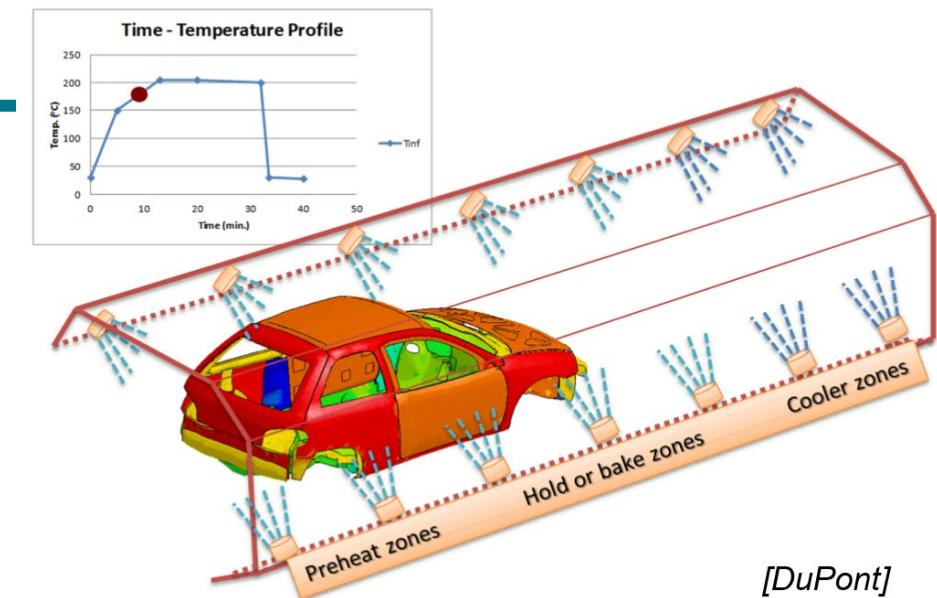


North American LS-DYNA User Forum 2023 – Novi, MI – Nov 16, 2023

# Recent enhancement for modelling adhesives in the closed manufacturing crashworthiness process chain

Dr.-Ing. Thomas Klöppel, Tobias Aubel

DYNAmore GmbH an Ansys Company, Stuttgart



[DuPont]

# This Presentation is a Sequel

16<sup>th</sup> LS-DYNA Forum 2022 , Bamberg



New material MAT\_307:  
A viscoelastic-viscoplastic constitutive formulation to model adhesives during the complete manufacturing-crashworthiness process chain

Thomas Klöppel, André Haufe  
DYNAmore GmbH



ARENA2036



# Recap

---

Most important points from last year's presentation

## Motivation: Adhesive Process chain



### ■ Manufacturing

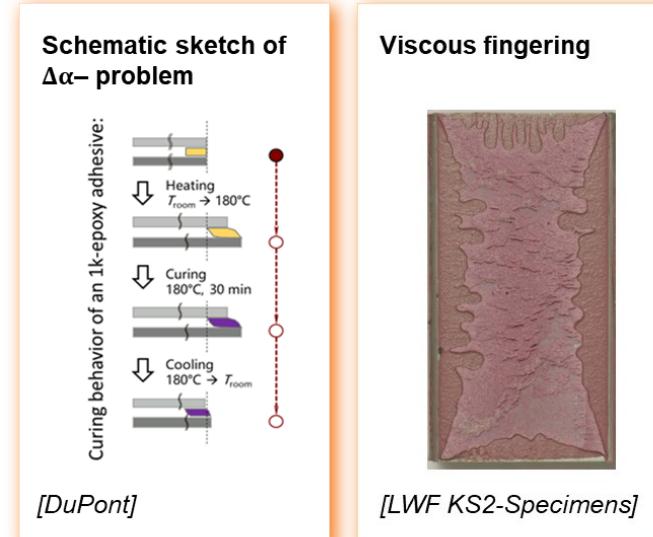
- Adhesive is applied to body in white during assembly
- Curing is activated by elevated temperatures during the drying process after cathodic dip painting
- Joining different materials may result in  $\Delta\alpha$ - problem
- Viscous fingering effect if joining partners separate

### ■ Crashworthiness

- Complex plasticity behavior with volume change under plastic deformation and non-associated flow rules
- Temperature and cure dependent material damage

### ■ Already existing or proposed material models

- \*MAT\_252 (TAPO), \*MAT\_277, UMAT for a modified TAPO model [Matzenmiller and Kühlmeyer, 2018]



Mercedes-Benz

DUPONT

inpro

ARENA2036

DYNA  
MORE

LWF

IFB  
Institut für Flugzeugbau

TÜV Rheinland<sup>®</sup>  
Genau. Richtig.

