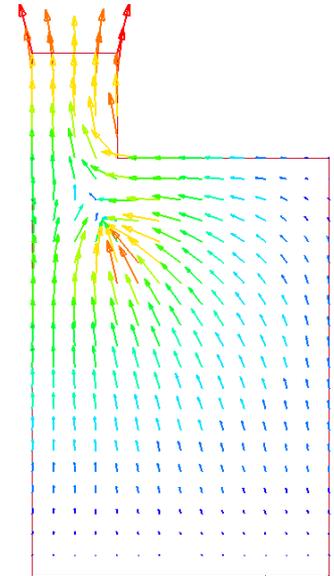
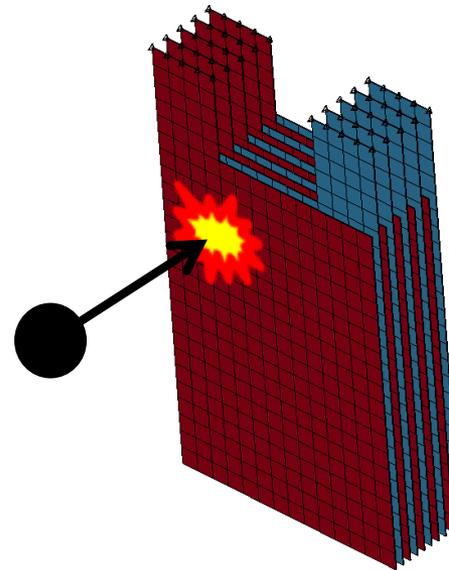
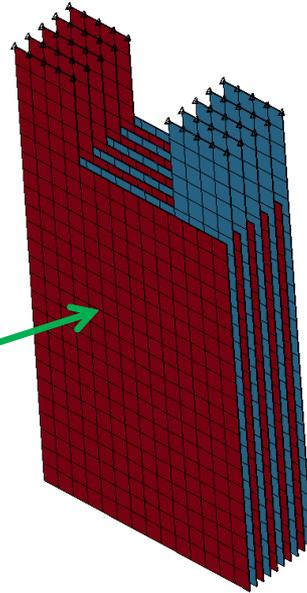


Batteries crash simulation with LS-DYNA



Lithium-Ion
cell

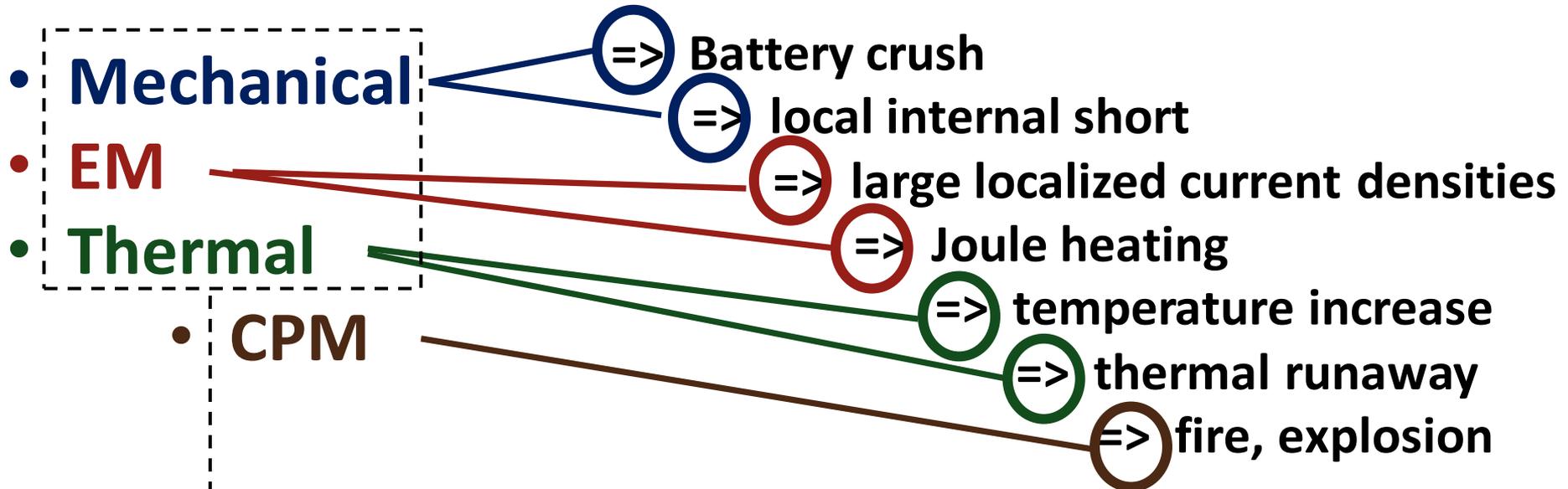


In collaboration with
J. Marcicki et al,
Ford Research and Innovation Center, Dearborn, MI



Battery crash simulation (general)

