

Mode Tracking In the Presence of Shape & Mesh Changes Using LS-OPT

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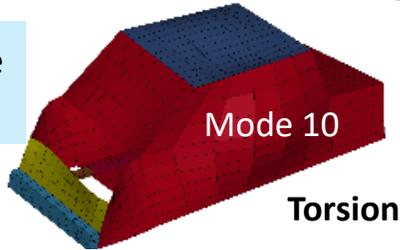
Outline

- **Importance of Mode Tracking**
- **Mode Tracking Criterion – Modal Assurance Criterion (MAC)**
- **Challenges due to Shape Changes and Remeshing**
- **Interpolated Modal Assurance Criterion (IMAC)**
 - **Point Set Registration (Coherent Point Drift)**
 - **Interpolation of Modal Eigenvector Components**
- **Examples**

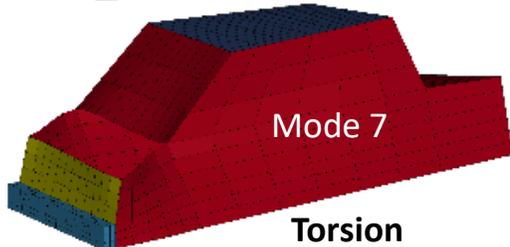
LS-OPT: Mode Tracking in the Presence of Shape and Meshing Changes

- Mode tracking is needed if a particular shape is of interest during design

Reference Mode
10



New Design
(changed thickness)



- No way to know beforehand that the new design will have mode 7 as torsional mode instead of 10.

- Modal Assurance Criterion (MAC)** used to identify similar modes in LS-OPT

- Based on vector operations over eigenvector corresponding to the baseline mode of interest and each eigenvector of the new design
- New design eigenvector with highest MAC is identified as being most similar to reference mode shape

Reference mode

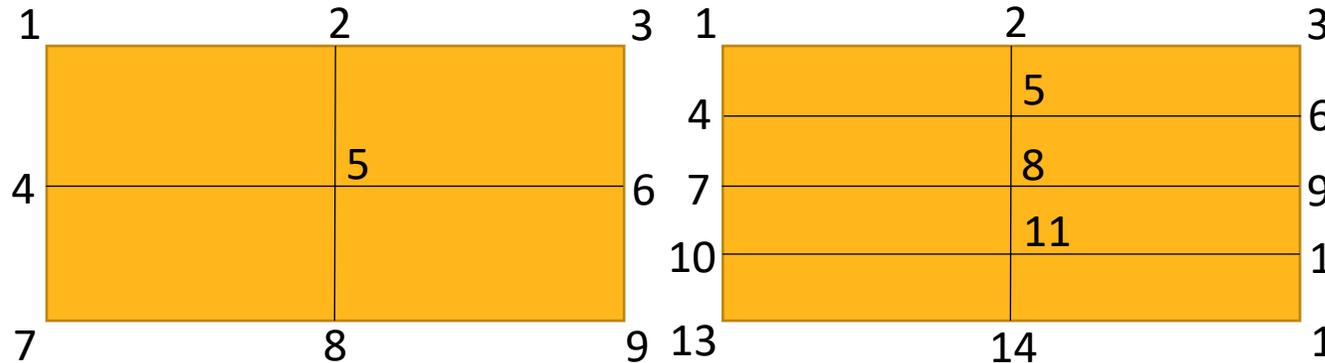
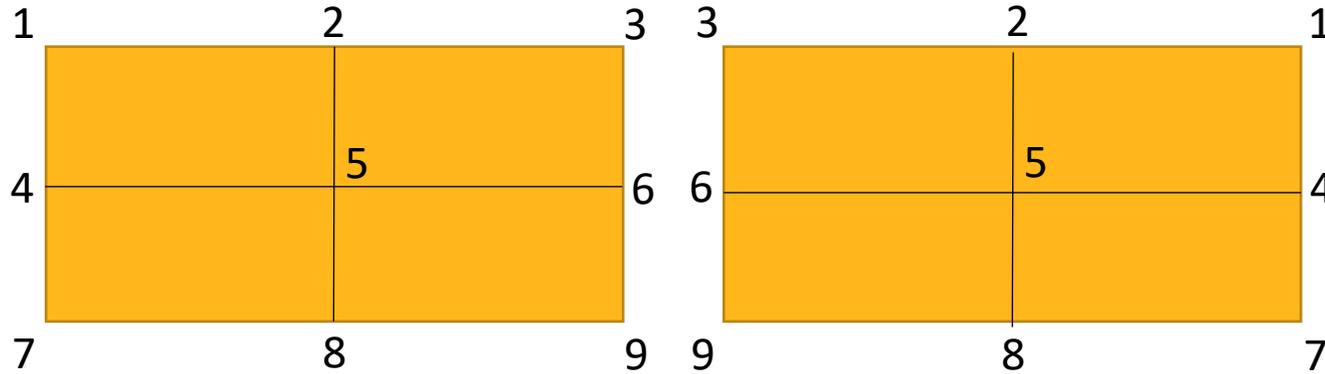
Compared mode

$$\max_j \frac{\{\varphi_0\}^H \{\varphi_j\} \{\varphi_j\}^H \{\varphi_0\}}{\{\varphi_0\}^H \{\varphi_0\} \{\varphi_j\}^H \{\varphi_j\}} = \max_j MAC_j$$

Eigenvectors φ_0 and φ_j must have same length and node order

Current Mode Tracking using Modal Assurance Criterion (MAC) in LS-OPT **requires identical mesh** for eigenvector comparison.

Incompatible Vectors for MAC Calculation Due to Re-meshing



Reference mode

Compared mode

$$\max_j \frac{\{\varphi_0\}^H \{\varphi_j\} \{\varphi_j\}^H \{\varphi_0\}}{\{\varphi_0\}^H \{\varphi_0\} \{\varphi_j\}^H \{\varphi_j\}} = \max_j MAC_j$$

$$\varphi_0 = \{v_{01}, v_{02}, v_{03}, v_{04}, v_{05}, v_{06}, v_{07}, v_{08}, v_{09}\}^T$$