## \*MAT\_307: Viscoelasticity – Shifting Operations



- Prony series expansion for shear modulus  $G(t)$  and bulk modulus  $K(t)$

$$G(t) = G_\infty + \sum_i G_i \cdot e^{-\beta_i^G t} = G_0 - \sum_i G_i + \sum_i G_i \cdot e^{-\beta_i^G t}$$

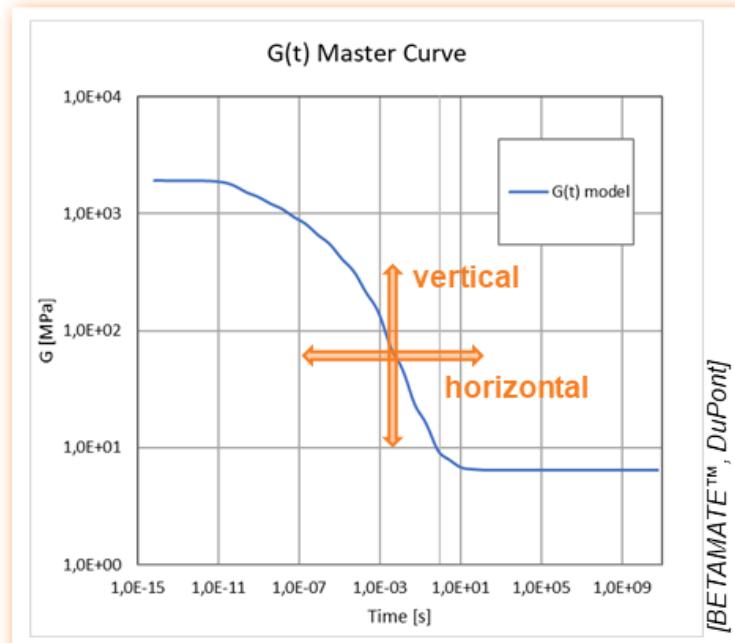
- Horizontal shift operations of a master curve

- Scaling of the decay parameters  $\beta_i^G$  and  $\beta_i^K$
- Scaling factors are  $a_T^G, a_p^G$  for shear and  $a_T^K, a_p^K$  for bulk

- Vertical shift operations of a master curve

- Scaling of  $G_i$  and  $K_i$  or of  $G(t)$  and  $K(t)$
- Scaling factors are  $b_T^G, b_p^G$  for shear and  $b_T^K, b_p^K$  for bulk

	1	2	3	4	5	6	7	8
Card 5	THOPT	TH1	TH2	TH3	TH4			
Card 6	TVOPT	TV1	TV2					
Card 7	PHOPT	PH1	PH2	PH3	PH4	PH5	PH6	
Card 8	PVOPT	PV1	PV2	PV3	PV4			
...	...	...	...	...	...	...	...	...