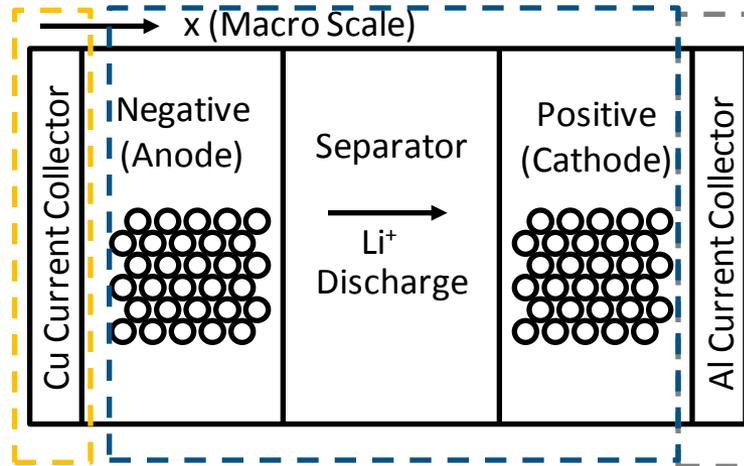
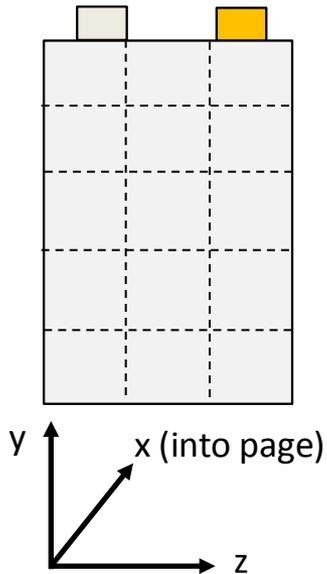
Car crash



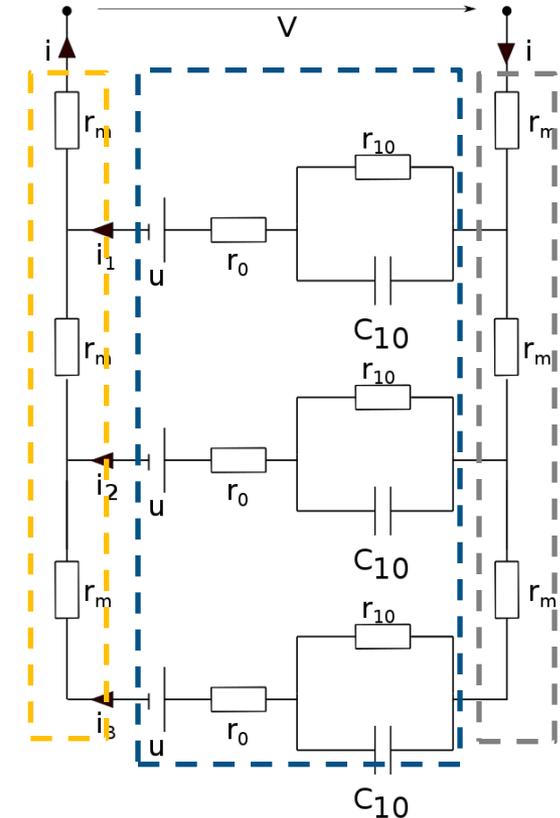
• **CPM**



Distributed Equivalent Circuit (1st Order Randle)



- Current collectors transport electrons to/from tabs; modeled by resistive elements
- Jelly roll (anode – separator – cathode) transports Li^+ ions; modeled with Randle circuit