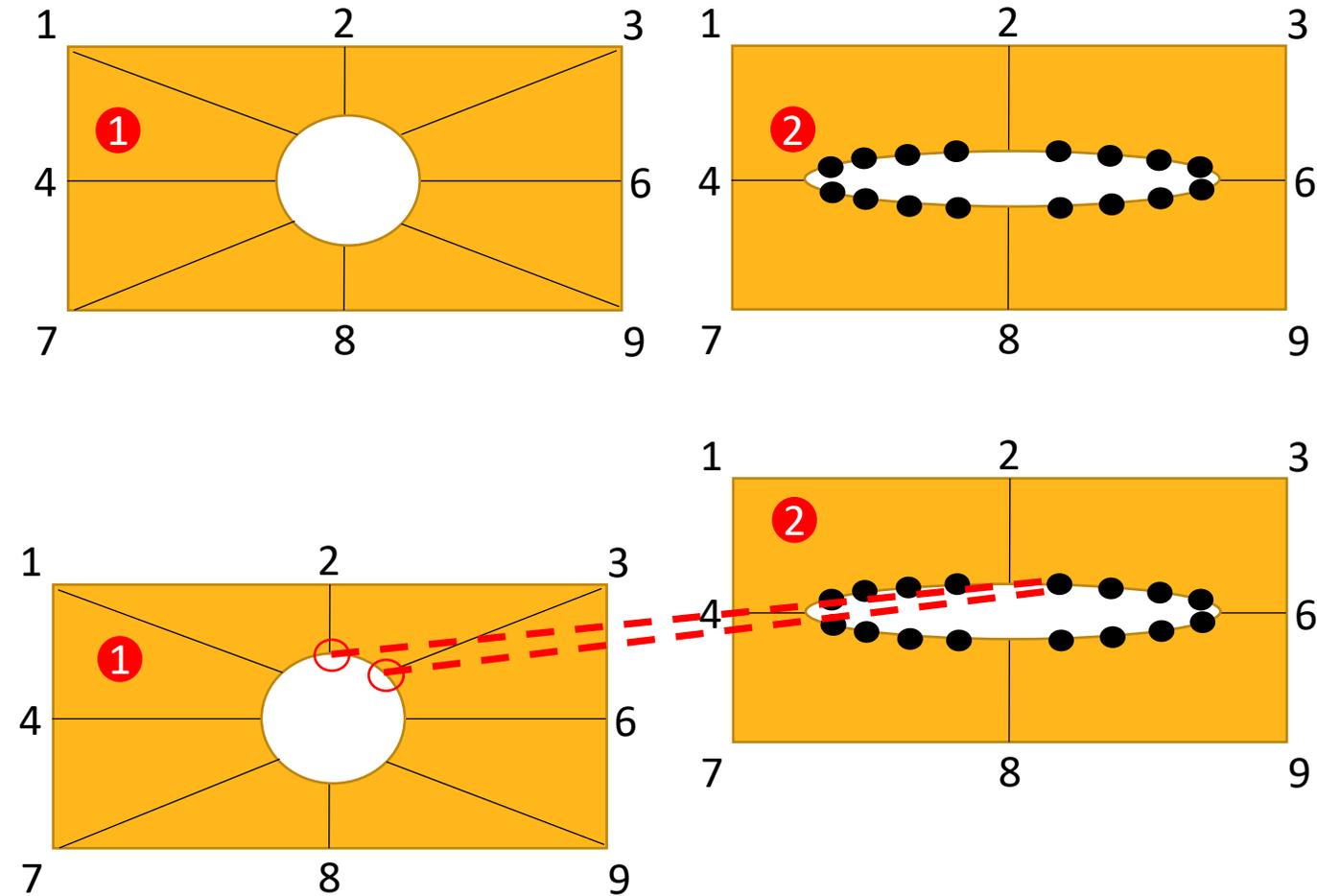
$$\varphi_j = \{v_{j3}, v_{j2}, v_{j1}, v_{j6}, v_{j5}, v_{j4}, v_{j9}, v_{j8}, v_{j7}\}^T$$

$$\varphi_0 = \{v_{01}, v_{02}, v_{03}, v_{04}, v_{05}, v_{06}, v_{07}, v_{08}, v_{09}\}^T$$

$$\varphi_j = \{v_{j1}, v_{j2}, v_{j3}, v_{j4}, v_{j5}, v_{j6}, v_{j7}, v_{j8}, v_{j9}, v_{j10}, v_{j11}, v_{j12}, v_{j13}, v_{j14}, v_{j15}\}^T$$

- Intuitive Interpolation (e.g. using shape functions) or node deletion
- Avoidable Re-meshing

Re-meshing & Eigenvector Incompatibility Due to Shape Change



- Re-meshing can be avoided even for shape changes, but unavoidable at times
- Non-intuitive mapping
- Non-intuitive interpolation weights

- Point Set Registration (PSR) algorithm used for mapping nodes
 - Non-rigid Coherent Point Drift (CPD) method

Non-Rigid Coherent Point Drift

- Alignment of two point sets as a probability density estimation problem
- Gaussian mixture model (GMM) centroids (1st point set $\mathbf{Y}_{M \times D}$) fit to the data (2nd point set $\mathbf{X}_{N \times D}$) by maximizing the likelihood

$$p(\mathbf{x}) = \sum_{m=1}^M P(m)p(\mathbf{x}|m)$$

$$p(\mathbf{x}|m) = \frac{1}{(2\pi\sigma^2)^{D/2}} \exp\left(-\frac{\|\mathbf{x}-\mathbf{y}_m\|^2}{2\sigma^2}\right)$$

- GMM centroids forced to move coherently as a group to preserve the topological structure of the point sets

- Coherence constraint imposed by regularizing the displacement field

$$\mathcal{T}(\mathbf{Y}, v) = \mathbf{Y} + v(\mathbf{Y})$$

- Regularized negative log likelihood

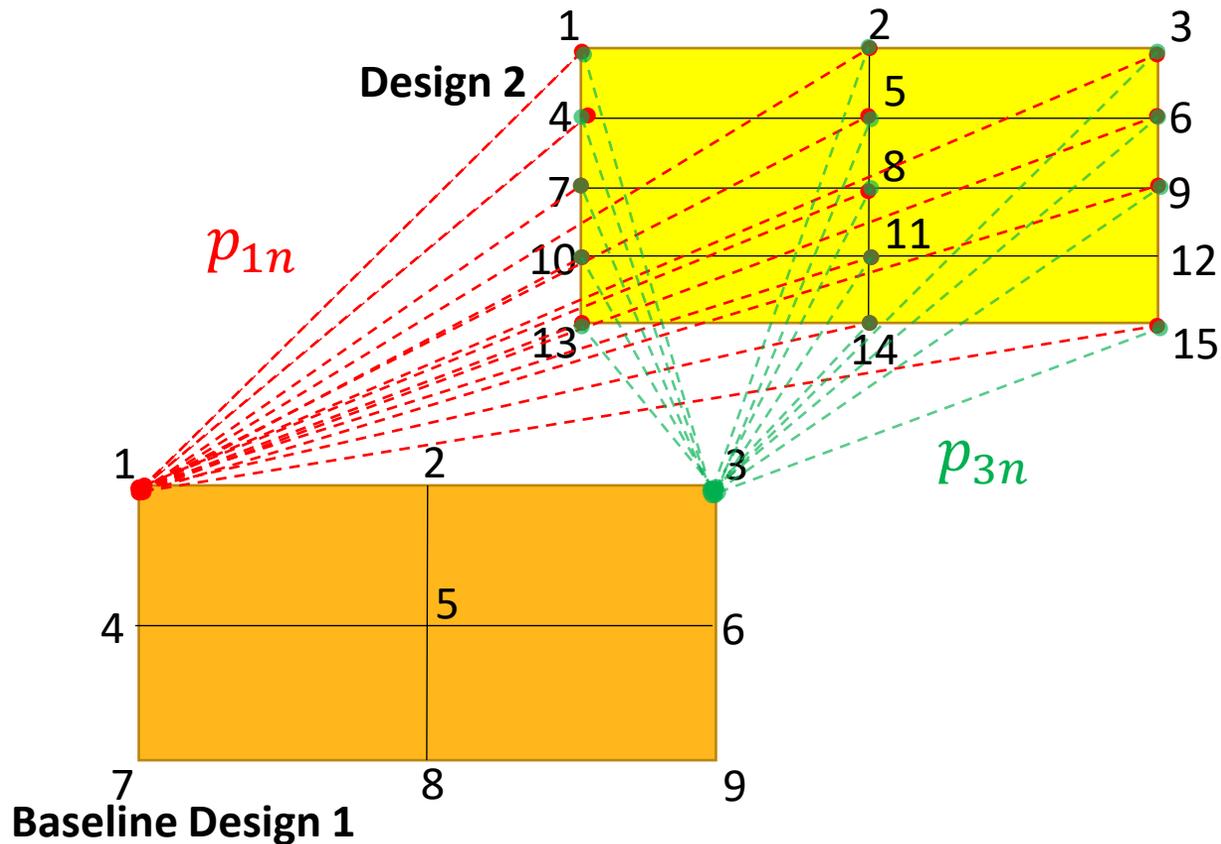
$$f(v, \sigma^2) = E(v, \sigma^2) + \frac{\lambda}{2}\phi(v)$$

$$E(v, \sigma^2) = -\sum_{n=1}^N \log \sum_{m=1}^M P(m)P(\mathbf{x}_n|m)$$

- v and σ^2 solved iteratively using Expectation Minimization (EM).
- *Pairwise probability of association between nodes of the two sets*