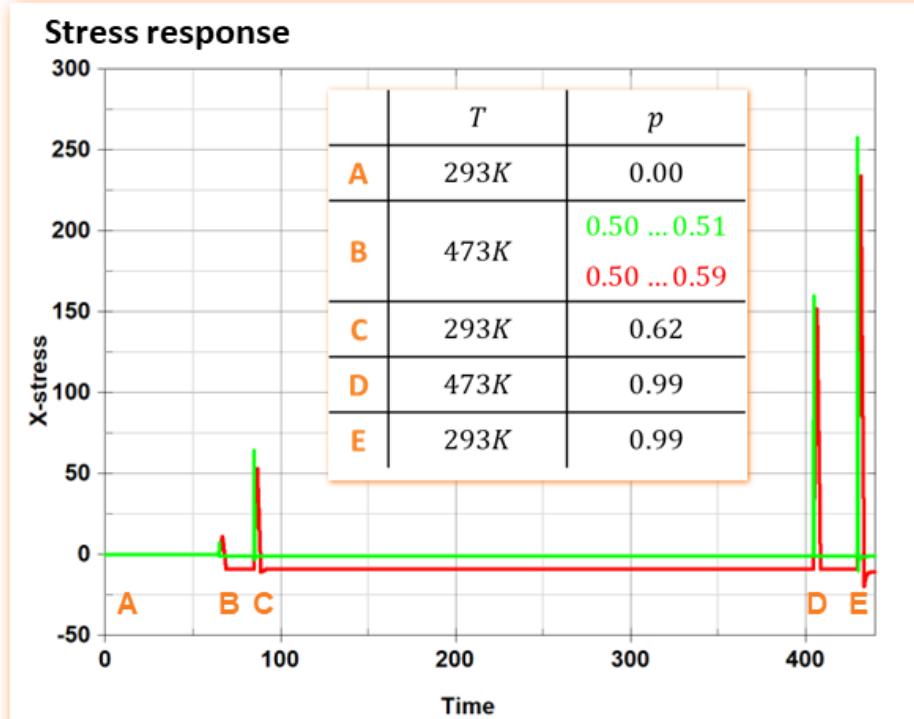
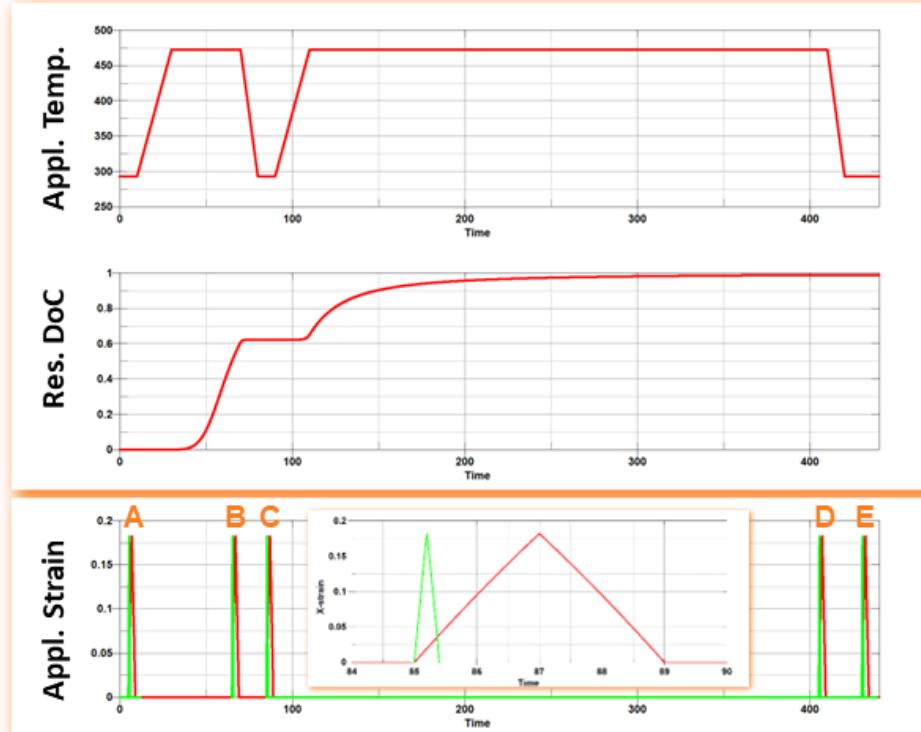


# Recap

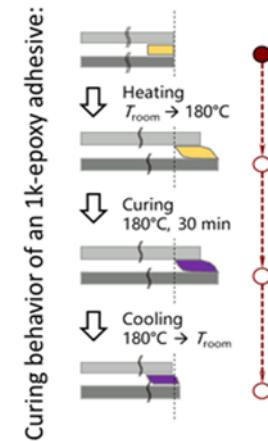
## \*MAT\_307: Viscoelasticity – Proof of Concept



### ■ Single element relaxation and hysteresis test



### Schematic sketch of $\Delta\alpha$ -problem



[DuPont]



Bundesministerium  
für Wirtschaft  
und Klimaschutz



Mercedes-Benz



ARENA2036



TÜV Rheinland®  
Genau. Richtig.

8

# Recap

## \*MAT\_307: Plasticity

	1	2	3	4	5	6	7	8
...	...	...	...	...	...	...	...	...
Card 9	<b>PL1OPT</b>	<b>PL11</b>	<b>PL12</b>	<b>PL13</b>	<b>PL14</b>	<b>PL15</b>		
Card10	<b>PL2OPT</b>	<b>PL21</b>	<b>PL22</b>	<b>PL23</b>	<b>PL24</b>	<b>PL25</b>	<b>PL26</b>	
...	...	...	...	...	...	...	...	...