r_0 : Ohmic & kinetic

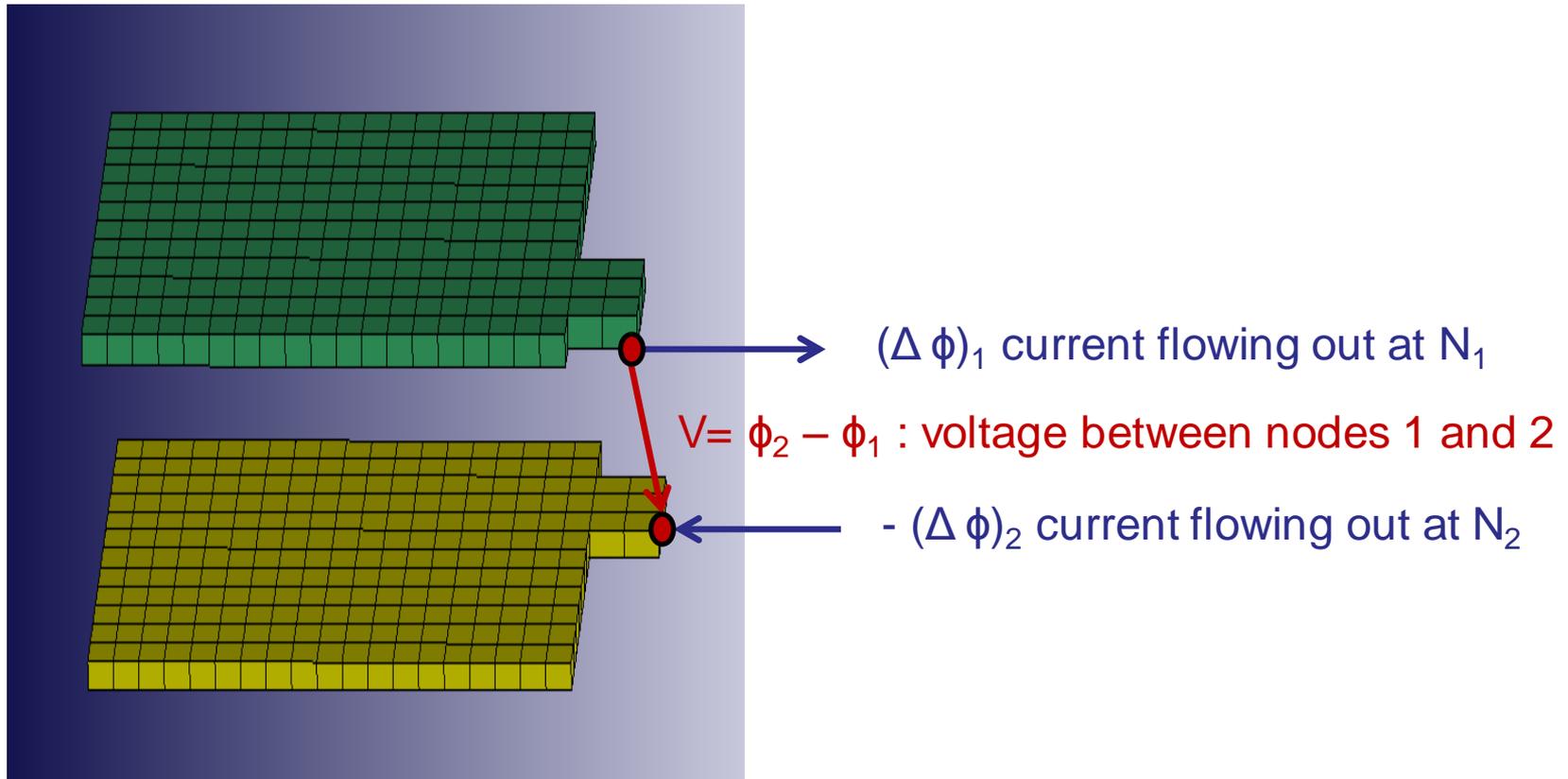
r_{10} & C_{10} : Diffusion

u : Equilibrium voltage (OCV)

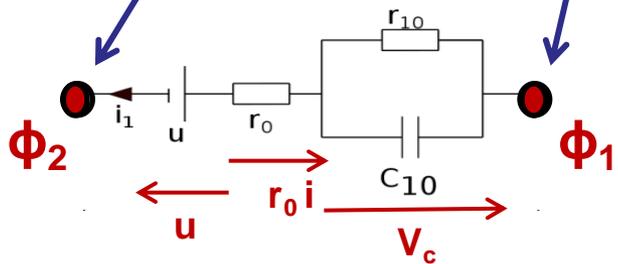
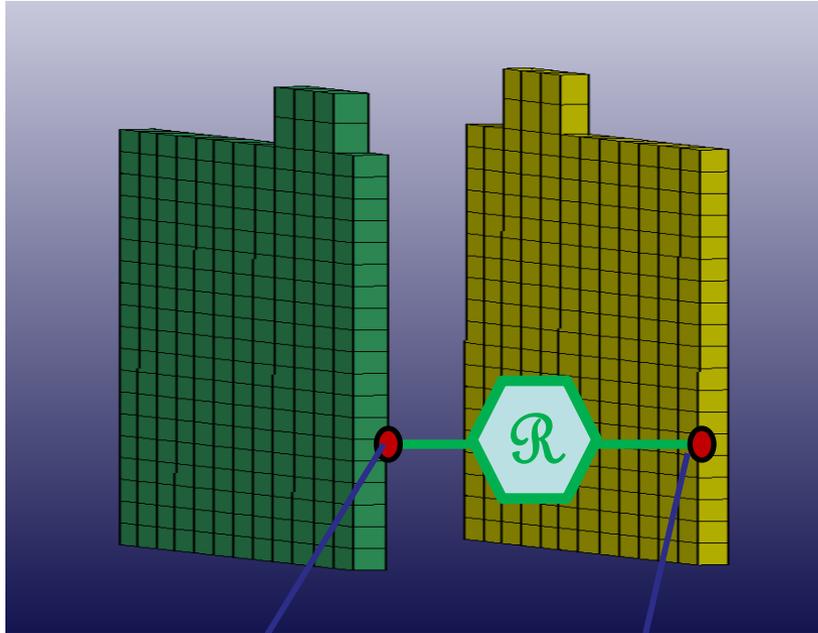
r_m : Current collectors

Standard EM resistive solver

- ϕ : potential
- $E = -\text{grad}(\phi)$: electric field
- $V = \phi_2 - \phi_1$: voltage
- $J = \sigma E$: current density (σ = electric conductivity)
- $\text{div}(J) = 0 \Rightarrow \Delta \phi = 0$ + boundary conditions



Introduction of randle circuits in resistive solver



Randle circuit

Page 5

$$\begin{aligned}\phi_2 - \phi_1 &= u - r_0^* i - V_c \\ r_0^* i + \phi_2 - \phi_1 &= u - V_c \\ i + (\phi_2 - \phi_1) / r_0 &= (u - V_c) / r_0\end{aligned}$$

FEM solve:

$$(S_0 + D) * \phi = b$$

Where

- S_0 is the Laplacian operator (nds x nds)
- D has
 - $1/r_0$ at (N_1, N_1) and (N_2, N_2)
 - $-1/r_0$ at (N_1, N_2) and (N_2, N_1)
 - 0 elsewhere
- b has
 - $1/r_0(u - v_c)$ at N_1
 - $-1/r_0(u - v_c)$ at N_2
 - 0 elsewhere

Actualization of randle circuits:

$$i = (S_0 * \phi)(N_1)$$

$$V_c(t+dt) = V_c(t) + dt * (i/c_0 - V_c(t)/r_{10}/c_{10})$$

$$\text{soc}(t+dt) = \text{soc}(t) - dt * i * c_Q / Q$$

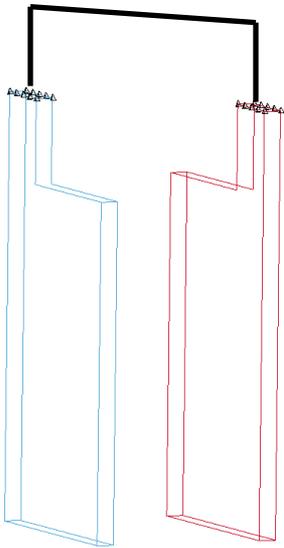
$$u = u(\text{soc})$$

Isopotentials

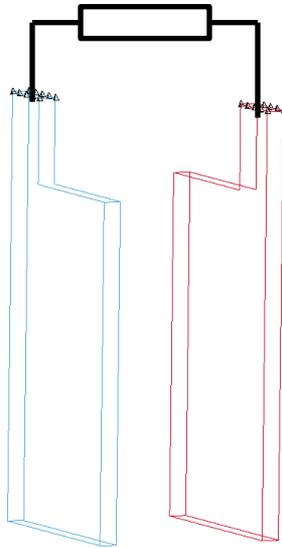
Isopotentials can be defined and connected:

- The connectors do not need to be meshed.
- Enables alignment of cell simulations with experimental conditions (low rate cycling, HPPC, continuous discharge, ...).