Interpolated Modal Assurance Criterion (IMAC) for Mode Tracking

- Pairwise probability of association between nodes of the two sets



- Interpolated j^{th} eigenvector

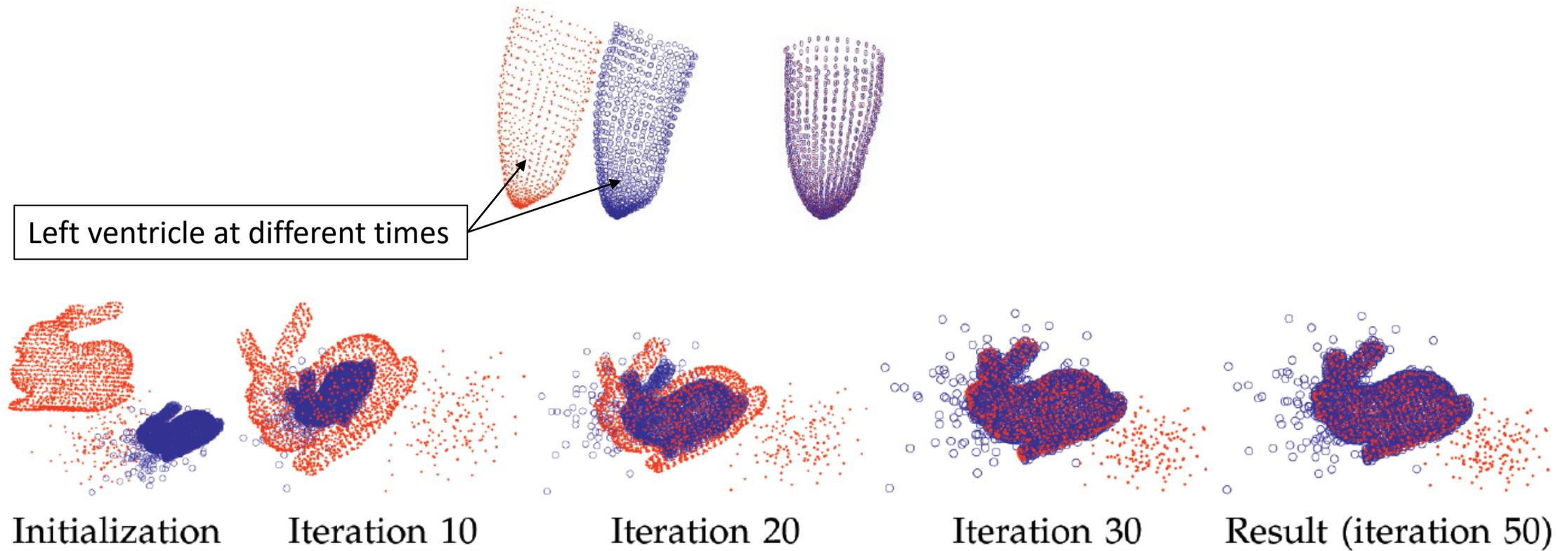
$$\hat{\varphi}_{jm} = \frac{1}{\sum_{n=1}^N p_{mn}} \sum_{n=1}^N p_{mn} \varphi_{jn} \quad (m \in [1,9])$$

$$\varphi_0: 9 \times 1 \quad \varphi_j: 15 \times 1 \quad \hat{\varphi}_j: 9 \times 1$$

- Interpolated MAC measure for design 2 (φ_0 and $\hat{\varphi}_j$ length = m)

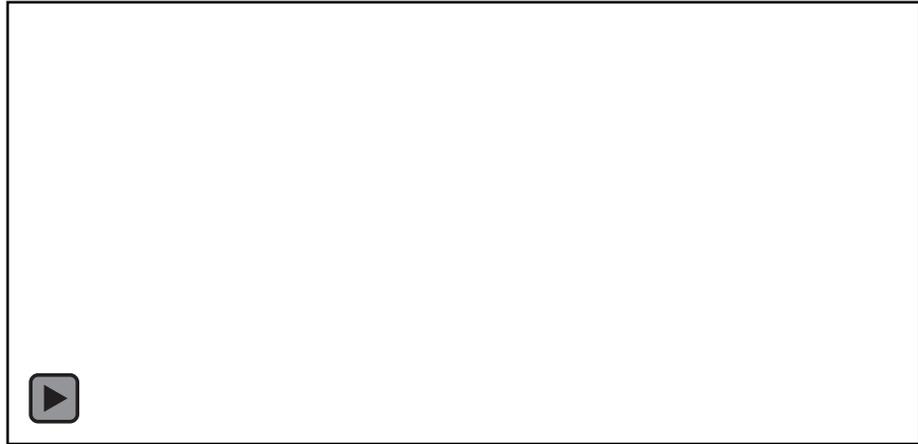
$$IMAC_j = \frac{\varphi_0^H \hat{\varphi}_j \hat{\varphi}_j^H \varphi_0}{\varphi_0^H \varphi_0 \hat{\varphi}_j^H \hat{\varphi}_j}$$