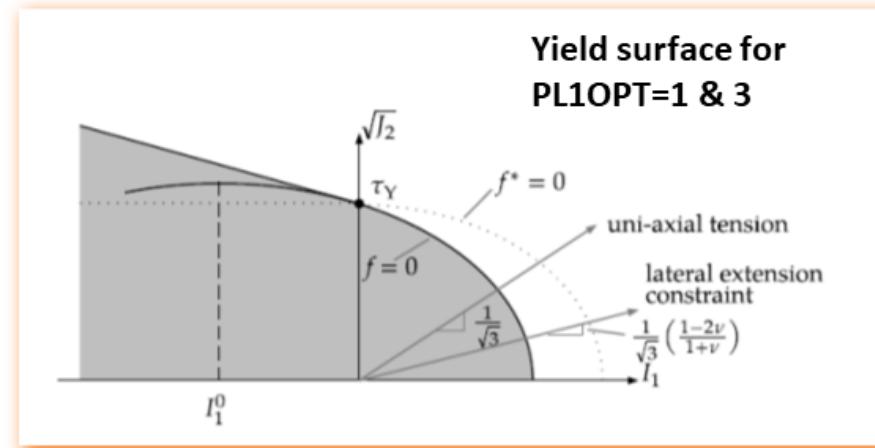


### ■ Plasticity formulation based on (extended) TAPO

- Non-associated  $I_1$ - $J_2$  - plasticity
- Cap in tension and Drucker & Prager in compression
- Distortional hardening with respect to temperature

### ■ Card 9 defines flow function $f$ and potential $f^*$

- Card 10 defines the yield strength  $\tau_Y$  as function of temperature  $T$  and degree of cure  $p$



Bundesministerium  
für Wirtschaft  
und Klimaschutz



Mercedes-Benz



**ARENA2036**



**TÜV Rheinland**  
Genau. Richtig.

10

## \*MAT\_307: Damage and Failure



	1	2	3	4	5	6	7	8
...	...	...	...	...	...	...	...	...
Card11	DAOPT	DAEVOFLG	DATRIAX	DA1	DA2	DA3	DA4	DA5
Card12	DA6	DA7	DA8	DA9	DA10	DA11	DA12	DA13
...	...	...	...	...	...	...	...	...

### ■ Two damage mechanisms are considered

- Material damage based on \*MAT\_252 (TAPO, Matzenmiller and Burbulla 2013) denoted by  $D_1$
- (Pre-) damage formulation for the effect of viscous fingering with damage parameter  $D_2$

### ■ Effective stress tensor $\tilde{\sigma}$ is given as

$$\tilde{\sigma} = \frac{\sigma}{(1 - D_1)(1 - D_2)}$$

### ■ Integration point failure is initiated as soon as one of the damage parameters is 1.0

## \*MAT\_307: Material Damage $D_1$

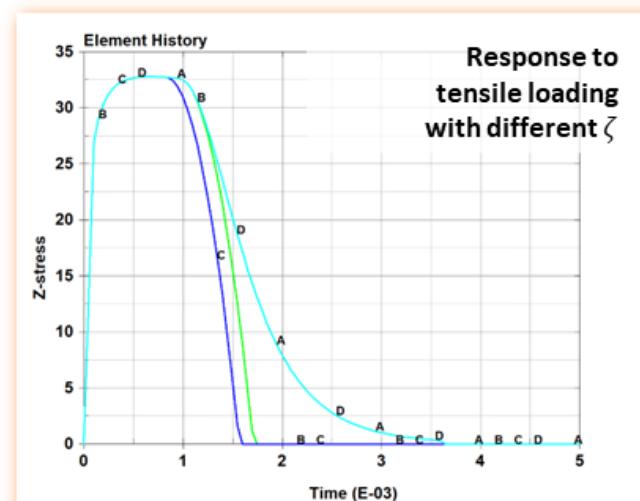
	1	2	3	4	5	6	7	8
...	...	...	...	...	...	...	...	...
Card11	DAOPT	DAEVOFLG	DATRIAX	DA1	DA2	DA3	DA4	DA5
Card12	DA6	DA7	DA8	DA9	DA10	DA11	DA12	DA13
...	...	...	...	...	...	...	...	...



- Empirical isotropic damage model based on Lemaitre [1985]

$$\dot{D}_1 = \dot{D}_1(\zeta, \dot{\zeta}) = n \left( \frac{\zeta - \gamma^c}{\gamma^f - \gamma^c} \right)^{n-1} \frac{\dot{\zeta}}{\gamma^f - \gamma^c}, \quad \dot{\zeta} \in \{\dot{r}, \dot{\gamma}_v, \dot{\gamma}\}$$

- Parameter DAOPT defines the strain thresholds  $\gamma^f$  and  $\gamma^c$
- Parameter DAEVOFLG defines effective strain measure  $\zeta$ 
  - arc length of damage plastic strain rate,
  - arc length of plastic strain rate,
  - arc length of viscoelastic strain rate



