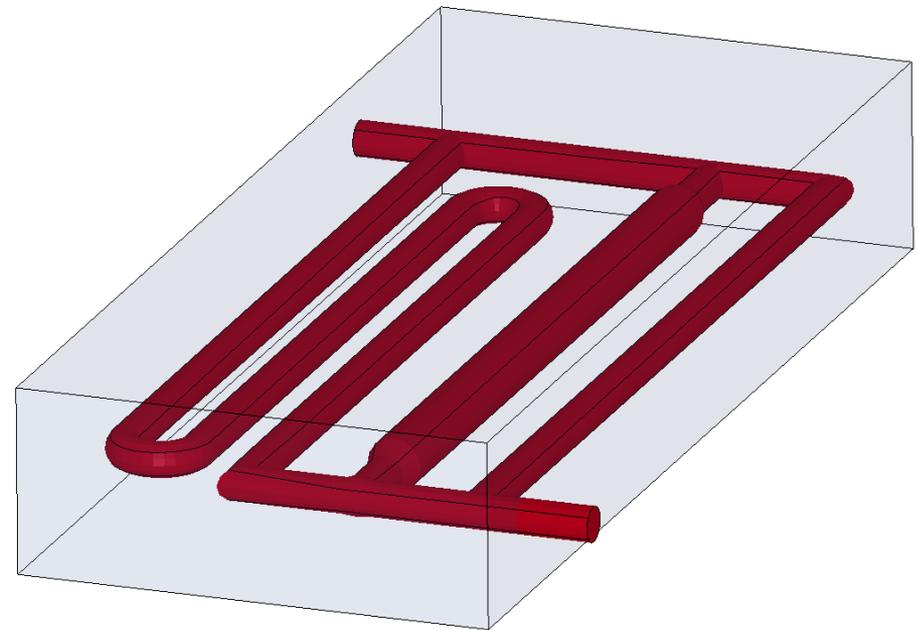
There are 2 methods to model fluid flow

LSTC

**BULKFLOW**



**Network Analyzer**

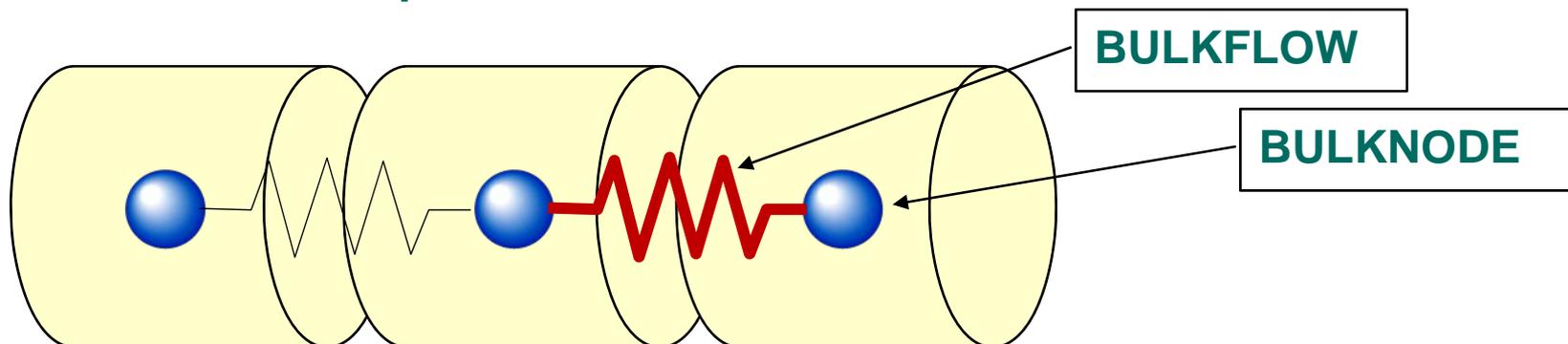
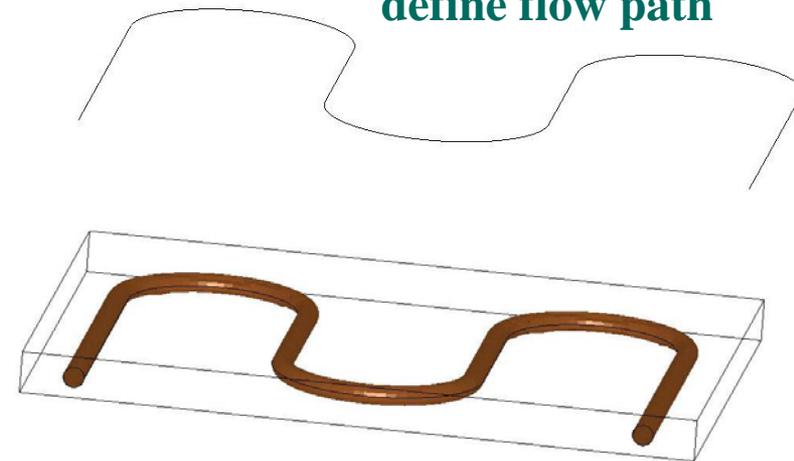


# BULKNODE and BULKFLOW method

LSTC

**BULK FLOW** is a lumped parameter approach to model fluid flow in a pipe. The flow path is defined with a contiguous set of beam elements. The beam node points are called **BULK NODES** and have special attributes in addition to their (x,y,z) location. Each **BULKNODE** represents a homogeneous slug of fluid. Using the **BULKFLOW** keyword we define a mass flow rate for the beams. We then solve the advection-diffusion equation.

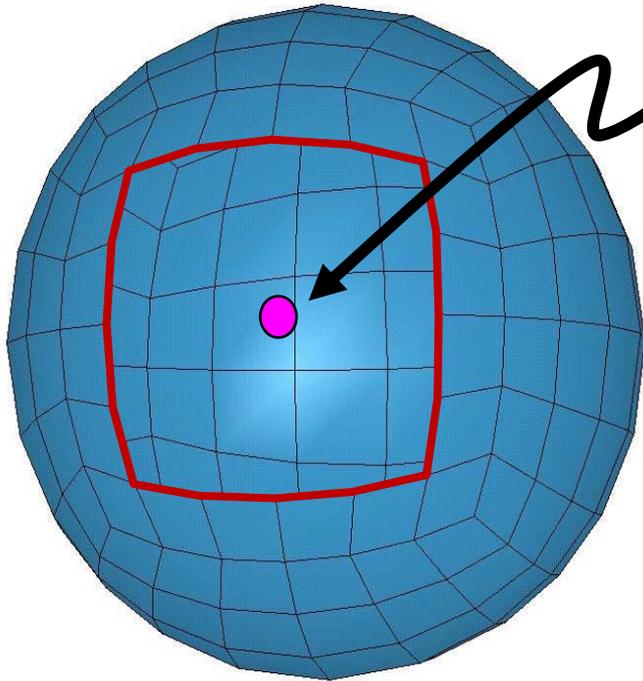
Beam elements  
define flow path



# BULKNODE – modeling a gas or fluid in a container

## \*BOUNDARY\_THERMAL\_BULKNODE

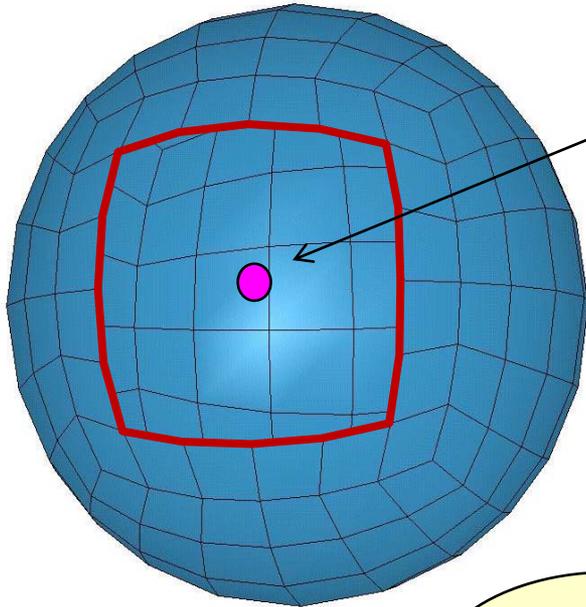
LSTC



**BULKNODE** -This is a lumped parameter approach to model a fluid inside a rigid container. A node is defined with a **specified volume, density, and heat capacity**. The node coordinates are arbitrary, but it makes sense to place the node in the correct geometric position for visualization. The **surface segments** of the container are also defined so the bulk node can exchange heat by convection and radiation to the container.

Note that we are not modeling conduction in the fluid. The entire fluid volume is homogeneous at temperature  $T$ . The fluid temperature changes due to convection and radiation heat exchange with the container.

# BULKNODE – modeling a gas or fluid in a container



The heat flow between the bulk node, B, and the surrounding surface, S, is given by

$$\dot{q}'' = h(T_S^a - T_B^a)^b$$

The value of h has the greatest uncertainty. The section on “How do you determine h” shows a hand calculation. Or, you may run a CFD code to numerically determine h.