Examples of CPD PSR

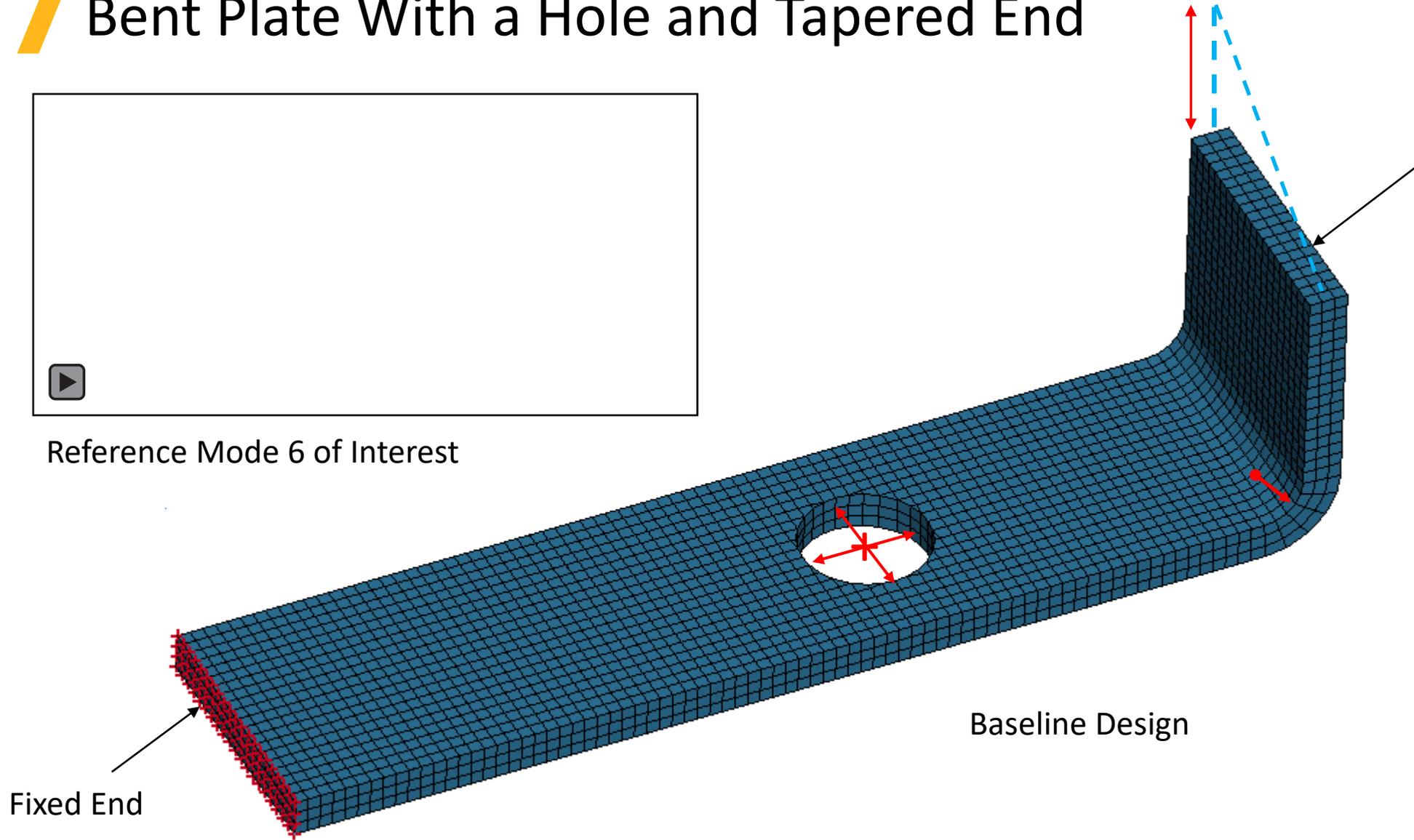


Myronenko A, Song X. Point set registration: Coherent point drift. IEEE transactions on pattern analysis and machine intelligence. 2010 Mar 18;32(12):2262-75.

Bent Plate With a Hole and Tapered End



Reference Mode 6 of Interest



Tapered End

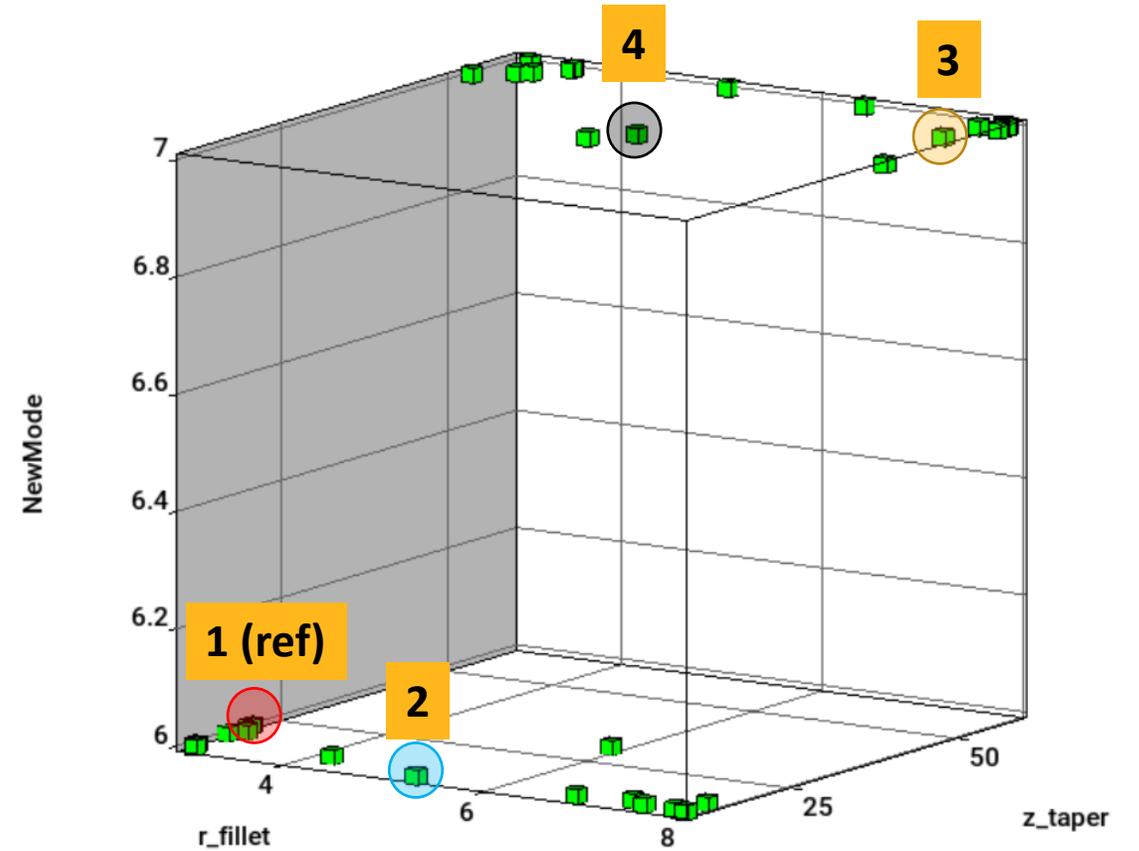
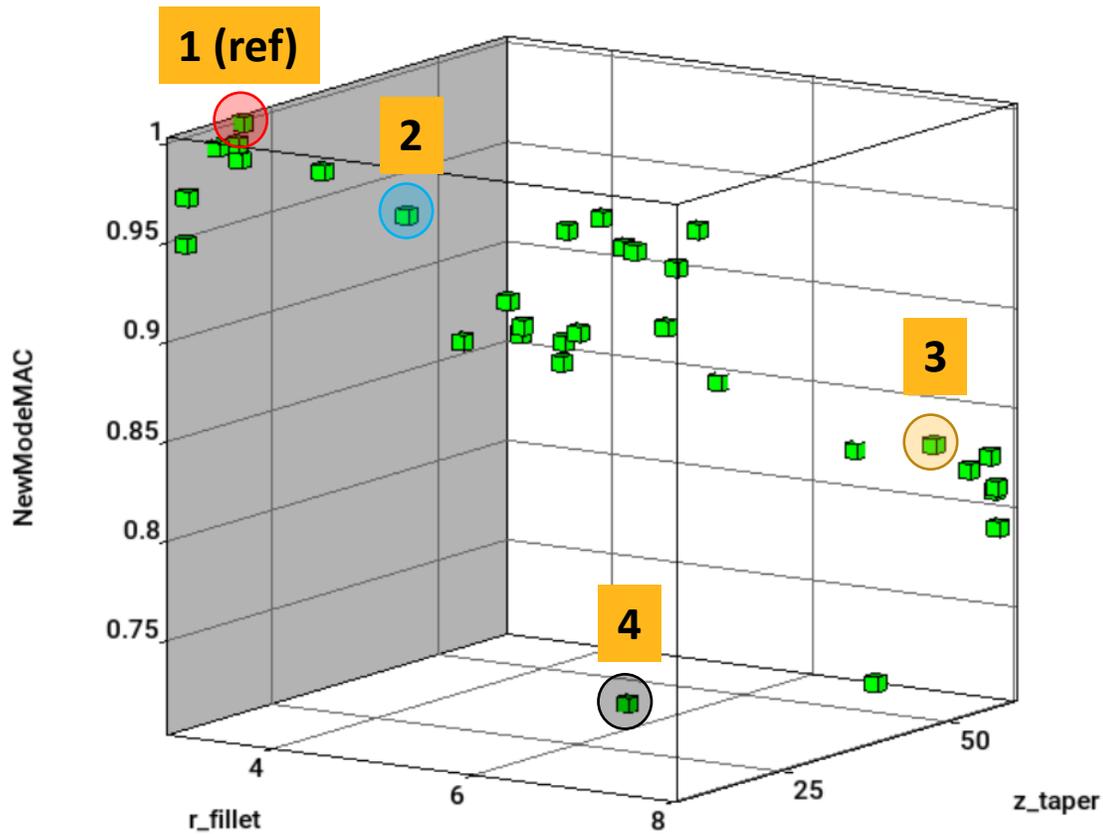
Variables