# Recap

## \*MAT\_307: (Pre-)Damage $D_2$

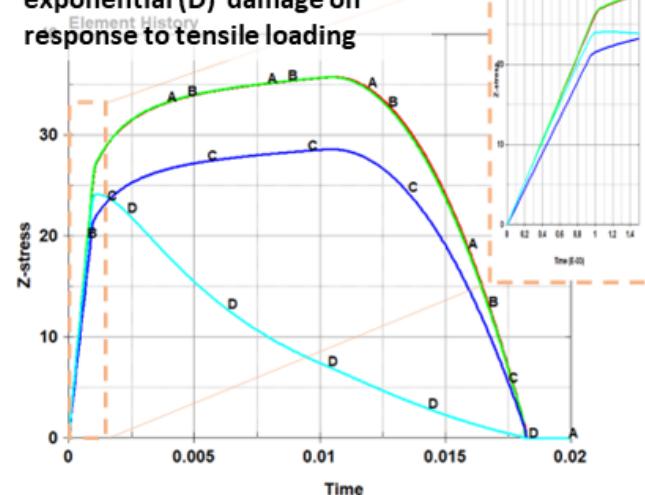
	1	2	3	4	5	6	7	8
...	...	...	...	...	...	...	...	...
Card11	DAOPT	DAEVOFLG	DATRIAX	DA1	DA2	DA3	DA4	DA5
Card12	DA6	DA7	DA8	DA9	DA10	DA11	DA12	DA13
...	...	...	...	...	...	...	...	...



### ■ Damage description

- Damage equivalent to reduction of the effective adhesive area  
 $\tilde{A} = (1 - D_2)A_0$
  - Area reduction can be defined as function of thickness strain  
 $(1 - D_2) = \delta_A(\varepsilon_{33})$
  - Exponential approach or direct input of  $\delta_A(\varepsilon_{33})$  available
- 
- Active and reversible in liquid phase, but remains fixed in solid phase

Effect of fixed (C) and exponential (D) damage on response to tensile loading



### Viscous fingering



[LWF KS2-Specimens]



Bundesministerium  
für Wirtschaft  
und Klimaschutz



Mercedes-Benz



ARENA2036



TÜV Rheinland®  
Genau. Richtig.

13

## Summary and Outlook



Introduced new LS-DYNA material \*MAT\_GENERALIZED\_ADHESIVE\_CURING / \*MAT\_307:

- Combines and extends the properties of existing material models in LS-DYNA (\*MAT\_277, \*MAT\_252) and of a modified TAPO model (UMAT, Kühlmeyer and Matzenmiller)
  - Curing kinetics with induced chemical shrinkage and heating
  - Visco-elastic behavior with temperature and degree of cure depending, horizontal and vertical shifts
  - Non-associated  $I_1 - J_2$  plasticity with distortional hardening
  - Empirical isotropic damage model for material damage
  - (Pre-) damage formulation for the effect of viscous fingering
- Successful material calibration
- Future work will concentrate on possibly necessary extensions with respect to curing kinetics and viscous fingering

# Curing Kinetics

New parameters and new curing models

# Curing Kinetics

## (Extended) Sourer-Kamal-Model

- Evolution equation for degree of cure  $p$ :

$$\dot{p} = K_1(T) \cdot (1 - p)^{n_1} + K_2(T) \cdot (1 - p)^{n_2} \cdot p^m$$

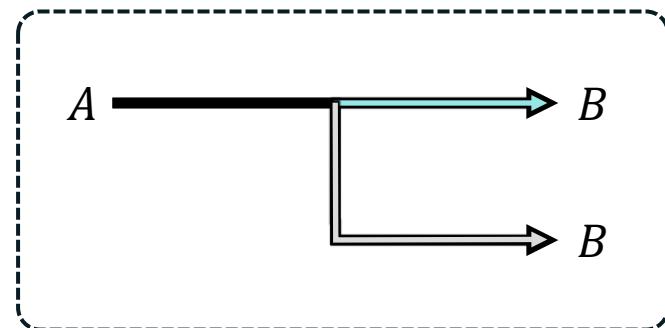
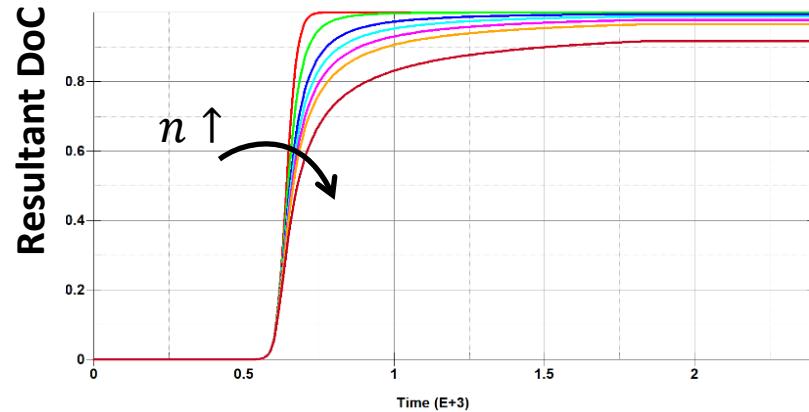
- Different options for expressions  $K_i(T)$ , but mostly used:

$$K_i(T) = k_i \cdot \exp\left(\frac{-Q_i}{RT}\right)$$

- Chemical interpretation:

- System of two species  $A$  and  $B$ , with concentrations  $c_1$  and  $c_2$
- Sum of concentrations is always 1.0
- Identifying  $c_2 = p$  and, thus,  $c_1 = 1 - p$  gives

$$\begin{aligned}\dot{c}_1 &= -K_1(T) \cdot c_1^{n_1} - K_2(T) \cdot c_1^{n_2} \cdot c_2^m \\ \dot{c}_2 &= K_1(T) \cdot c_1^{n_1} + K_2(T) \cdot c_1^{n_2} \cdot c_2^m\end{aligned}$$



# Curing Kinetics

## Three Species models

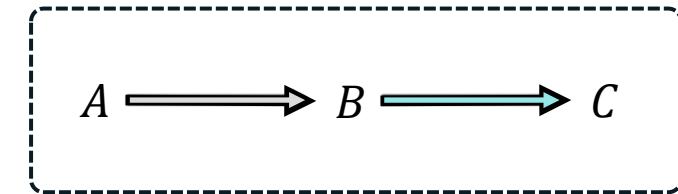
- System of three species  $A$ ,  $B$  and  $C$ , with concentrations  $c_1$ ,  $c_2$  and  $c_3$ , respectively
- Three options available

- System 1:

$$\dot{c}_1 = -K_1(T) \cdot c_1^{n_1} \cdot c_2^{m_1}$$

$$\dot{c}_2 = K_1(T) \cdot c_1^{n_1} \cdot c_2^{m_1} - K_2(T) \cdot c_2^{n_2}$$

$$\dot{c}_3 = K_2(T) \cdot c_2^{n_2}$$



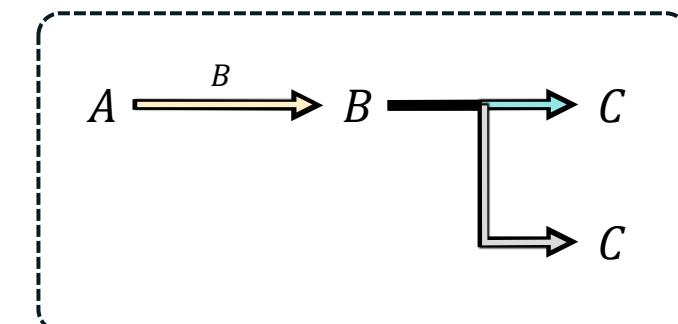
- System 2:

$$\dot{c}_1 =$$

$$\dot{c}_2 = -K_2(T) \cdot c_2^{n_2} \cdot c_3^{m_2}$$

$$\dot{c}_3 = K_2(T) \cdot c_2^{n_2} \cdot c_3^{m_2} - K_3(T) \cdot c_2^{n_3}$$

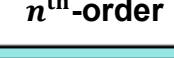
$$\dot{c}_3 = + K_3(T) \cdot c_2^{n_3}$$



$n^{\text{th}}$ -order with  
autocatalysis



$n^{\text{th}}$ -order



Prout-Tompkins



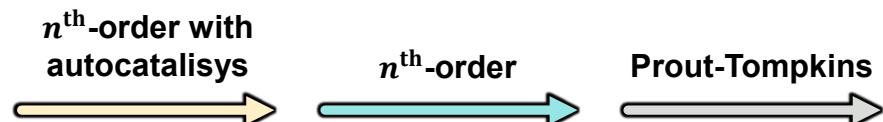
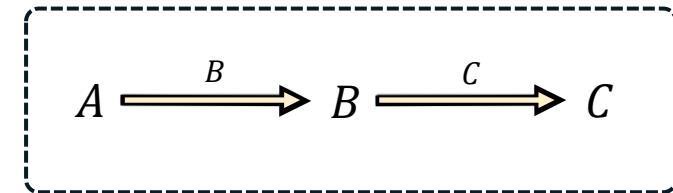
# Curing Kinetics

## Three Species models

- System of three species  $A$ ,  $B$  and  $C$ , with concentrations  $c_1$ ,  $c_2$  and  $c_3$ , respectively
- Three options available:
- System 3:

$$\begin{aligned}\dot{c}_1 &= -K_1(T) \cdot (1 + k_{c1} \cdot c_2) c_1^{n_1} \\ \dot{c}_2 &= K_1(T) \cdot (1 + k_{c1} \cdot c_2) c_1^{n_1} \\ \dot{c}_3 &= \end{aligned}$$