# **BULKNODE** – modeling a gas or fluid in a container

## **BOUNDARY\_THERMAL\_BULKNODE** keyword

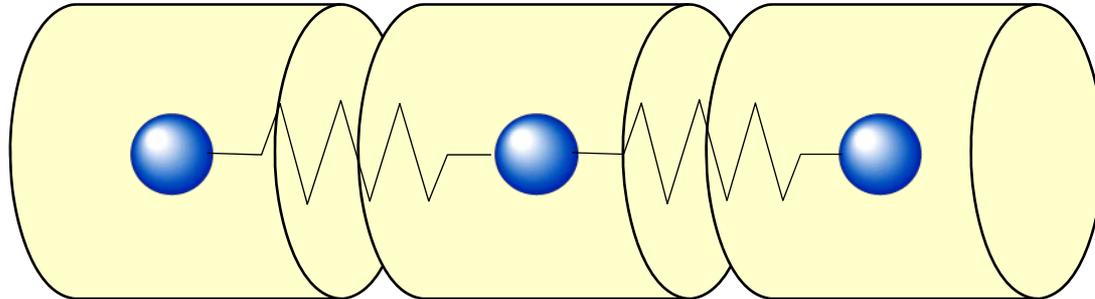
LSTC

### **\*BOUNDARY\_THERMAL\_BULKNODE**

**NID PID NBNSEG VOL LCID H A B**

<b>NID</b>	bulk node number
<b>PID</b>	this bulk node is assigned a PID which in turn assigns material properties
<b>NBNSEG</b>	number of surface segments surrounding the bulk node
<b>VOL</b>	volume of bulk node (i.e., cavity volume – calculated by LSPP during mesh generation)
<b>LCID</b>	load curve ID for heat transfer coefficient h
<b>H</b>	heat transfer coefficient h
<b>A</b>	exponent a
<b>B</b>	exponent b

# BULKFLOW – modeling flow through a pipe



Using the **BULKFLOW** keyword we define a mass flow rate for the beams connecting the **BULKNODES**. We then solve the advection-diffusion equation.

$$\rho c \frac{\partial T}{\partial t} + \rho c V \frac{\partial T}{\partial x} = K \frac{\partial^2 T}{\partial x^2}$$

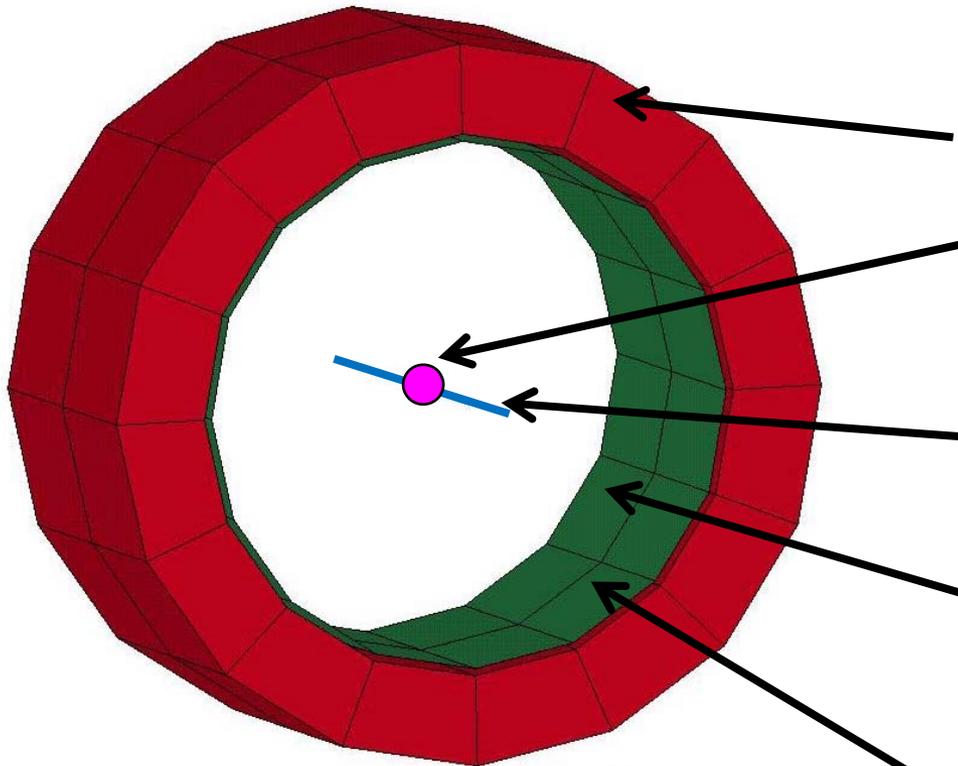
\*BOUNDARY\_THERMAL\_BULKFLOW\_ { ELEMENT SET

EID LCID MDOT

# Modeling flow through a pipe

Five entities are required

1. **Pipe / Die** – solid elements.
2. **BULKNODE**– defines fluid properties, fluid volume and heat transfer to surface layer.
3. **BULKFLOW**– beam elements define the flow path (centerline of the pipe).
4. **Surface layer** – shell elements define the outer boundary surface of the fluid.
5. **Contact** - used to connect dissimilar surface layer to pipe mesh.



LS-PrePost can create these entities

# Modeling flow through a pipe

## Required keywords

LSTC

**\*PART**

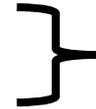
**\*ELEMENT\_SOLID**



**1. define pipe / die**

**\*PART**

**\*BOUNDARY\_THERMAL\_BULKNODE**



**2. define bulk node**

**\*PART**

**\*ELEMENT\_BEAM**

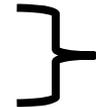
**\*BOUNDARY\_THERMAL\_BULKFLOW\_ELEMENT**