- Hole center position
- Major axis
- Minor axis
- Extent of taper
- Fillet radius

Baseline Design

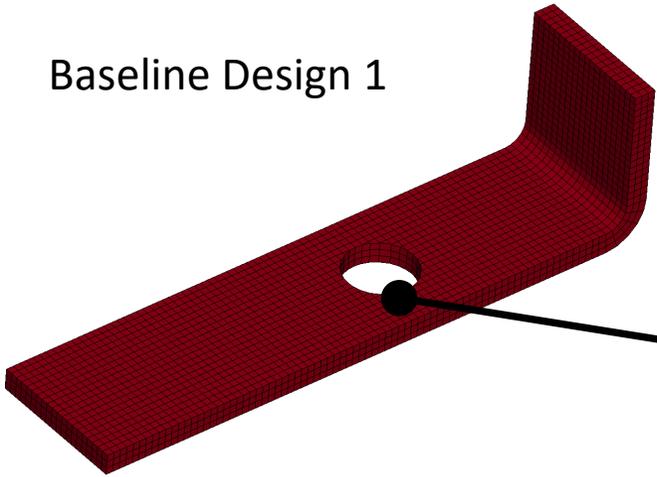
Fixed End

Bent Plate With a Hole and Tapered End: New Modes & MAC

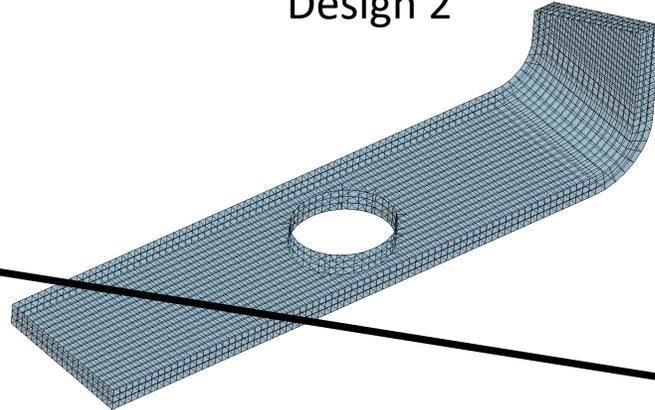


Bent Plate With a Hole and Tapered End: Design 2 Mapping

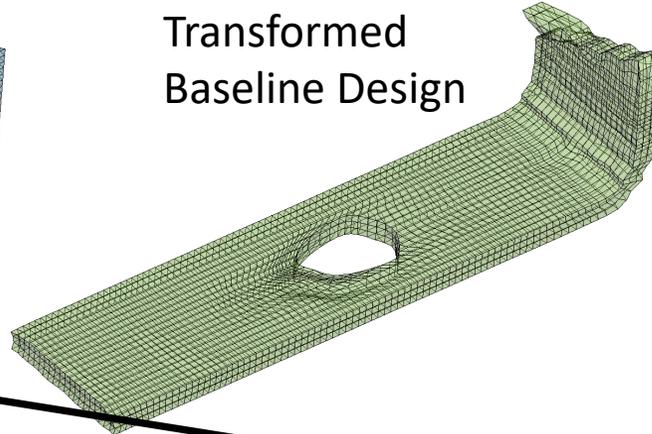
Baseline Design 1



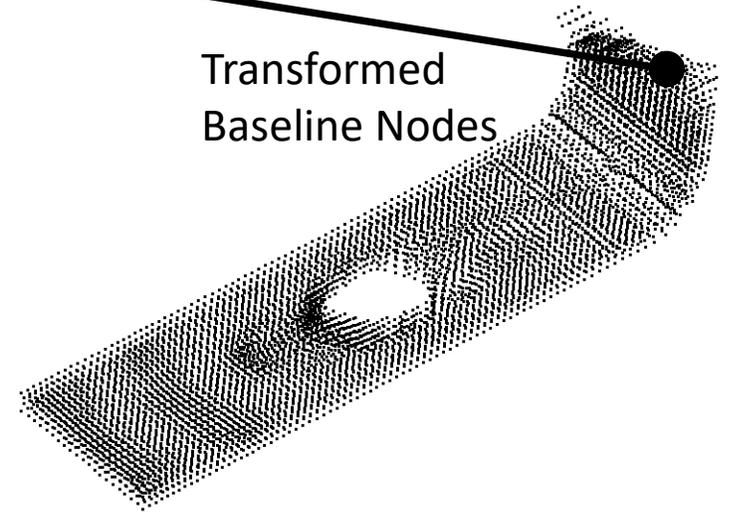
Design 2



Transformed Baseline Design

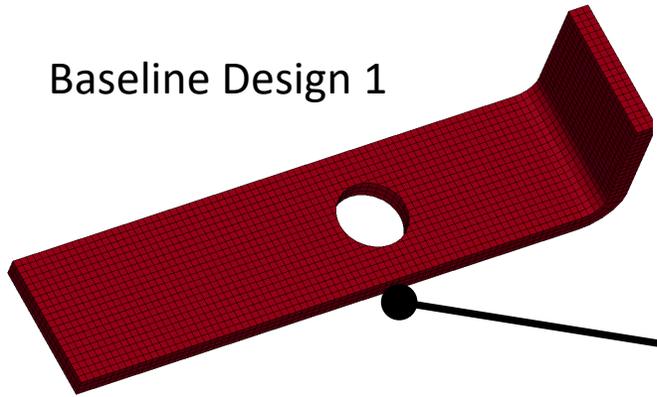


Transformed Baseline Nodes

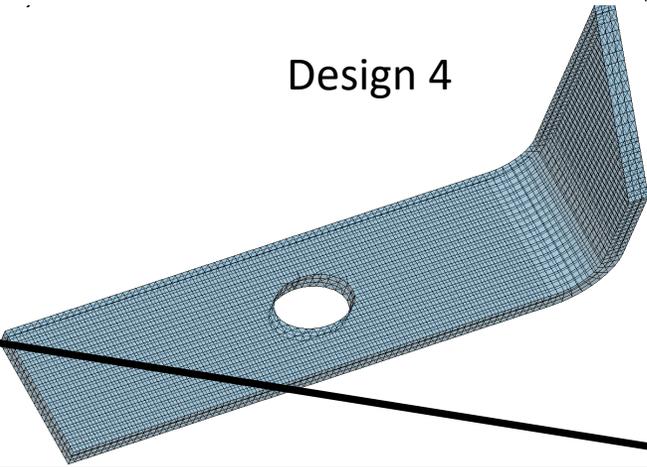