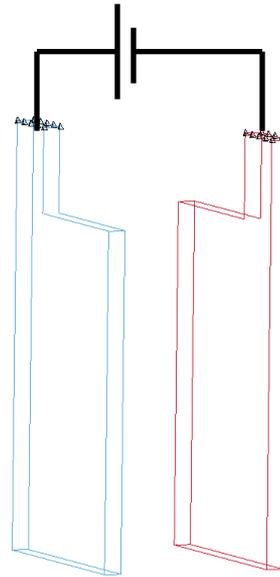
short



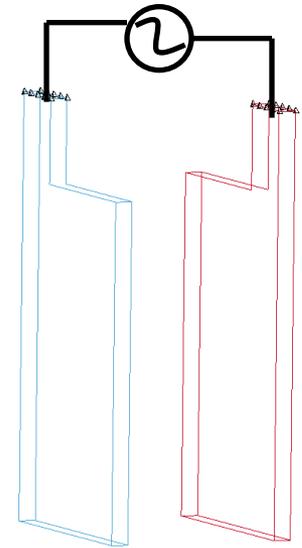
resistance



voltage

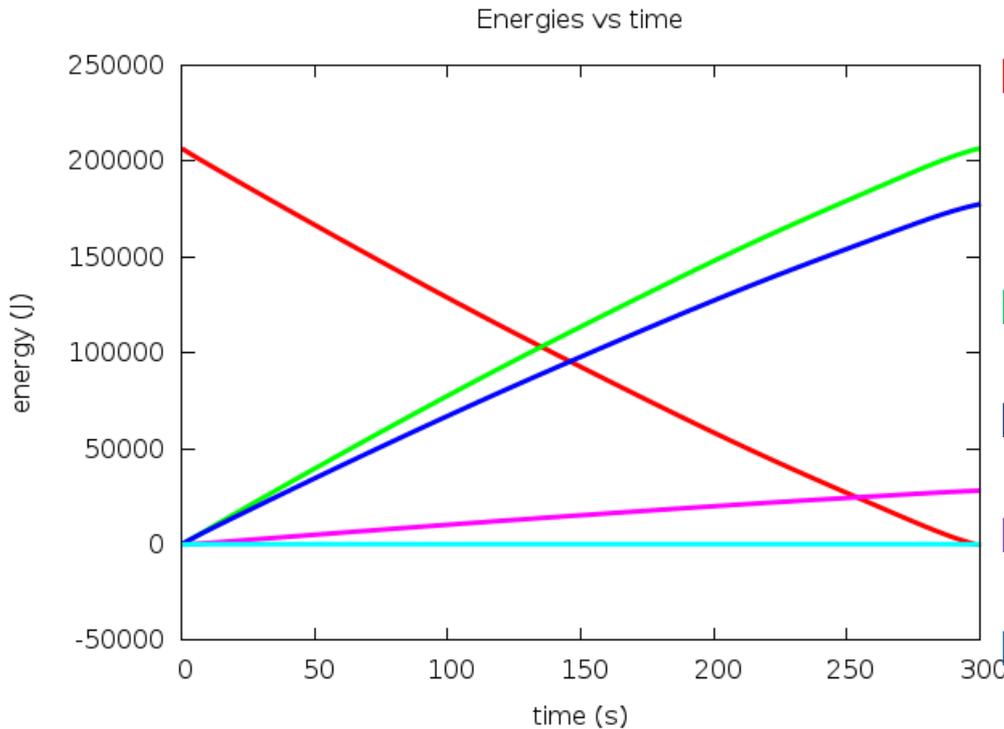


current



Randle circuits energy balance

The different parts of the energy are tracked down



$$\begin{aligned}
 E_{\text{available}} &= \sum_{\text{randle}} \int (u(t) \cdot i(t)) dt \\
 &= \sum_{\text{randle}} \int u dq \\
 &= \sum_{\text{randle}} Q/cQ \int u(\text{SOC}) d \text{SOC}
 \end{aligned}$$