**3. define bulk flow**

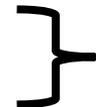
**\*PART**

**\*ELEMENT\_SHELL**



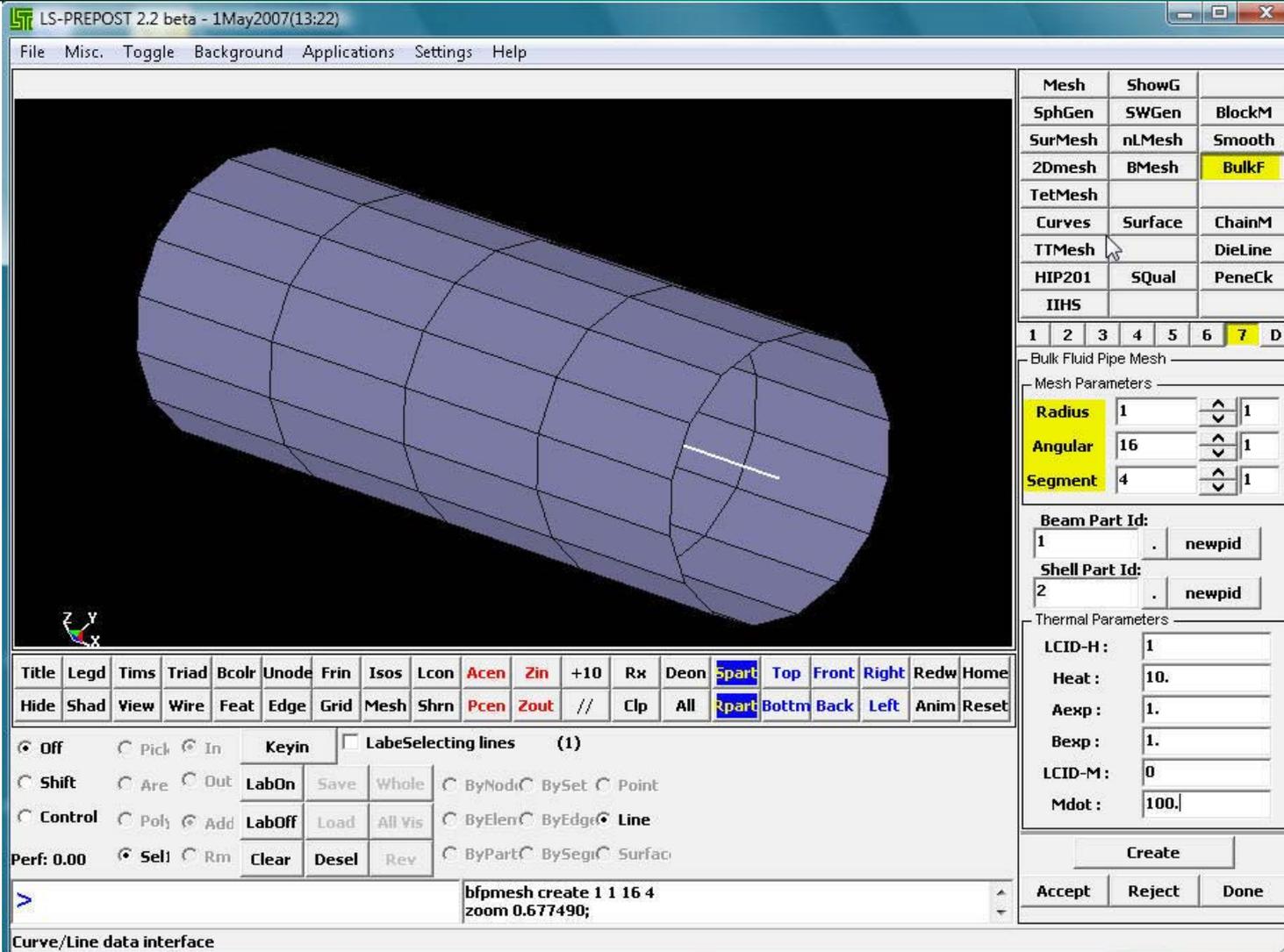
**4. define surface layer**

**\*CONTACT\_SURFACE\_TO\_SURFACE**



**5. Fluid structure interaction**

# Using LS-PrePost to create BULKNODE & BULKFLOW keywords



Bulk flow button

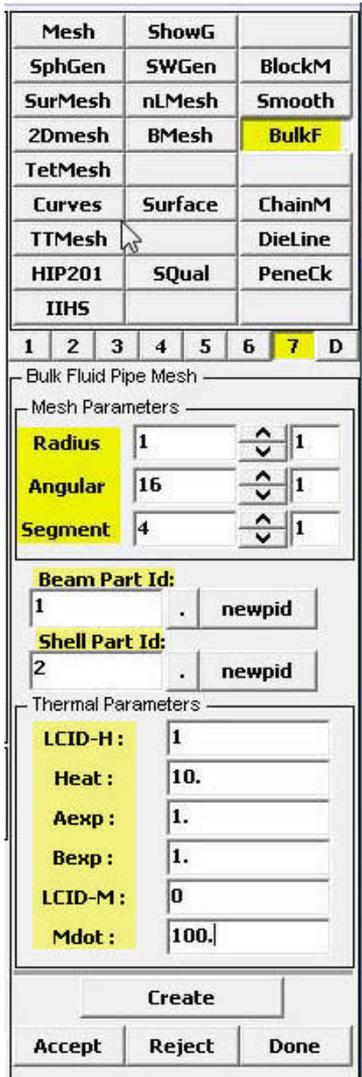
Screen 7

Mesh

Part definitions

Fluid structure interaction

# Using LS-PrePost to create BULKNODE & BULKFLOW keywords



**Bulk flow button**

**Generate mesh**

- radius of pipe
- number of angular segments
- number of axial segments

**Screen 7**

**Beam PID - used to associate fluid material properties to the BULKFLOW elements.**

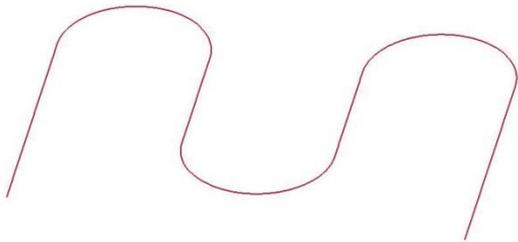
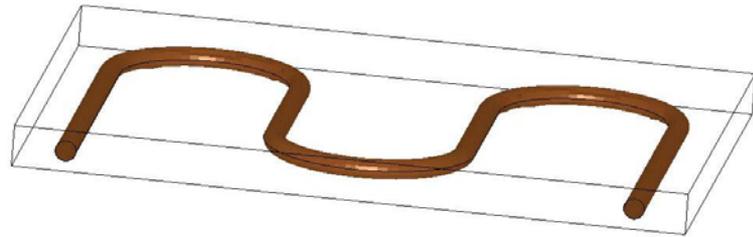
**Shell PID - used to associate fluid material properties to the BULKNODES and shell outer surface layer.**

**Fluid structure interaction  $\dot{q}'' = h(T_s^a - T_b^a)^b$**

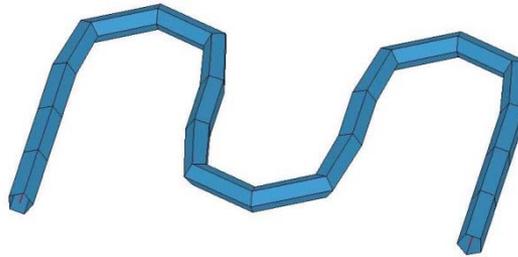
**Fluid mass flow rate**

# Using LS-PrePost to create BULKNODE & BULKFLOW keywords

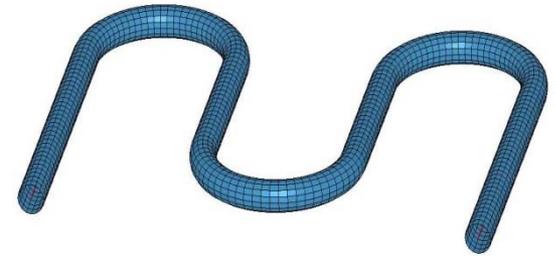
Shown is a serpentine flow channel passing through a die



Curve defining flow path



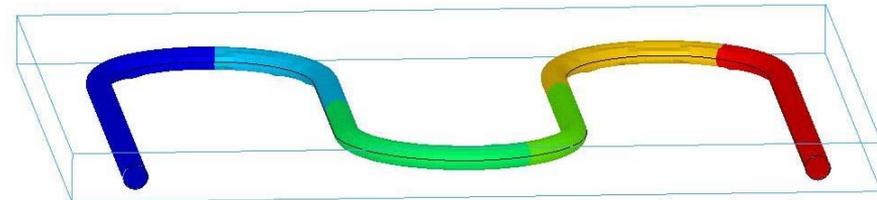
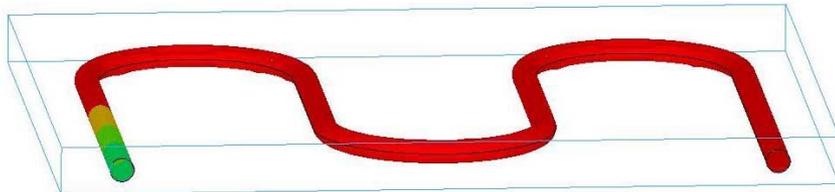
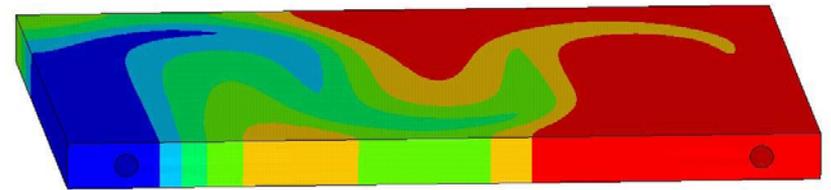
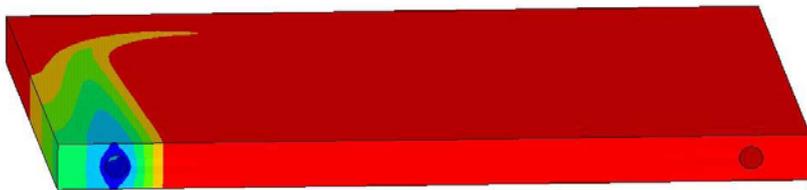
Radial 5  
Axial 20



Radial 16  
Axial 200

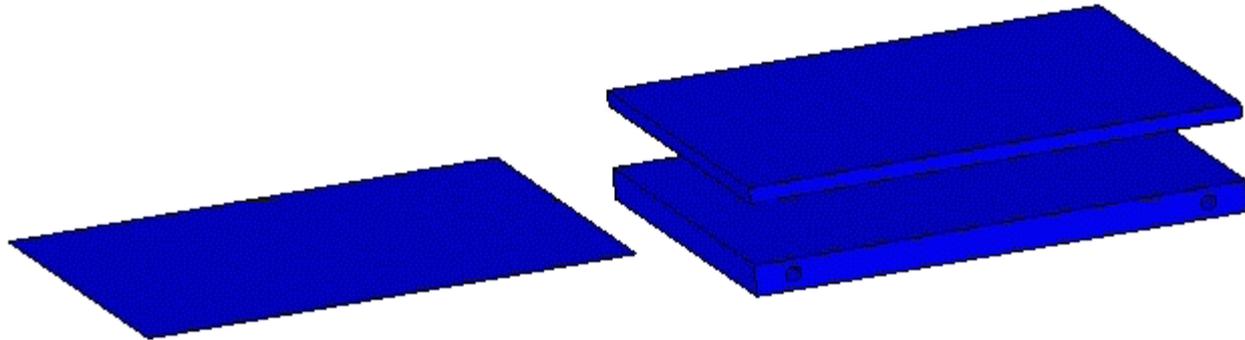
# Application – die cooling

A Bulk Fluid Flow algorithm is used to model the energy exchange between the cold fluid flowing through the die cooling channels.



# Application – die cooling

LS-DYNA KEYWORD DECK BY LS-PRE  
Time = 0



# Water properties

LSTC

T [C]	$\rho$ [kg/m <sup>3</sup> ]	$C_p$ [J/kg C]	$\mu$ [kg/m s]	k [W/m C]
20	998.	4182.	1.002e-03	0.603
40	992.	4179.	0.651e-03	0.632
60	983.	4185.	0.462e-03	0.653
80	972.	4197.	0.350e-03	0.670
100	958.	4216.	0.278e-03	0.681

# How do you determine a pipe flow convection coefficient

## Problem definition

LSTC

Pipe diameter =  $D = 15\text{mm} = 0.015\text{ m}$

Pipe cross section area =  $A = \pi D^2/4 = \pi(0.015)^2/4 = 1.77\text{e-}04\text{ m}^2$

Volumetric flow rate =  $G = 20\text{ l/min} = 0.02\text{ m}^3/\text{min} = 3.33\text{e-}04\text{ m}^3/\text{sec}$

Flow velocity =  $G/A = 1.89\text{ m/sec}$

Pipe wall temperature =  $T_{\text{wall}} = 100\text{C}$

Water temperature =  $T_{\text{fluid}} = 20\text{C}$

# How do you determine a pipe flow convection coefficient

## Some preliminaries

LSTC

Fully developed – the effect of entrance conditions (e.g., pipe from a header) on  $h$  are negligible.

$$\frac{L}{D} > 40$$

Fluid properties are evaluated at the film temperature,  $T_{film}$

$$T_{film} = \frac{T_{wall} + T_{fluid}}{2} = \frac{100 + 20}{2} = 60$$

Reynolds number

$$Re = \frac{V\rho D}{\mu} = \frac{(1.89)(983)(0.015)}{0.462 * 10^{-3}} = 6.03 * 10^4$$

Prandtl number

$$Pr = \frac{c_p \mu}{k} = \frac{(4185.)(0.462 * 10^{-3})}{0.653} = 2.96$$

# How do you determine a pipe flow convection coefficient

## Classical empirical correlations

LSTC

### Dittus-Boelter equation

$$h = 0.023 \frac{k}{D} \text{Re}^{0.8} \text{Pr}^n$$

$n=0.3$  for cooling of the fluid

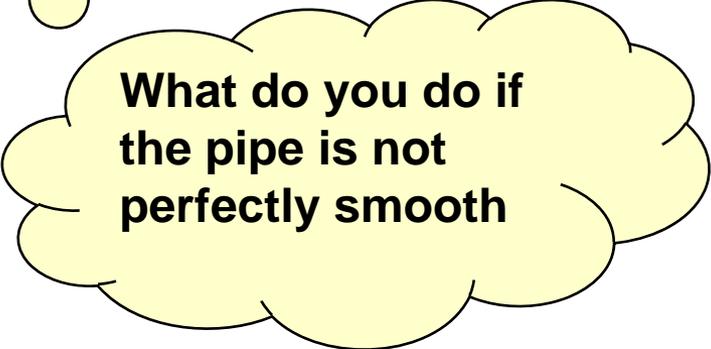
$n=0.4$  for heating of the fluid

$$= 0.023 \frac{0.653}{0.015} (6.03 * 10^4)^{0.8} (2.96)^{0.4} = 10,300 \frac{W}{m^2 C}$$