Bent Plate With a Hole and Tapered End: Design 4 Mapping

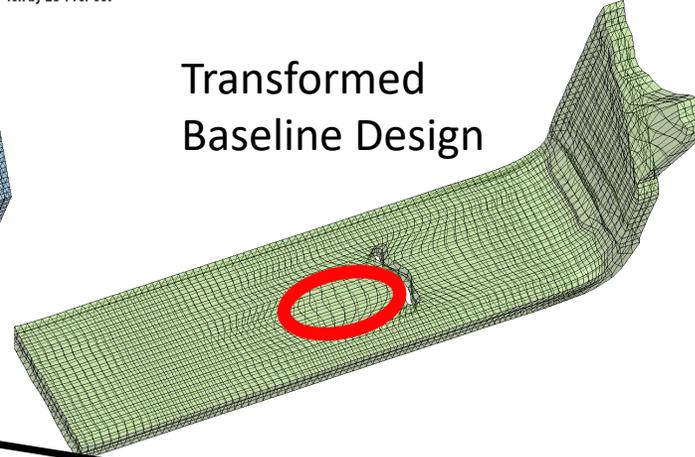
Baseline Design 1



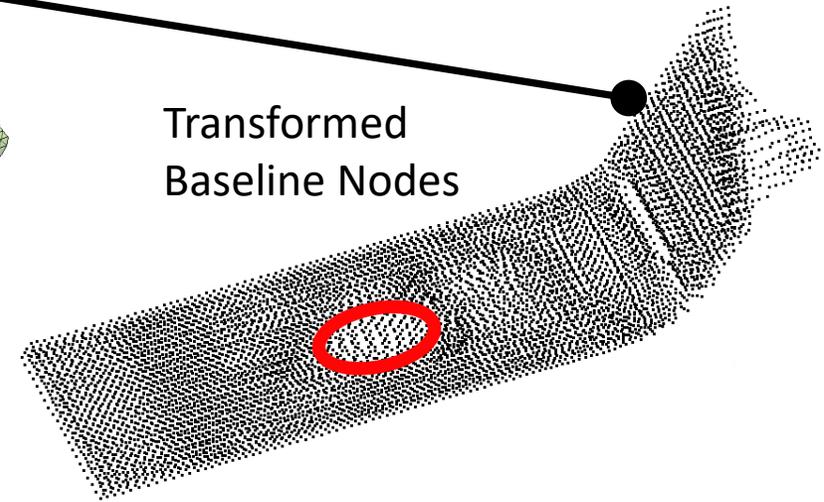
Design 4



Transformed Baseline Design

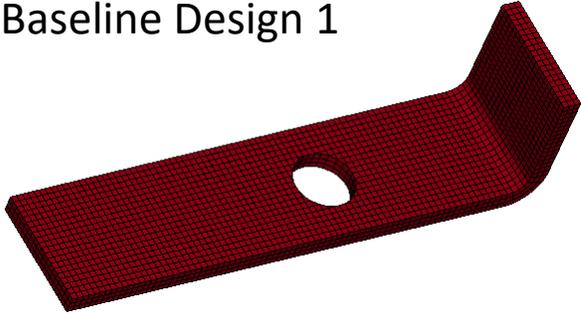


Transformed Baseline Nodes

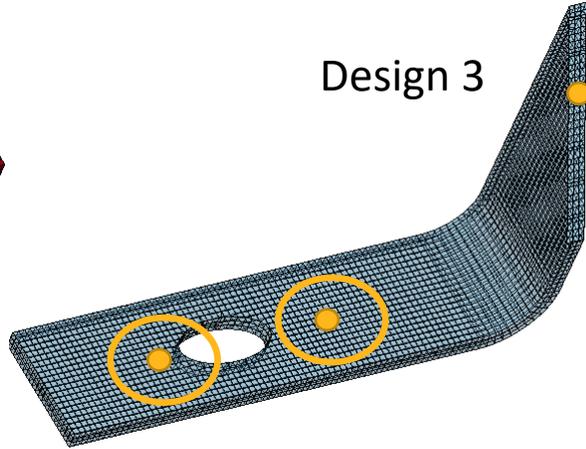


Bent Plate With a Hole and Tapered End: Design 3 Mapping

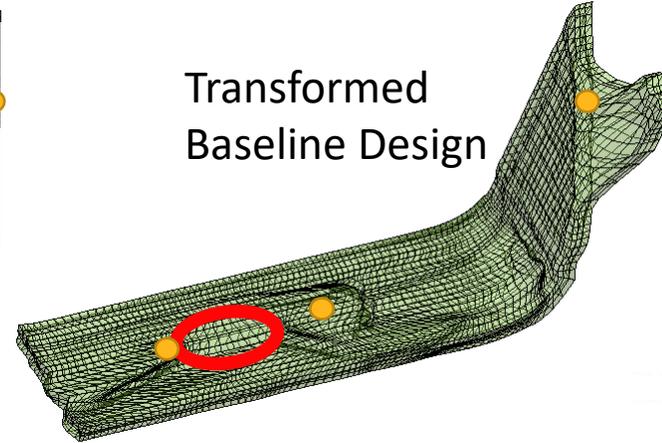
Baseline Design 1



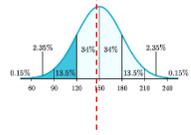
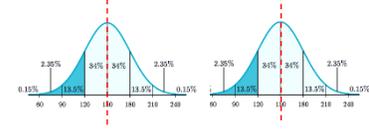
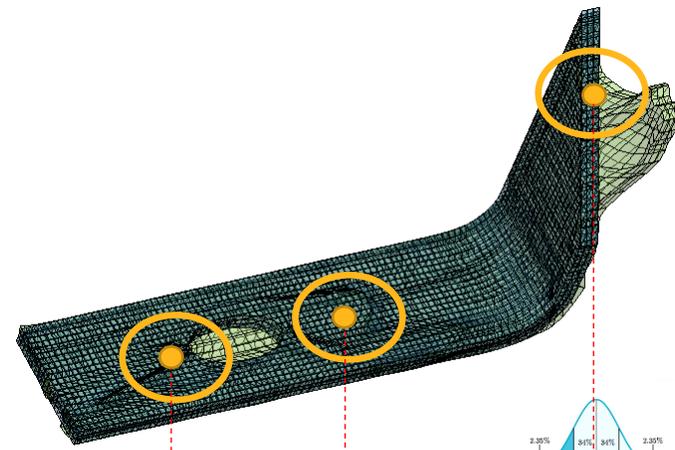
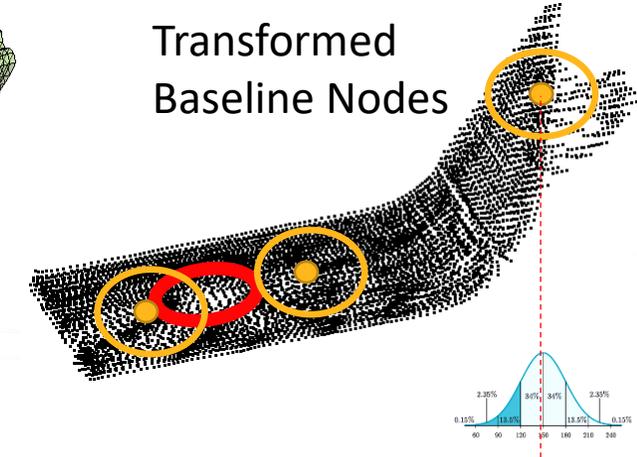
Design 3