$$E_{\text{delivered by } u} = \sum_{\text{randle}} \int u \cdot i dt$$

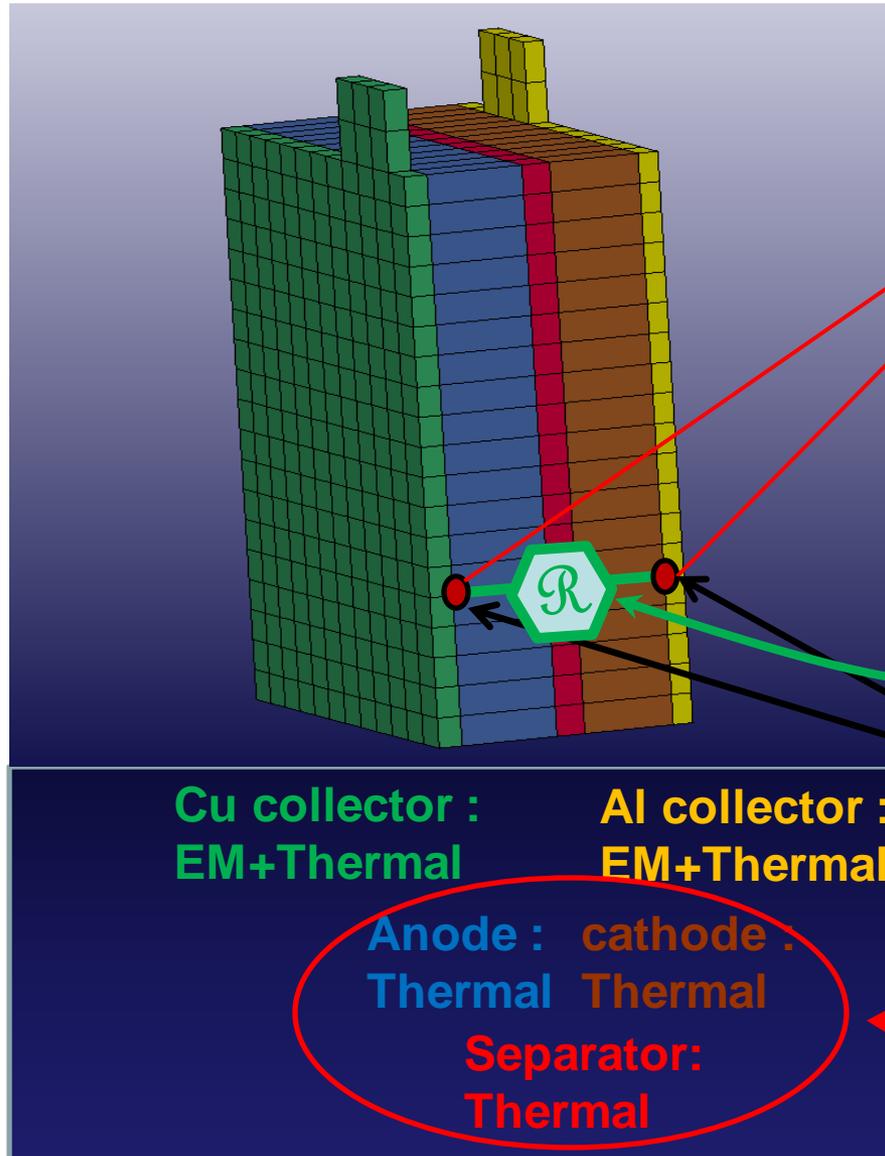
$$E_{\text{delivered to load}} = \sum_{\text{randle}} \int u_{\text{load}} \cdot i_{\text{load}} dt$$

$$E_{\text{joule heating in } r_0} = \sum_{\text{randle}} \int r_0 \cdot i^2 dt$$

$$E_{c10} = \sum_{\text{randle}} 1/2 C_{10} \cdot V_c^2$$

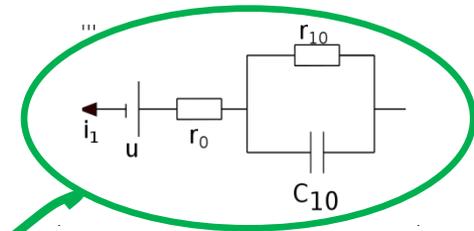
Typical discharge of unit cell in a resistance

EM/thermal connection



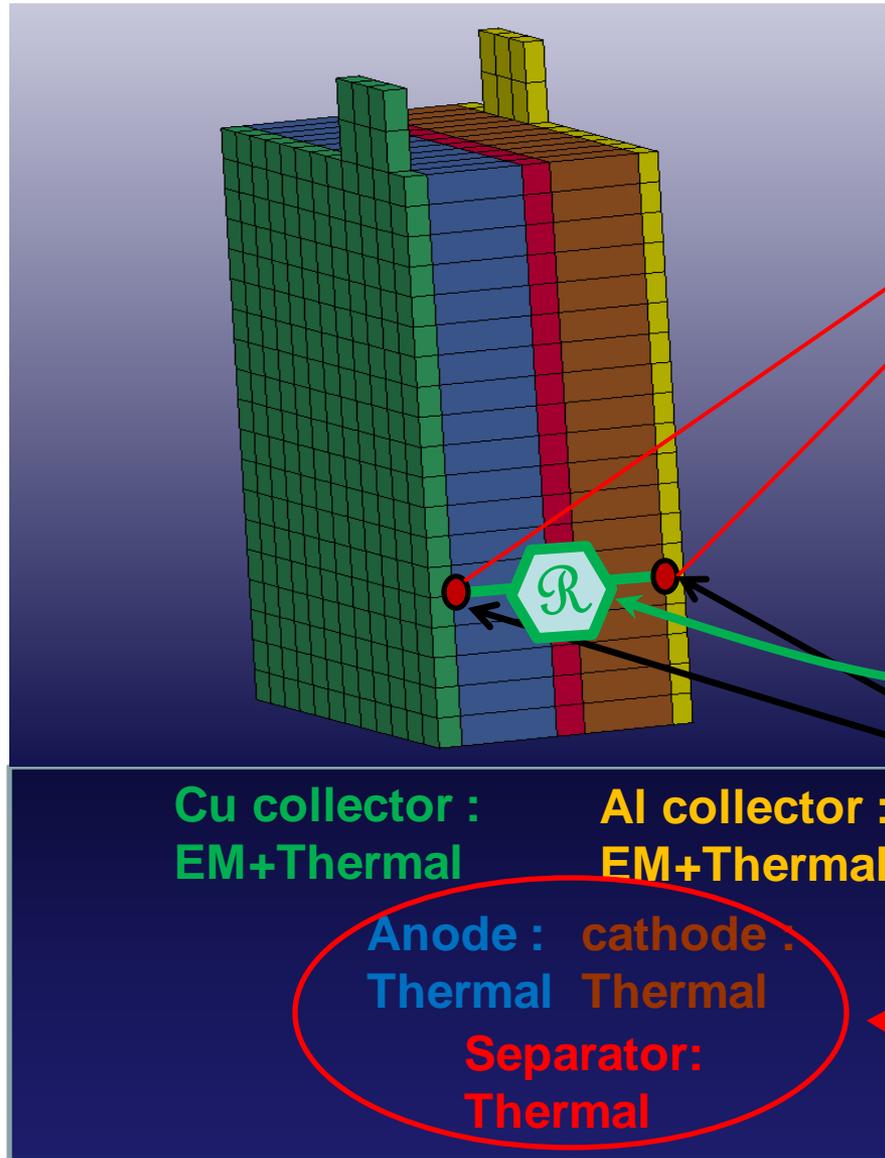
T from thermal for r_0, r_{10}, C_{10} vs T