### Sieder-Tate equation

$$h = 0.023 \frac{k}{D} \text{Re}^{0.8} \text{Pr}^n \left( \frac{\mu_{bulk}}{\mu_{wall}} \right)^{0.14}$$

←  $\mu(T)$  correction factor



What do you do if the pipe is not perfectly smooth

How do you determine a pipe flow convection coefficient

## Gnielinski correlation

LSTC

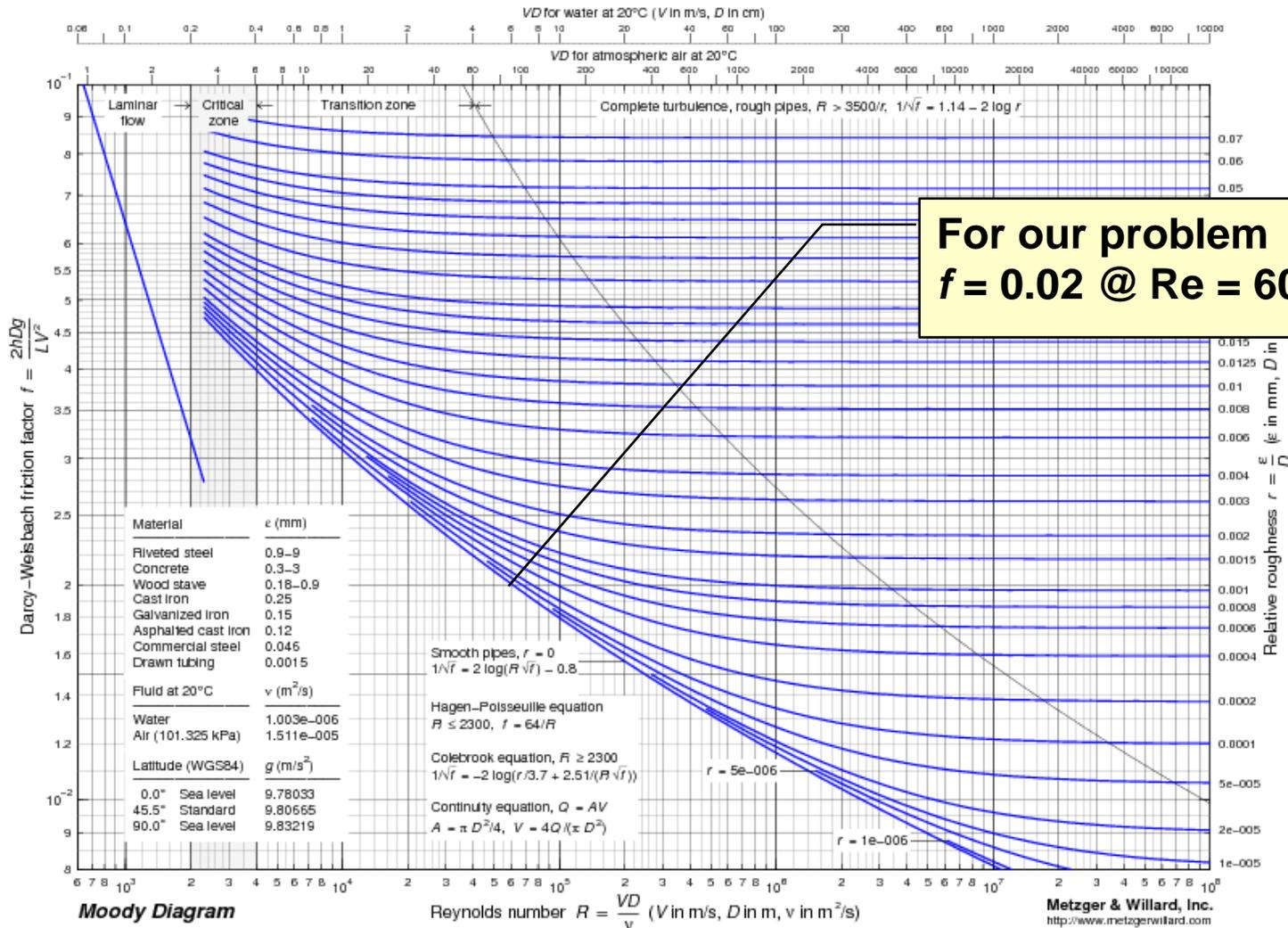
$$h = \left( \frac{k}{D} \right) \left[ \frac{(f/8)(\text{Re} - 1000)\text{Pr}}{1 + 12.7(f/8)^{0.5}(\text{Pr}^{2/3} - 1)} \right] = 11,400 \text{ W} / \text{m}^2 \text{C}$$

$f$  = Darcy–Weisbach friction factor (see next vu-graph for value)

There are 2 definitions for  $f$ . The Darcy–Weisbach friction factor is 4 times larger than the Fanning friction factor, so attention must be paid to note which one of these is meant in any "friction factor" chart or equation being used. The Darcy–Weisbach factor is more commonly used by civil and mechanical engineers, and the Fanning factor by chemical engineers, but care should be taken to identify the correct factor regardless of the source of the chart or formula.

# How do you determine a pipe flow friction factor

[http://www.mathworks.com/matlabcentral/fx\\_files/7747/1/moody.png](http://www.mathworks.com/matlabcentral/fx_files/7747/1/moody.png)



# Workshop problem: Advection – Diffusion

pipe.k

LSTC

Consider steady state 1-dimensional bulk fluid flow through a pipe

Entry temperature  
 $T_2 = 2$

Pipe size  
dia=0.01, length=1.

Exit temperature  
 $T_1 = 1$

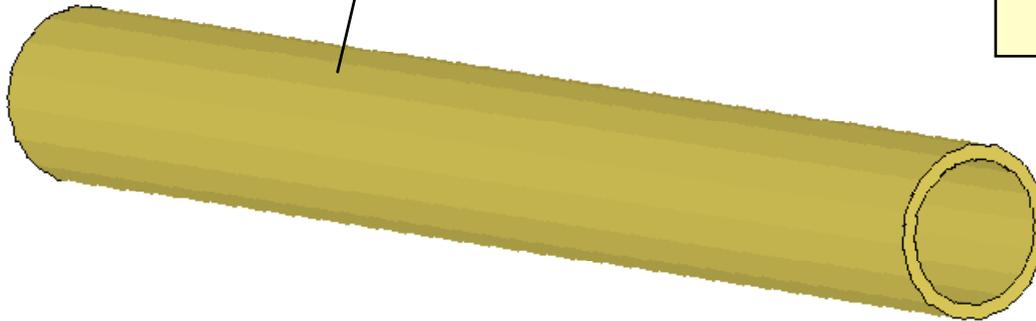
Fluid properties

$k = \rho = c = 1$

Fluid velocity

$v=1$

The inner pipe wall is fixed at  $T = 0$ . The flowing fluid loses heat by convection to the pipe with  $h = 0.005$



# Workshop problem: Advection – Diffusion

pipe.k

LSTC

## Pipe geometry

$x = \text{half length} = 0.5$

$d = \text{diameter} = 0.01$

$p = \text{perimeter} = pd = 0.0314$

$A = \text{cross sectional area} = pd^2 / 4 = 7.85 \cdot 10^{-5}$

## Fluid data

$r = \text{density} = 1.$

$k = \text{thermal conductivity} = 1.$

$c = \text{heat capacity} = 1.$

$a = \text{thermal diffusivity} = k/pc = 1.$

$V = \text{velocity} = 1.$

$m = \text{mass flow rate} = r \cdot A \cdot v = 7.85 \cdot 10^{-5}$

## Boundary conditions

$h = \text{convection coefficient} = 0.005$

$T_0 = \text{pipe wall temperature} = 0.$

$T_1 = \text{inlet (x=0.) temperature} = 2.$

$T_2 = \text{exit (x=2l) temperature} = 1.$

# Workshop problem: Advection – Diffusion

Carslaw & Jaeger, Conduction of Heat in Solids, 2<sup>nd</sup> ed., p148

LSTC

$$T = \frac{T_2 e^{-V(L-x)/2\alpha} \sinh \xi x + T_1 e^{Vx/2\alpha} \sinh \xi(L-x)}{\sinh \xi L}$$

$$\xi = \sqrt{\frac{V^2}{4\alpha^2} + \frac{hp}{Ak}}$$

$$\alpha = \frac{k}{\rho c}$$

Three analytical solutions to benchmark against: T at x = 0.5

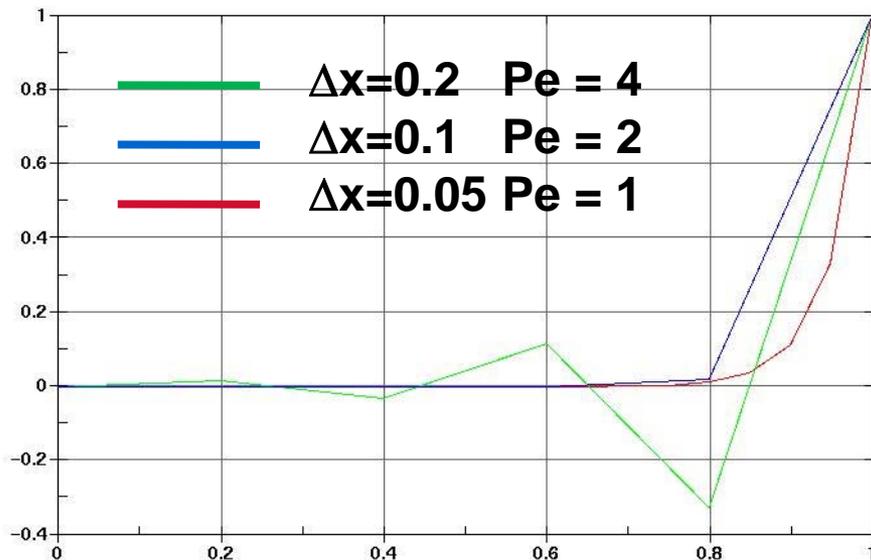
1) pure conduction	T = 1.500
2) conduction + advection (h=0)	T = 1.622
3) conduction + advection + convection	T = 1.293

# BOUNDARY\_THERMAL\_BULKFLOW\_UPWIND

## Advanced feature

LSTC

For many flow problems, dissipative mechanisms are only significant in a narrow layer typically adjacent to a boundary. Computational solutions obtained with grids appropriate to the main flow region are often oscillatory when the true solution changes rapidly across the boundary layer.