Transformed Baseline Design

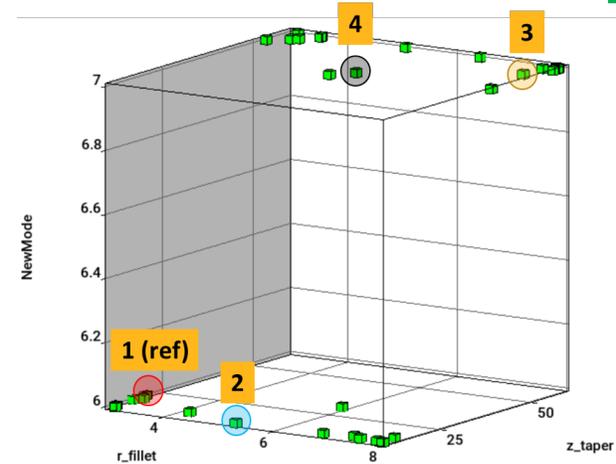
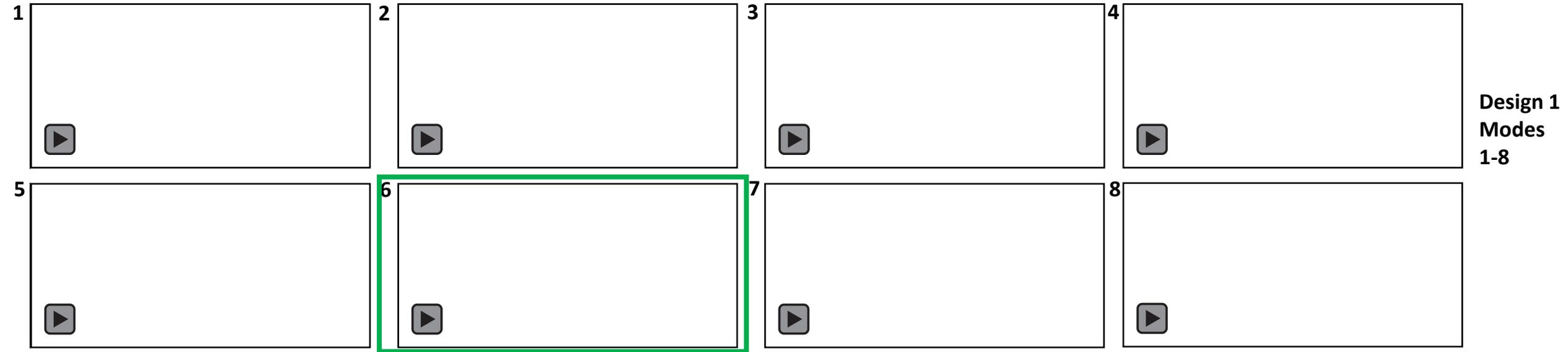


Transformed Baseline Nodes



- There are still some points in regions that should be empty after transformation.
- Such points are spaced out (lower density)
- As distance increases, weightage decreases
- The outlier points have minimal effect
- The transformed mesh isn't used for FE analysis
- Originally empty regions are filled up nicely

Matched Mode Shapes Using IMAC



Design 2 Mode 6



Design 3 Mode 7



Design 4 Mode 7

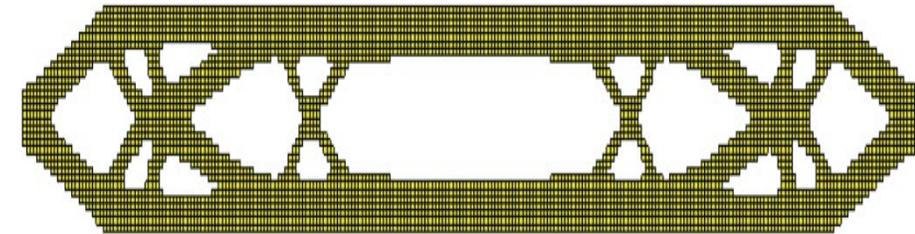


LS-OPT Mode Tracking with LS-TaSC Topology Optimization

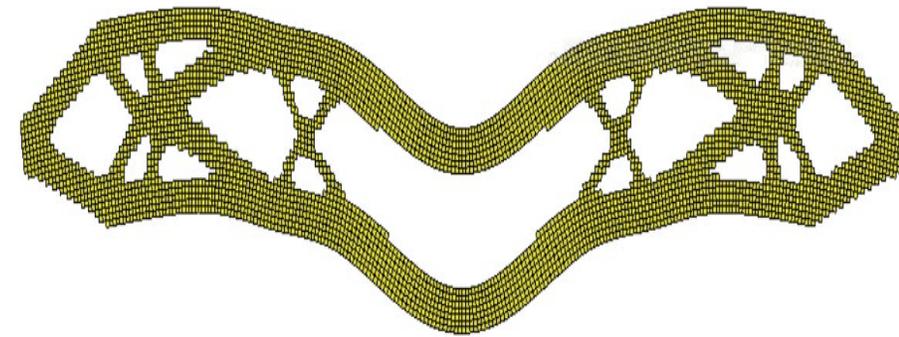
NVH Optimization

- LS-OPT features with LS-TaSC to unlock complex design schemes
- NVH constraint for topology optimization handled using LS-OPT
- Multilevel optimization problem with global and local variables
 - LS-OPT variables: Design part mass fraction
 - LS-TaSC variables: Element densities