Randle circuit



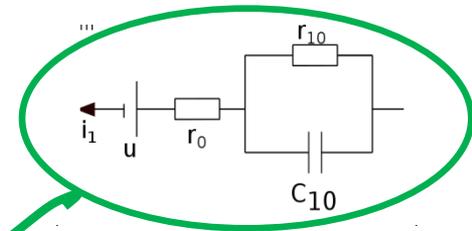
$r_0 * i^2$ added to thermal
 $ITdU/dT$ added to thermal

Allow correct material mass, heat capacity and thermal conductivity



T from thermal for r_0, r_{10}, C_{10} vs T

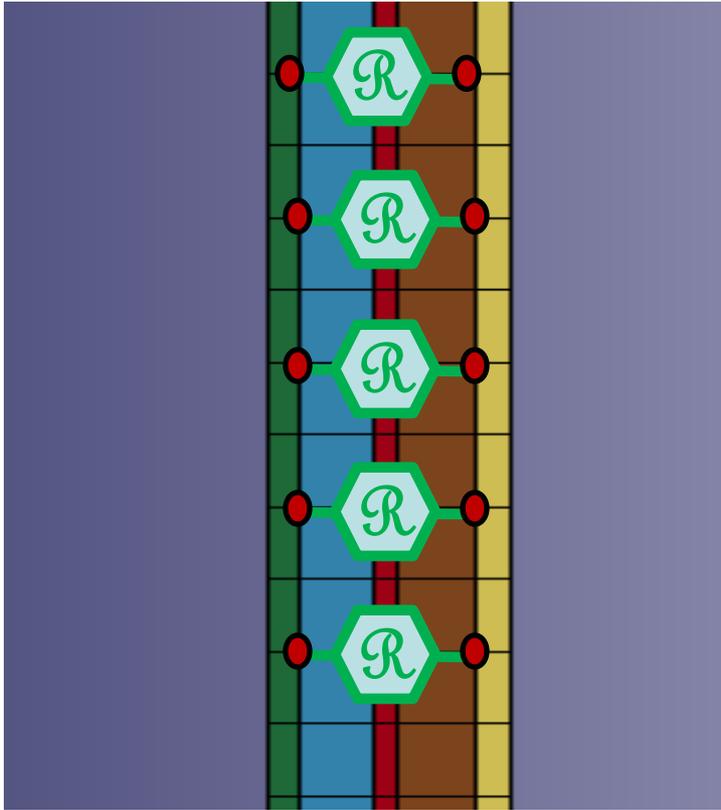
Randle circuit



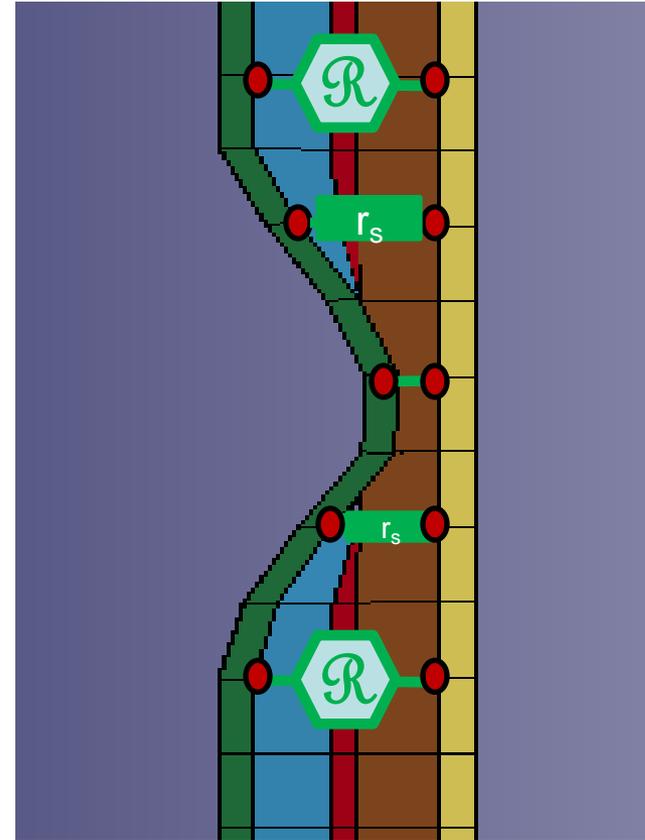
$r_0 * i^2$ added to thermal
 $ITdU/dT$ added to thermal