1D steady advection diffusion problem

$$V \frac{dT}{dx} - \alpha \frac{d^2T}{dx^2} = 0$$

with  $T(0)=0$ . and  $T(1)=1$ .

‘Wiggles’ occur at cell Peclet numbers greater than 1.

$$Pe = Re Pr = \left( \frac{\rho V \Delta x}{\mu} \right) \left( \frac{\mu c}{k} \right) = \frac{V \Delta x}{\alpha}$$

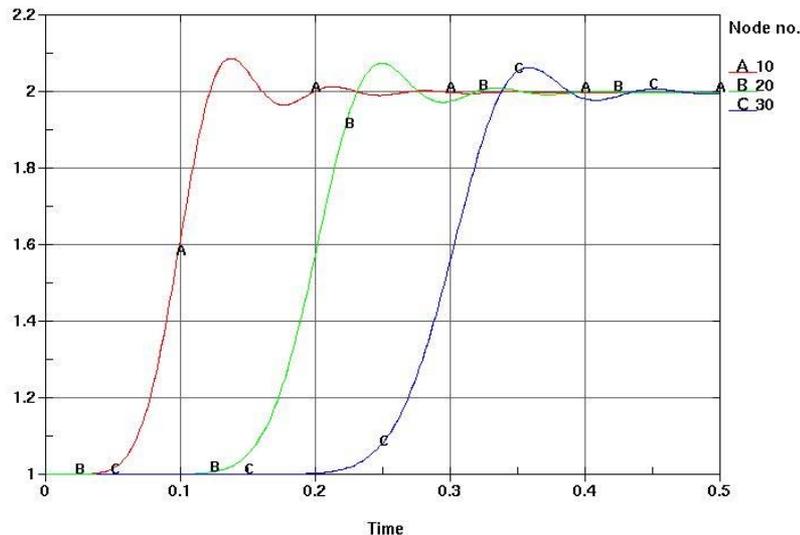
# BOUNDARY\_THERMAL\_BULKFLOW\_UPWIND

## Advanced feature, upwind\_transient.k

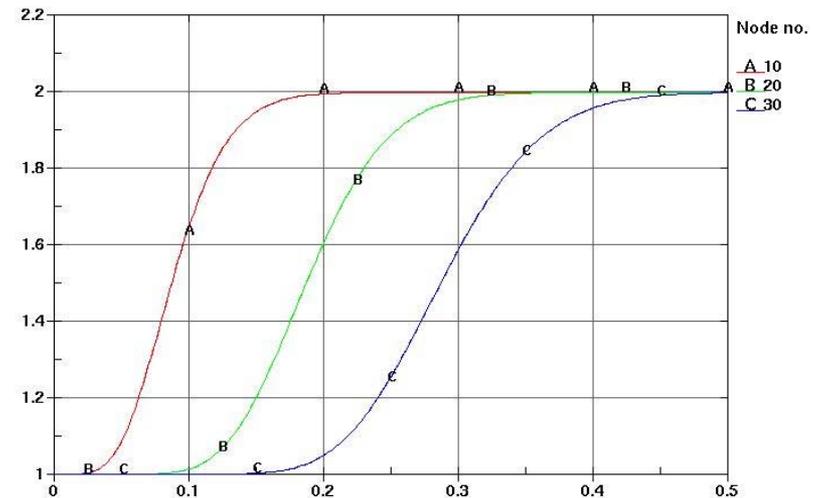
LSTC

**UPWIND** adds a term (sometimes called **artificial viscosity**) to the element stiffness matrix. This eliminates the 'wiggles' but also makes the solution more diffusive. Note that the curves are now not as steep and their shape is more spread out over time. Wiggles are gone but the solution is less accurate.

**UPWIND off**



**UPWIND on**



Transient 1D flow with a step change in entering fluid temperature. Shown is the temperature history at 3 locations down the pipe. Initial and boundary conditions:  $T(x,0)=1$ ,  $T(0,t)=2$ .

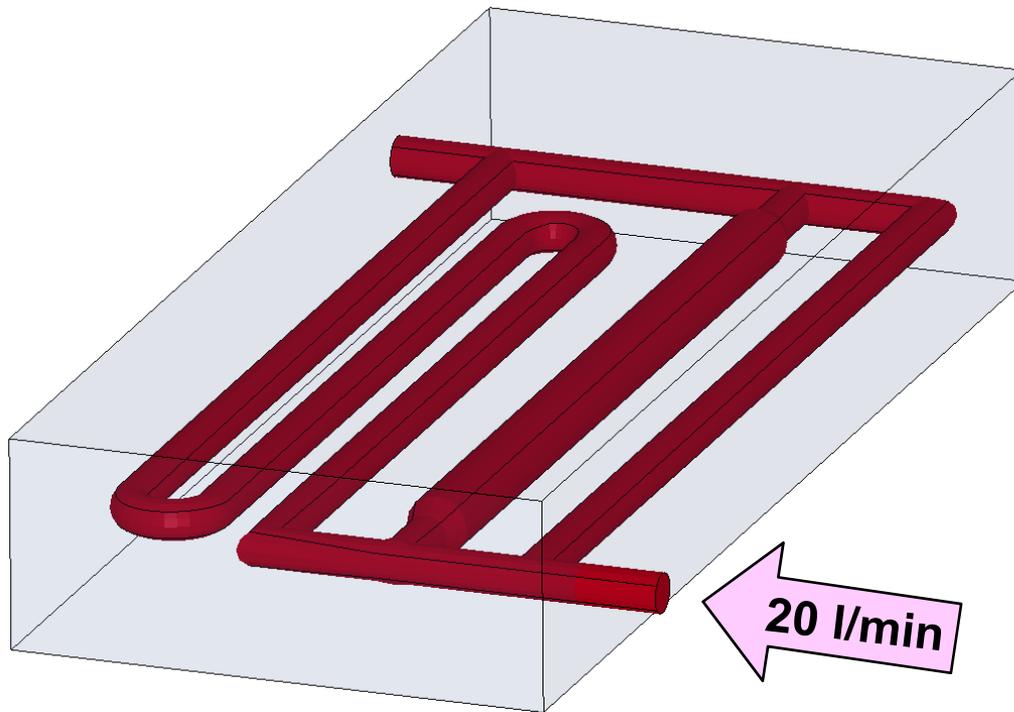
# Pipe Network

Think about pipes in your house. The starting point is the valve on the pipe entering your house. We will call this **NODE 1**. Node 1 is special and has a boundary condition specified. The BC is the pressure you would read on a pressure gauge at this location. The water enters your house and passes through several pipe junctions before it exits through your garden hose. Every junction is represented by a **NODE**. The last node also needs a BC specified. This BC is the mass flow rate. The pipe flow code will calculate the pressure at the intermediate junction nodes and the flow rate through the pipes.