Simple Plate Model



Optimized topology at baseline mass fraction

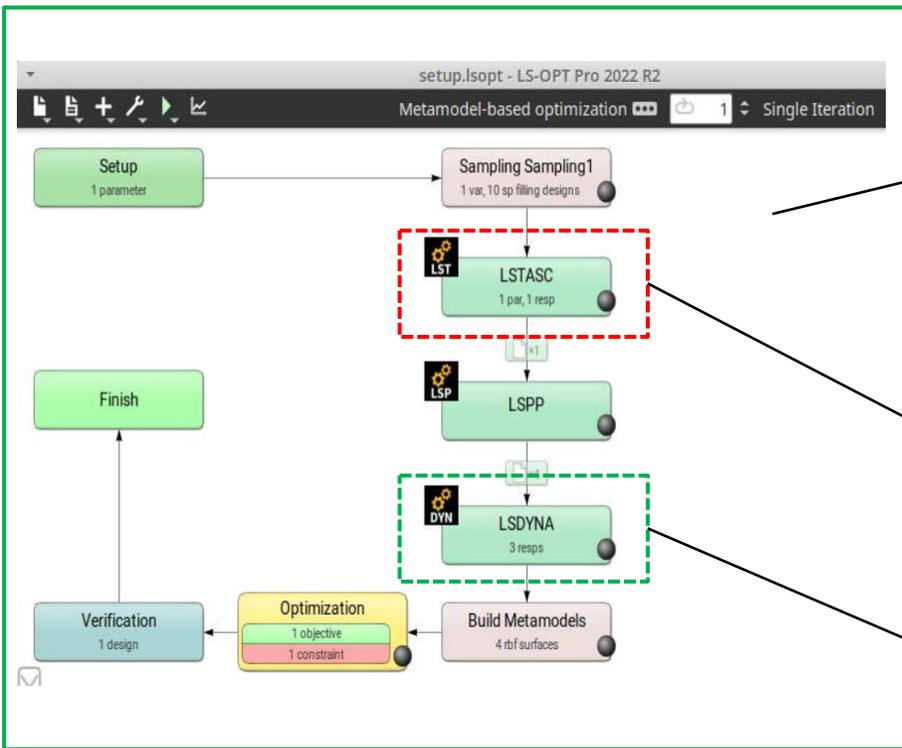


Interested mode shape

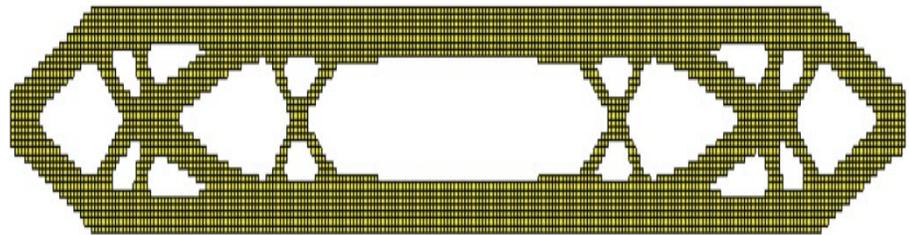
Global problem:
Minimize total mass with
bending frequency constraints and
part mass fraction variables

Local problem:
Unconstrained topology optimization
at constant mass fraction
with element density variables

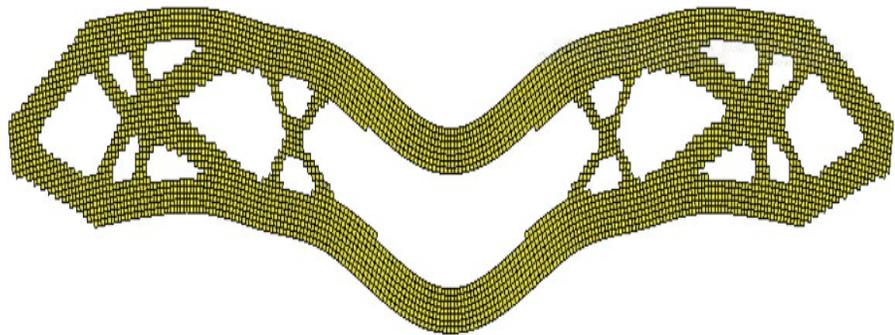
Eigenvalue analysis of
optimized topology



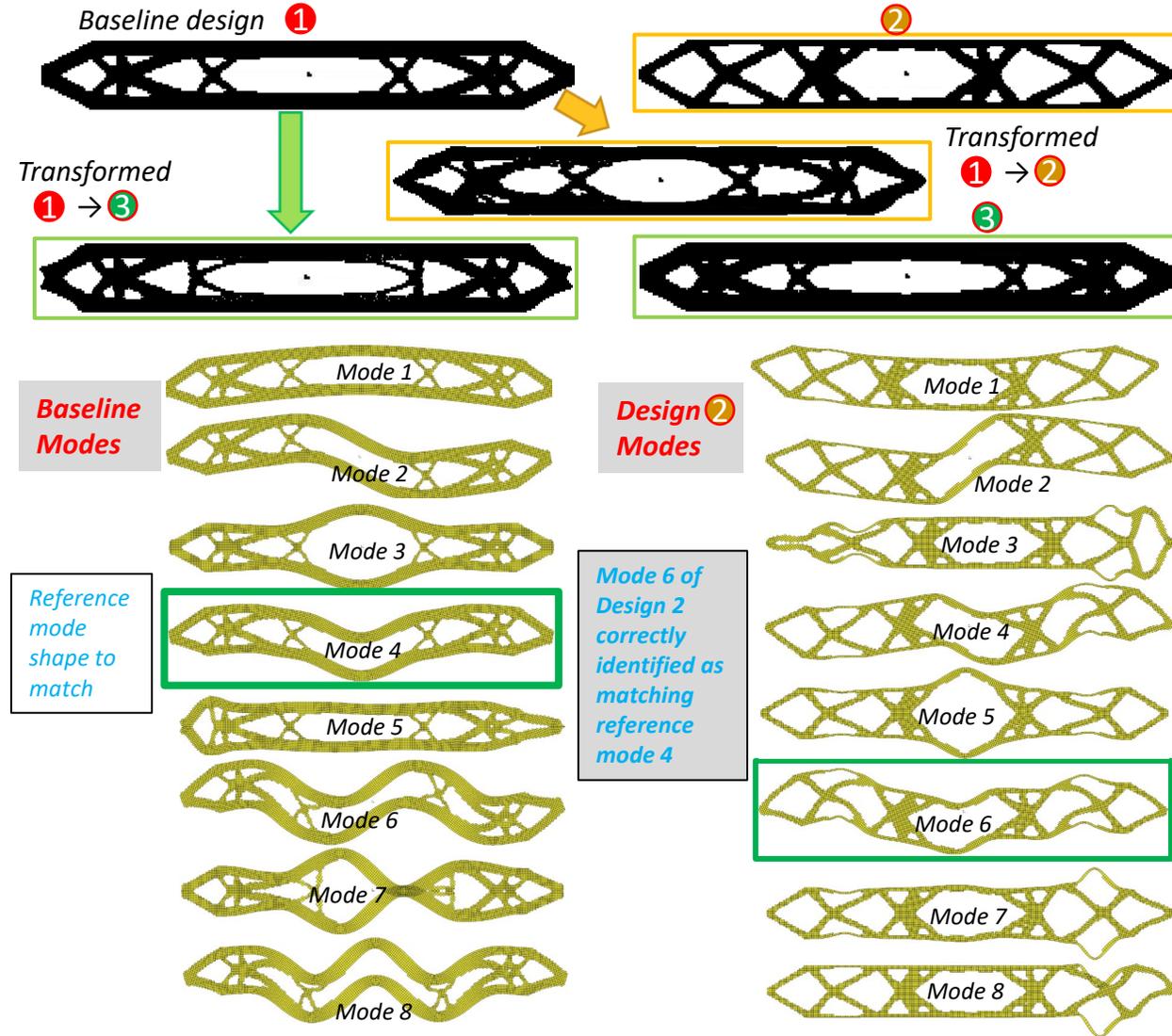
LS-OPT Mode Tracking with LS-TaSC Topology Optimization



Optimized topology at baseline mass fraction

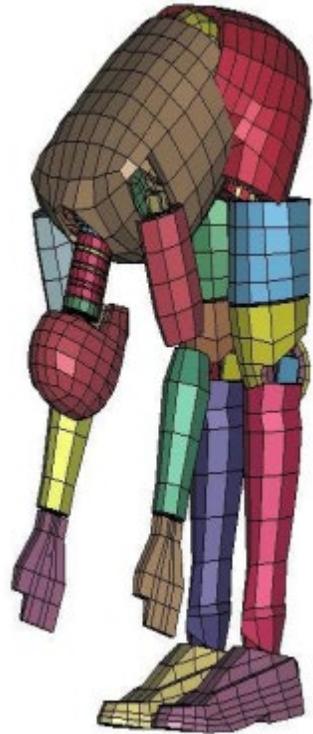


Interested mode shape



Summary and Future Work

- Mode tracking based on MAC has been available in LS-OPT for quite some time, but is limited to designs with same mesh
- Changes in shape and mesh require special handling
- Interpolated MAC (IMAC) based on mapping non-identical sets of nodes has been implemented
- Based on non-rigid Coherent Point Drift (CPD)
- Available in 2023R1
- Work on improving performance is ongoing.



Thank you!!