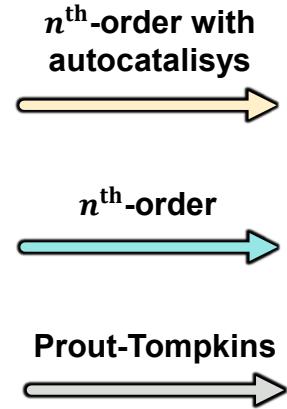
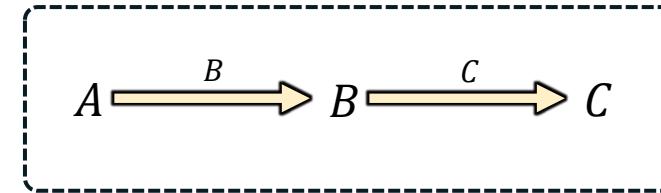
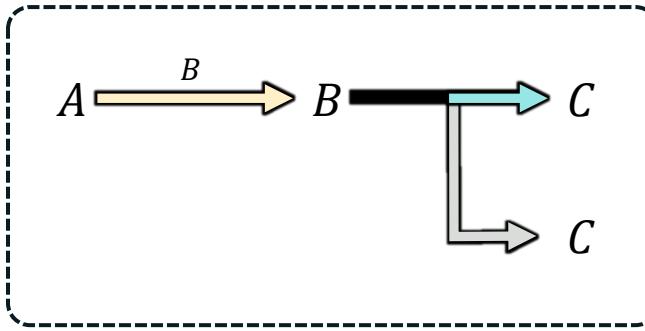
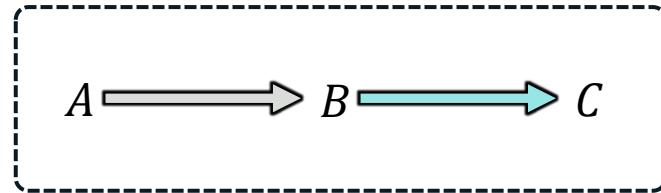
$$\begin{aligned}& -K_2(T) \cdot (1 + k_{c2} \cdot c_3) c_2^{n_2} \\ & K_2(T) \cdot (1 + k_{c2} \cdot c_3) c_2^{n_2}\end{aligned}$$



# Curing Kinetics

## Three Species models

- System of three species  $A$ ,  $B$  and  $C$ , with concentrations  $c_1$ ,  $c_2$  and  $c_3$ , respectively
- Three options available:

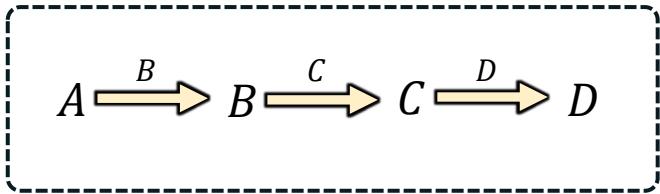


- Sum of concentrations is always 1.0
  - Product  $c_3 = 1 - c_1 - c_2$  can be eliminated from the systems
  - Only system of two ordinary differential equations to be solved
- Degree of cure  $p$  is a function of the concentrations:  $p = 1 - c_1 - c_2 + F_1 \cdot c_2$

# Curing Kinetics

## Four Species models

- System of four species  $A$ ,  $B$ ,  $C$  and  $D$ , with concentrations  $c_1$ ,  $c_2$ ,  $c_3$  and  $c_4$ , respectively
- One option available:



$n^{\text{th}}$ -order with  
autocatalysis

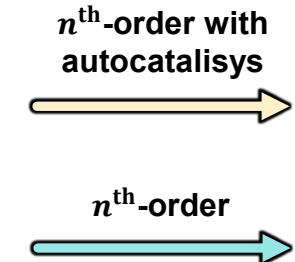
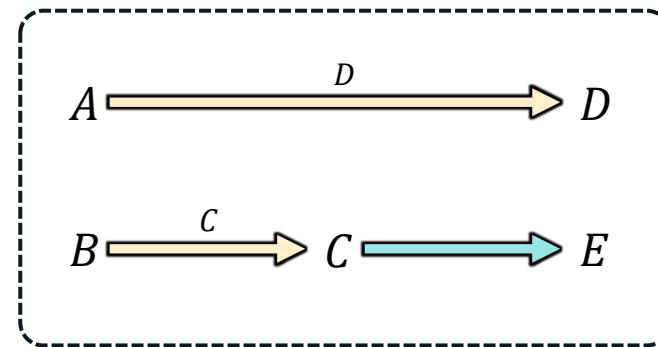
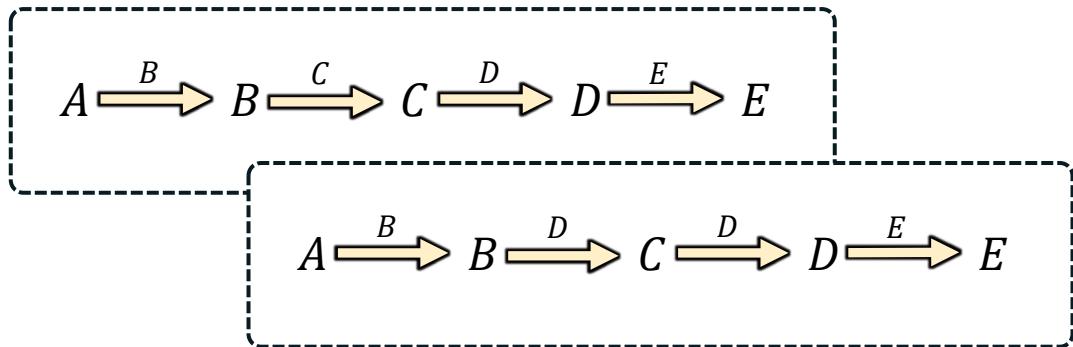