Allow correct material mass, heat capacity and thermal conductivity

Contact for Internal Short Models

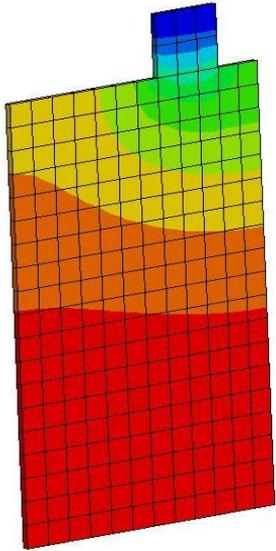


Replace randle circuit by resistance r_s
 $R_s * i^2$ added to thermal

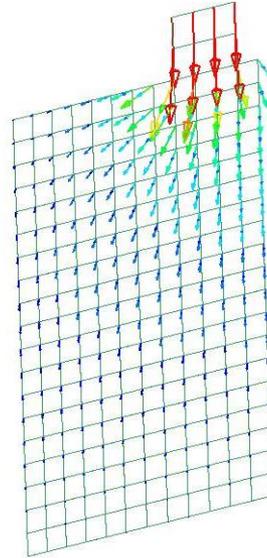


Experiment + simulation
(voltage, current, temperature)
should give good models

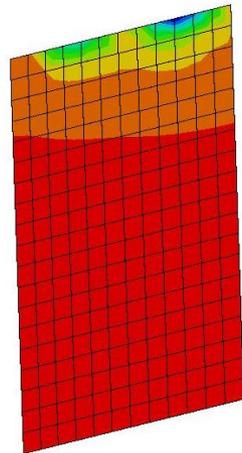
Randle circuits in LS-PREPOST



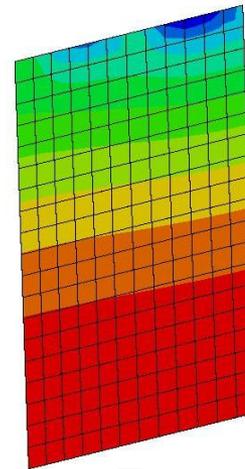
Scalar potential



Current density



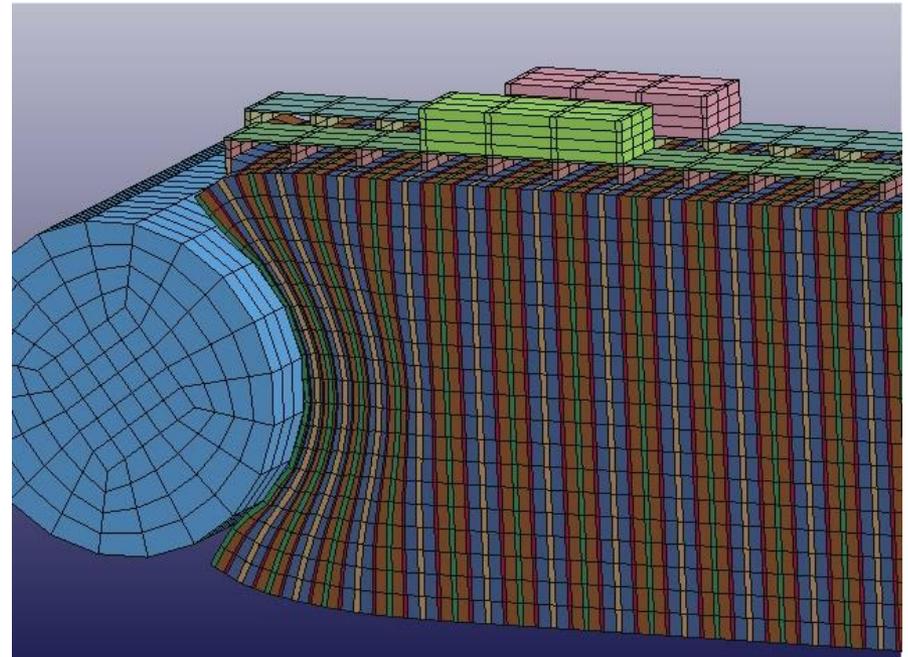
Randle r0



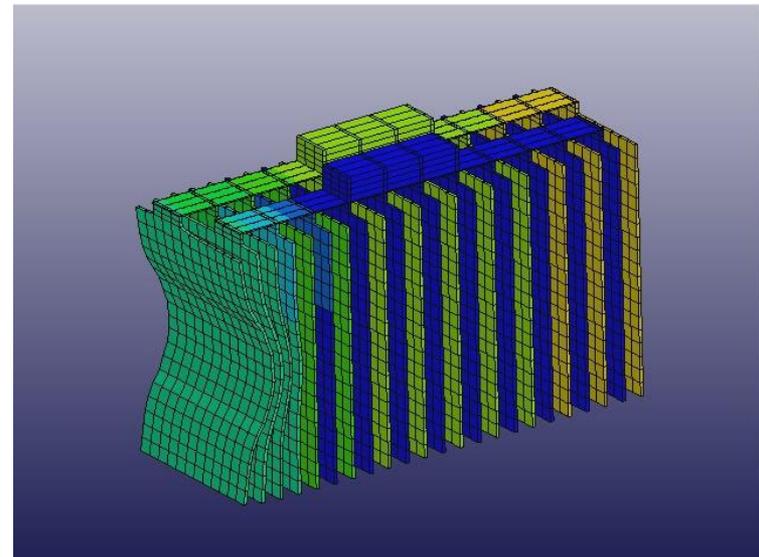
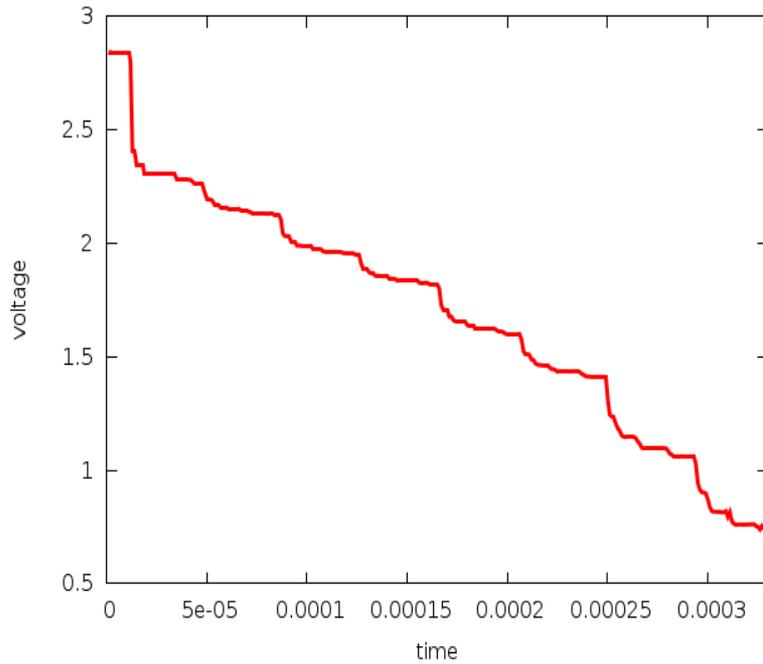
Randle SOC