# Pipe Network

LSTC

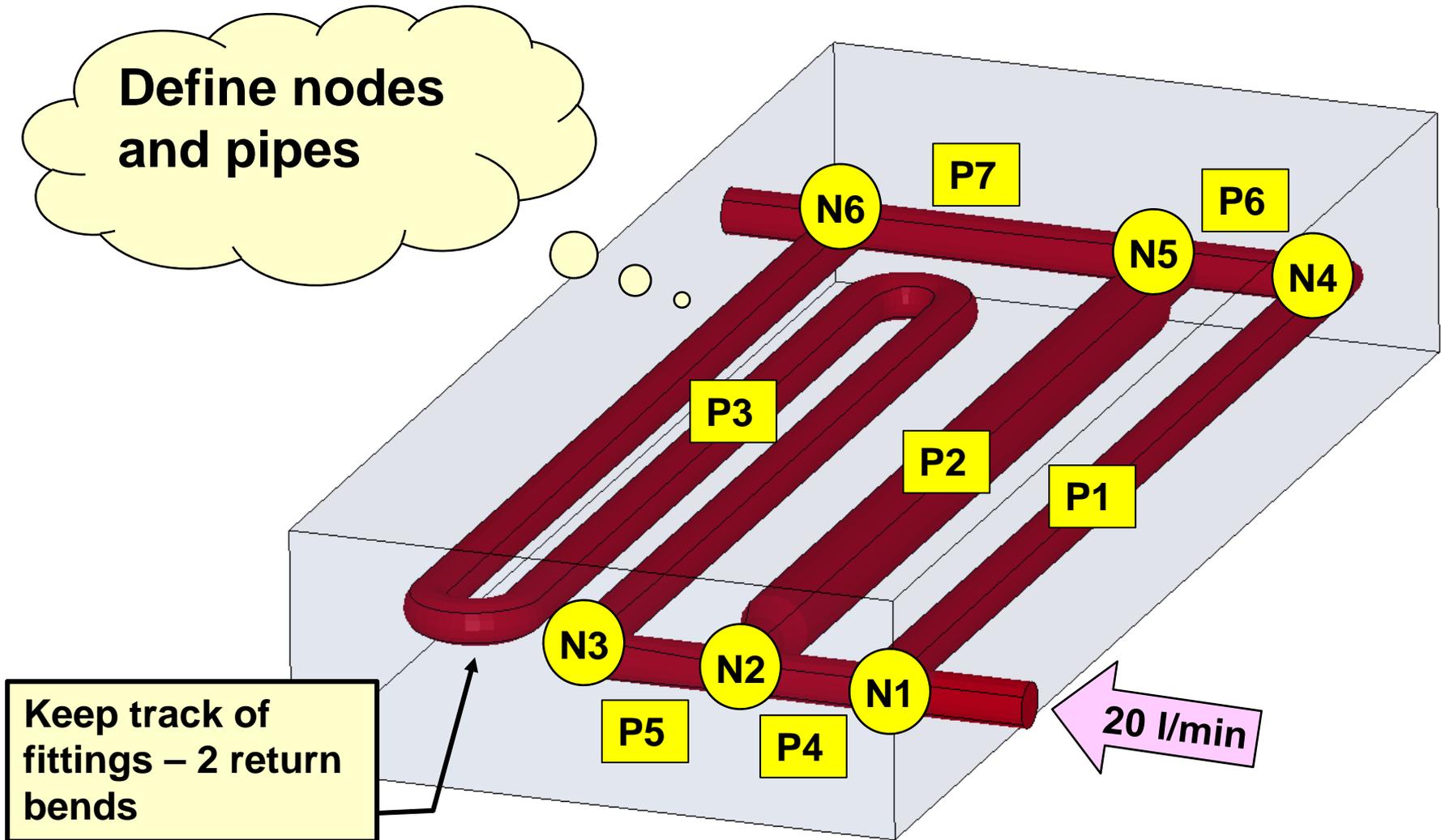


**Given an entering flow rate, calculate the flow in each pipe and the convection heat transfer coefficient**

# Pipe Network

## Define nodes and pipes

LSTC



# Pipe Network

**input**

**output**

Pipe	N1	N2	Length [m]	Dia. [mm]	Rough [mm]	Ftg. [ $L_e/D$ ]	Q [l/min]	h [W/m <sup>2</sup> C]
1	1	4	1	10	0.05		5.7	5600
2	2	5	1	20	0.05		9.7	2400
3	3	6	3	10	0.05	100	4.5	4600
4	1	2	0.2	10	0.05		14.2	11000
5	2	3	0.2	10	0.05		4.5	4600
6	4	5	0.2	10	0.05		5.7	5600
7	5	6	0.4	10	0.05		15.5	12000

# Pipe Network

Pipe type	Roughness, $e$ [mm]
Cast iron	0.25
Galvanized iron	0.15
Steel or wrought iron	0.046
Drawn tubing	0.0015

Fitting type	Equivalent length $L_e/D$
Globe valve	350
Gate valve	13
Check valve	30
90° std. elbow	30
90° long radius	20
90° street elbow	50
45° elbow	16
Tee flow through run	20
Tee flow through branch	60
Return bend	50

# Pipe Network

## Solution algorithm

LSTC

### Solve:

Bernoulli equation

$$\left( \frac{V_1^2 - V_2^2}{2g} \right) + \left( \frac{P_1 - P_2}{\rho g} \right) + (z_1 - z_2) = H_f$$

Friction equation

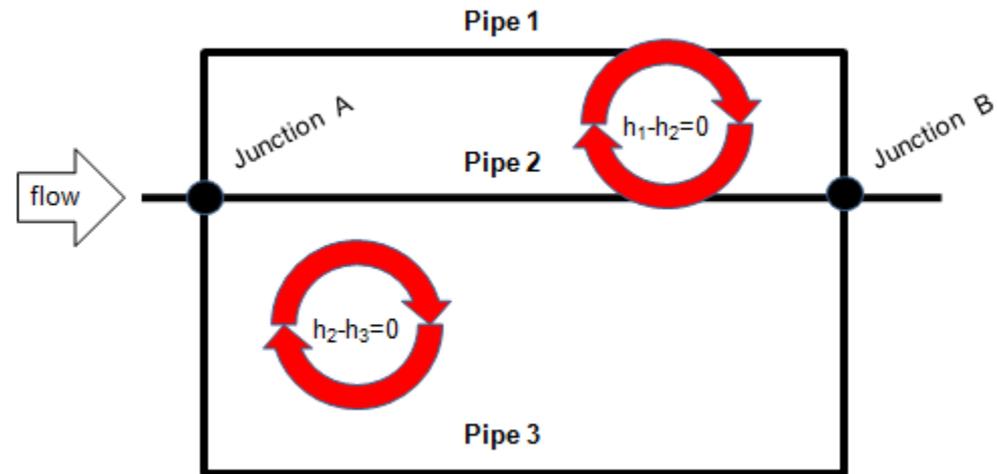
$$H_f = f \frac{L}{D} \frac{V^2}{2g} + H_{fitting}$$

Gnielinski equation

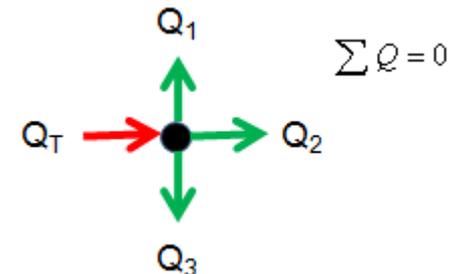
$$h = \left( \frac{k}{D} \right) \left[ \frac{(f/8)(\text{Re} - 1000)\text{Pr}}{1 + 12.7(f/8)^{0.5}(\text{Pr}^{2/3} - 1)} \right]$$

### Subject to:

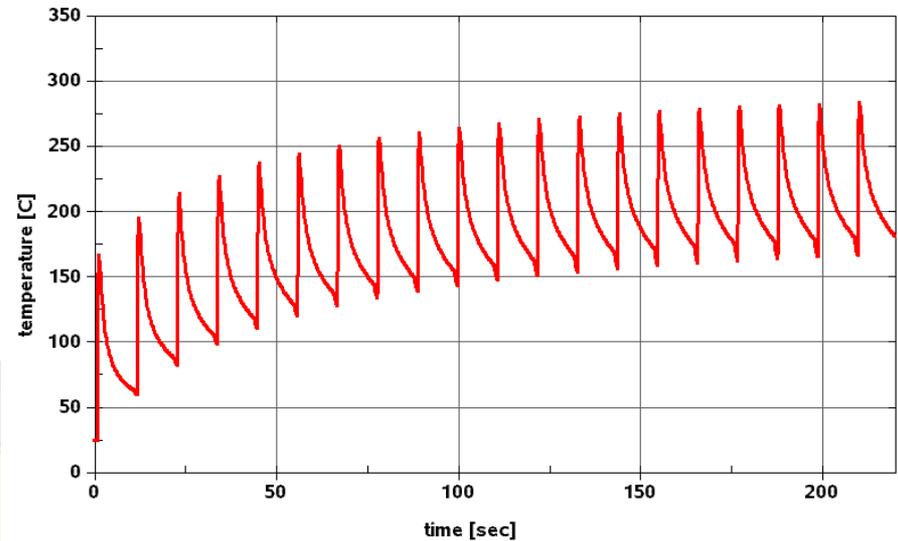
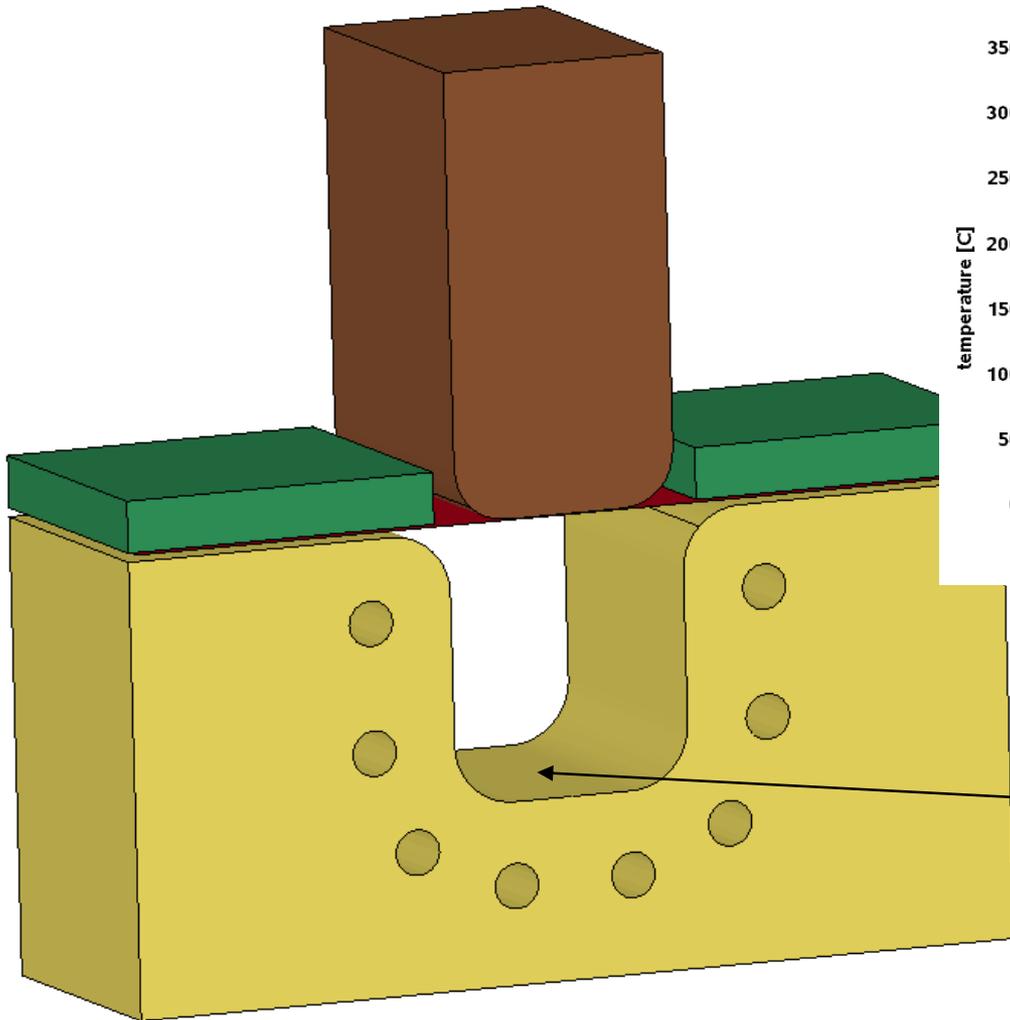
Pressure drop around each circuit = 0.