Contact illustration (1)

- Mechanical models for cells with very thin layers of materials of very different stiffnesses are still under investigation.
- In the meanwhile, in order to avoid the difficulties of the small thicknesses, model where the thickness was * 100, as proof of principle
- Rod crushes cell with 22 unit cells

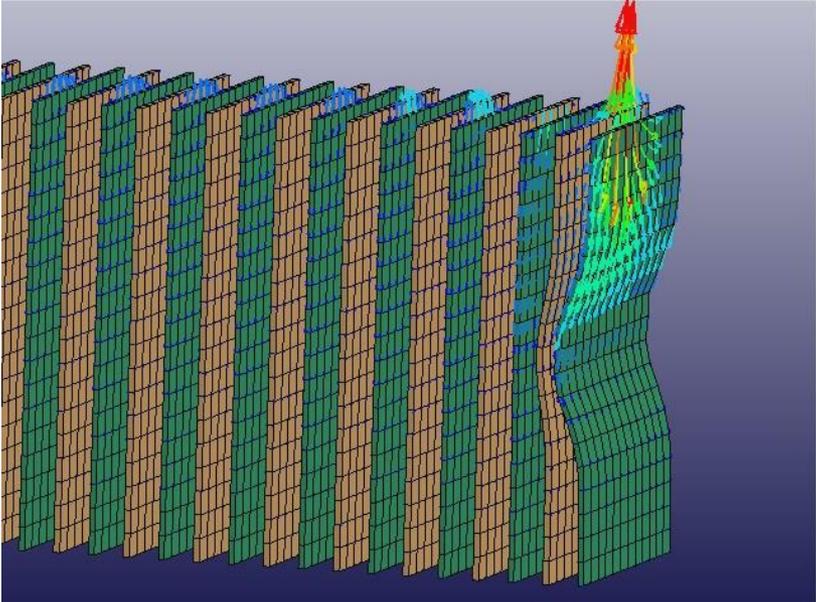


Contact illustration (2)

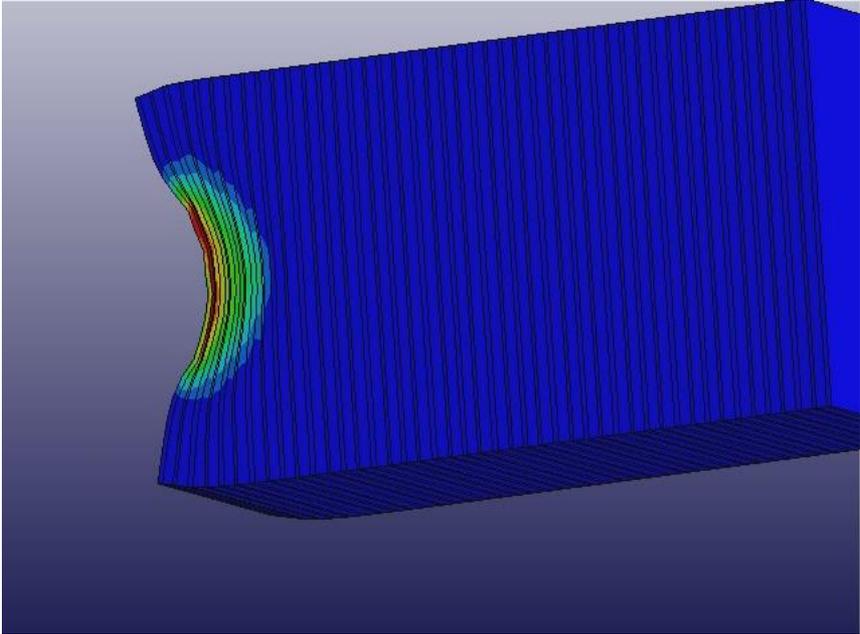


Voltage vs time

Contact illustration (3)



Current density



Temperature

More at
the 14th International LS-DYNA User's Conference
Dearborn, MI, June 12-14, 2016

A Distributed Randle Circuit Model for Battery Abuse Simulations Using LS-DYNA®

Pierre L'Eplattenier¹, İñaki Çaldichoury¹

James Marcicki², Alexander Bartlett², Xiao Guang Yang²,

Valentina Mejia², Min Zhu², Yijung Chen²

¹*LSTC, Livermore, CA, USA*

²*Ford Research and Innovation Center, Dearborn, MI, USA*

Battery Abuse Case Study Analysis Using LS-DYNA

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