Flow into each junction = 0.

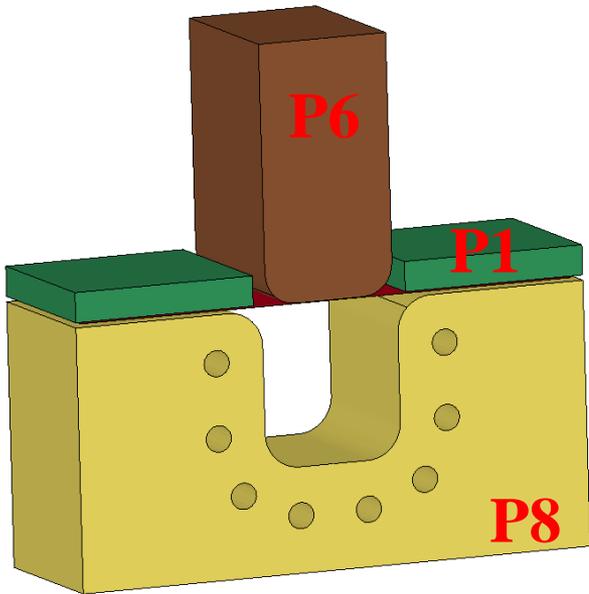


# Process start-up time



**Shown is the teperature history for this location during 20 stamping cycles.**

# Process start-up time



```
#!/bin/csh -f
set i=1
while ( $i <= 20 )
./ls971 i=stamping.k g=d3plot$i"_"
@ i = $i + 1
end
```

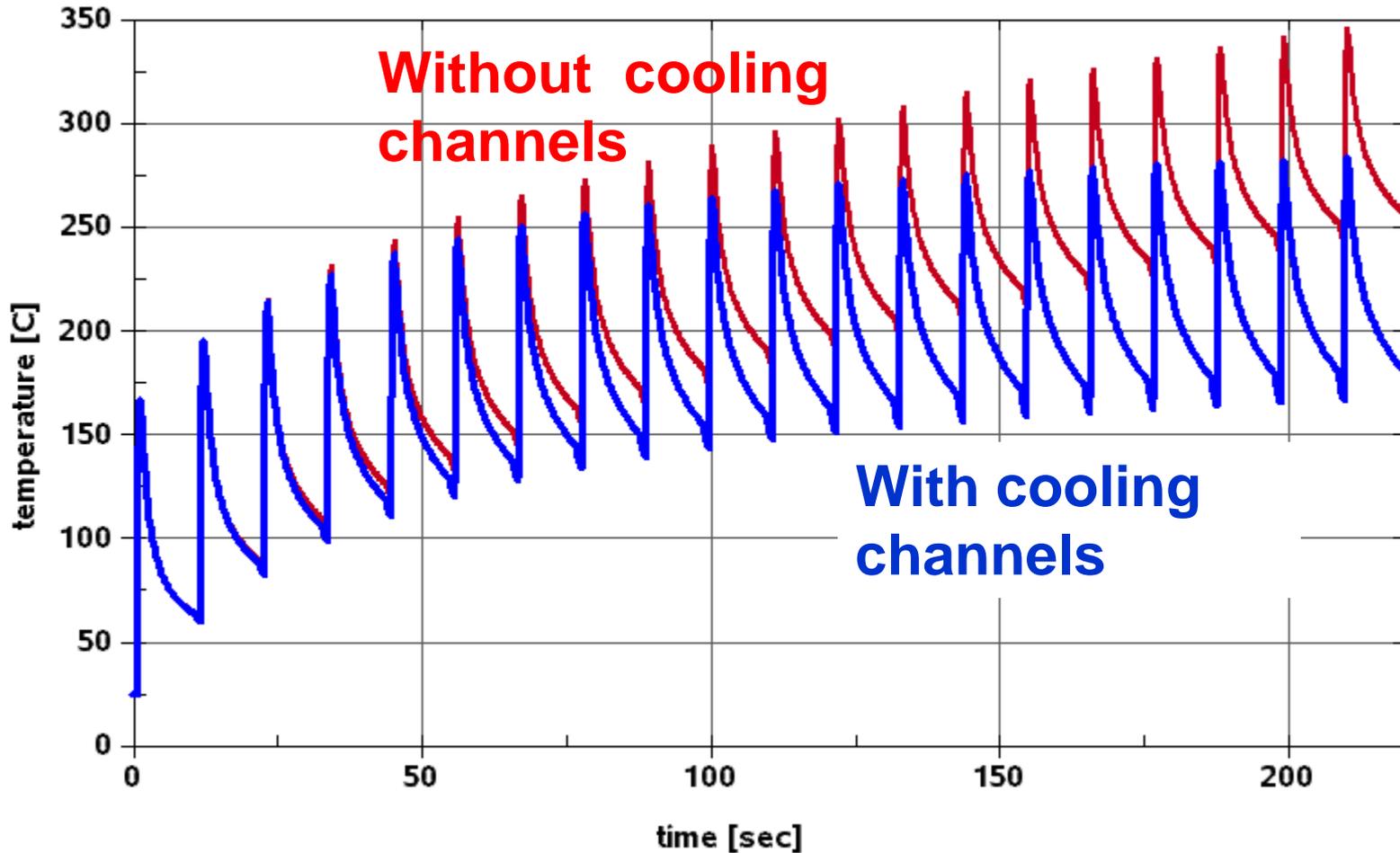
```
*KEYWORD
*INITIAL_TEMPERATURE_SET
$  nsid  temp
    1    25.
    6    25.
    8    25.
*END
```

```
*INCLUDE
new_temp_ic.inc

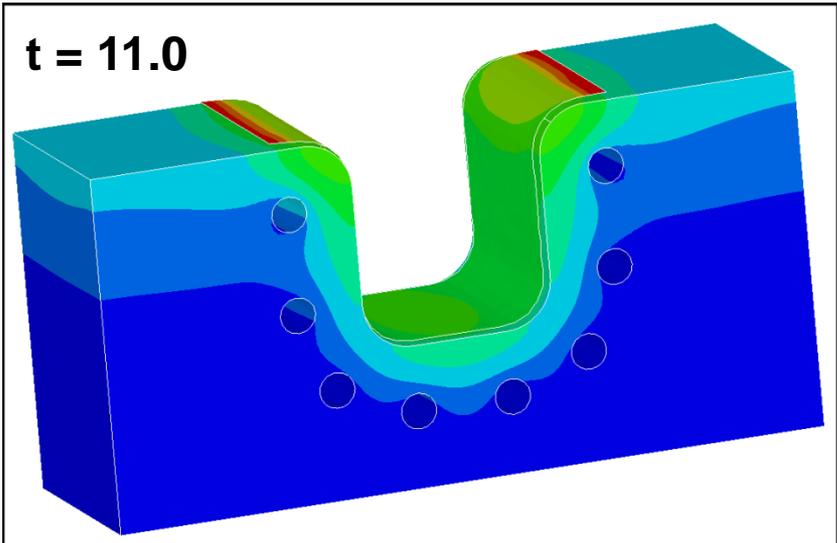
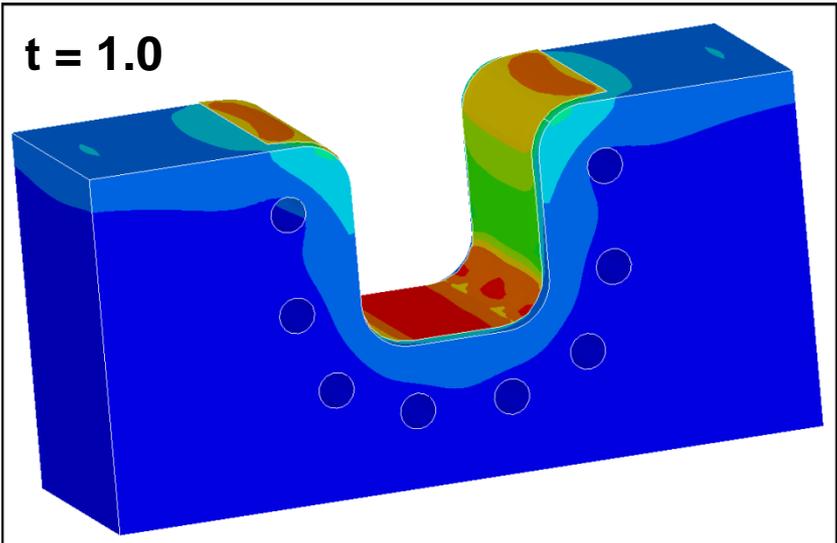
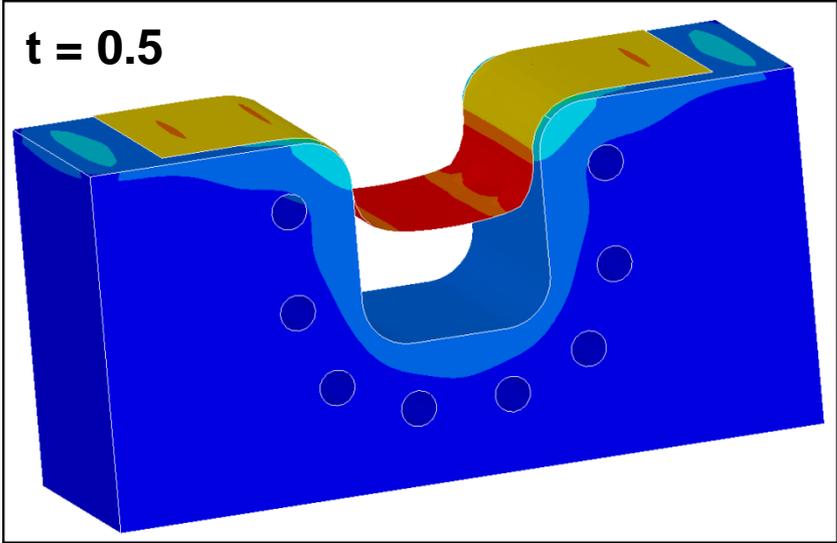
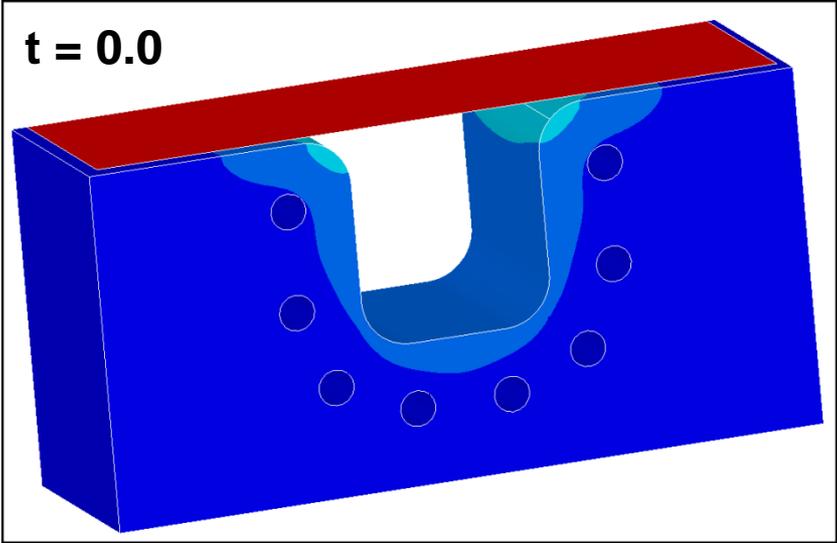
*INTERFACE_SPRINGBACK_LSDYNA
$  psid
    1
*SET_PART_LIST
$  psid
    1
$  pid1  pid2  pid3
    1    6    8
```

# Process start-up time

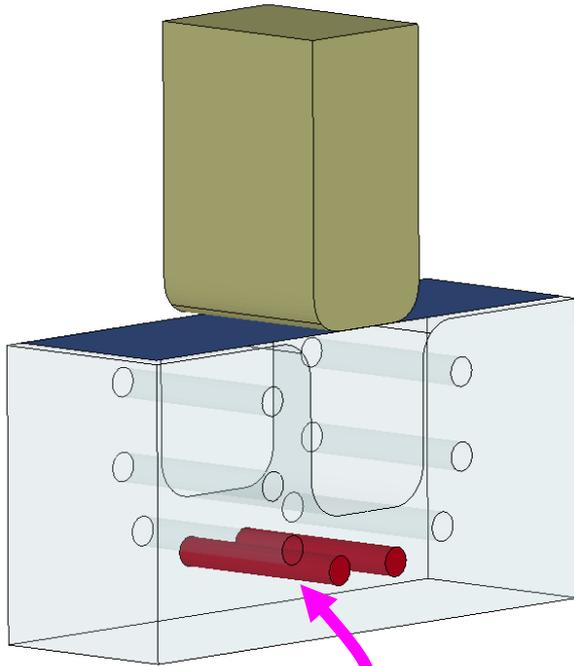
## Tool temperature after 20 stampings



# Process start-up time



# Thermostat feature adjusts the heating rate to keep the sensor temperature at the set point.



## \*LOAD\_HEAT\_CONTROLLER

$Q_{cont}$	volumetric heating rate
$Q_0$	constant volumetric heating rate
$G_p$	proportional gain
$G_i$	integral gain
$T_{set}$	set point temperature
$T$	sensor temperature (at a node)

$$Q_{cont} = Q_0 + \underbrace{G_p (T_{set} - T)}_{\text{proportional}} + \underbrace{G_i \int_{t=0}^t (T_{set} - T) dt}_{\text{integral}}$$

proportional

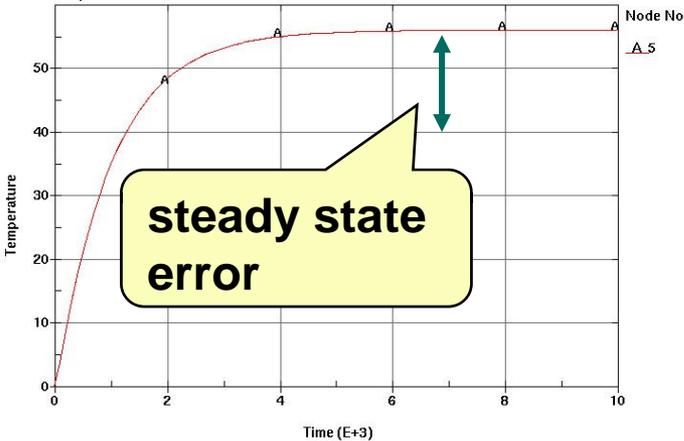
integral

# Thermostat controller

## set point $T_{\text{set}}=40$

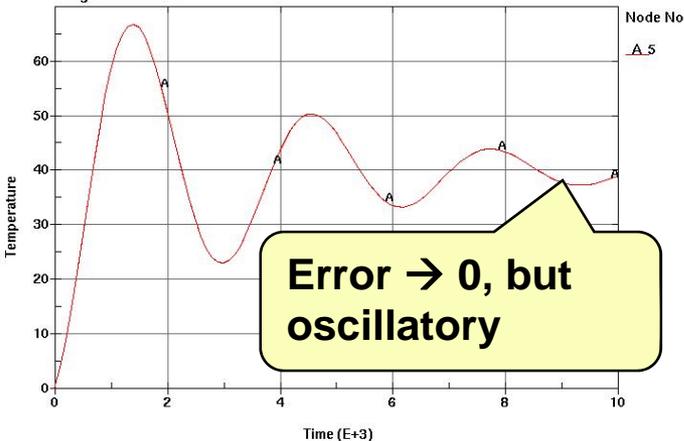
LSTC

Proportional Controller



**Proportional Control** – corrective action is taken which is proportional to the error. Should a sustained correction (brought about by a sustained disturbance) be required, an accompanying steady state error will exist.

Integral Controller

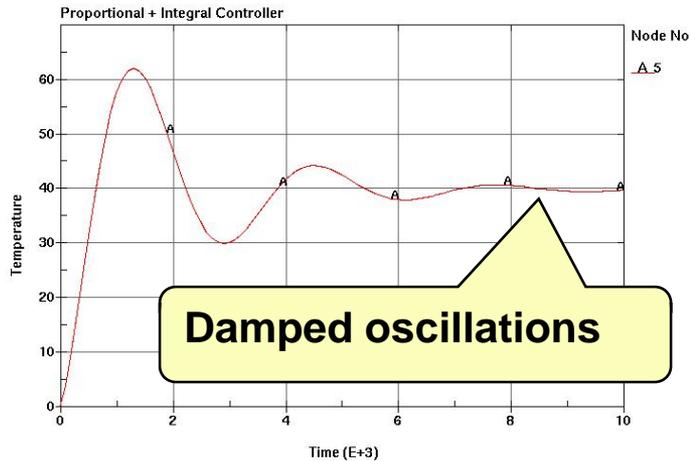


**Integral Control** – corrective action is made which is proportional to the time integral of the error. An integral controller will continue to correct until the error is zero (eliminating any steady state system error). But, there is also a weakness. Integral control tends to overshoot, thereby producing an oscillatory response and, in some cases, instability.

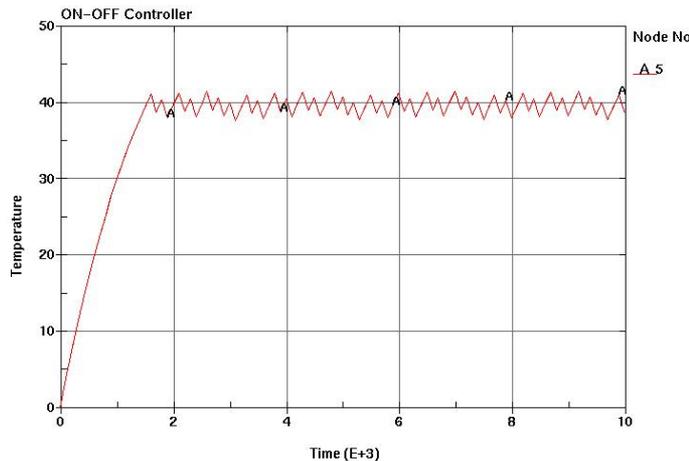
# Thermostat controller

## Set point $T_{set}=40$

LSTC



**Proportional + Integral Control – the oscillations will be damped and the set point error  $\rightarrow 0$ .**



**On – Off Control can also be activated.**

# Thermostat controller

## \*LOAD\_HEAT\_CONTROLLER keyword

LSTC

NODE	PID	LOAD	TSET	TYPE	GP	GI
------	-----	------	------	------	----	----

**NODE** sensor is located at this node

**PID** heater (or cooler) part id being controlled

**LOAD** heater output  $Q_0$  [W/m<sup>3</sup>]

**TSET** set point temperature @ **NODE**

**TYPE** 1 = on off  
2 = proportional + integral

**GP** proportional gain

**GI** integral gain