- Sum of concentrations is always 1.0
  - Product  $c_4$  can be eliminated from the systems
  - System of three ODEs to be solved
- Degree of cure  $p$  is a function of the concentrations:  $p = (1 - c_1 - c_2 - c_3) + F_1 \cdot (c_2 + c_3) + F_2 \cdot c_3$

# Curing Kinetics

## Five Species models

- System of five species  $A, B, C, D$  and  $E$ , with concentrations  $c_1, c_2, c_3, c_4$  and  $c_5$ , respectively
- Three options available:



- Sum of concentrations of each system of reactions is always 1.0
  - $c_5$  can be eliminated from the system
  - System of four ODEs to be solved
- Degree of cure  $p$  is a function of the concentrations

$$p = (1 - c_1 - c_2 - c_3 - c_4) + F_1 \cdot (c_2 + c_3 + c_4) + F_2 \cdot (c_3 + c_4) + F_3 \cdot c_4$$

$$p = F_1 \cdot (1 - c_1) + (1 - F_1)(F_2(1 - c_2) + (1 - F_2)(1 - c_2 - c_3))$$

# Curing Kinetics

## Model free kinetics

- So far, scalar parameters  $(k_i, Q_i, k_{ci}, n_i, m_i)$  for a pre-defined model had to be defined

- Alternative approach: Model free kinetics option

- Evolution equation for degree of cure  $p$

$$\dot{p} = \exp(\ln(A'(p))) \cdot \exp\left(-\frac{Q(p)}{RT}\right)$$

- Direct, tabulated input of the logarithmic scaling function  $\ln(A'(p))$  and the activation energy  $Q(p)$

# Visco-Elasticity

New input possibilities

# Visco-Elasticity

## Prony-Series input

- Behavior is governed by the Prony-series expansion for shear and bulk modulus

$$G(t) = G_{\infty} + \sum_{i=1}^{n_G} G_i e^{-\beta_i^G t}, \quad K(t) = K_{\infty} + \sum_{i=1}^{n_K} K_i e^{-\beta_i^K t}$$

- Standard input:

- Individual input for  $G_i, K_i, \beta_i^G, \beta_i^K$
- Maximum flexibility of visco-elastic response (frequency dependent Poisson's ratio  $\nu$ )
- Input restricted to  $n_G \leq 18$  and  $n_K \leq 18$

- Feedback

- “Would be great to have more Prony-series terms”
- “We always assume a constant  $\nu$ ”

# Visco-Elasticity

## Prony-Series input

- Behavior is governed by the Prony-series expansion for shear and bulk modulus

$$G(t) = G_{\infty} + \sum_{i=1}^{n_G} G_i e^{-\beta_i^G t}, \quad K(t) = K_{\infty} + \sum_{i=1}^{n_K} K_i e^{-\beta_i^K t}$$

- New parameter VIOPT. If value less than zero, then...

- ... a constant value for  $\nu$  and, consequently,  $K_i = \frac{2+2\nu}{3(1-2\nu)} G_i$  are assumed
- ... the decay constants match:  $\beta_i^G = \beta_i^K$

- Two options for VIOPT

- -1: Input of  $E_i$ , that are internally translated into shear relaxation moduli  $G_i = \frac{1}{2+2\nu} E_i$
  - -2: Direct input of shear relaxation moduli  $G_i$
- Up to 25 Prony-series terms possible

# Visco-Elasticity

## Prony-Series input

**Card 13a.** The keyword reader assumes the input deck includes this version of Card 13 if, in the first instantiation of this card, the value in the first entry is  $\geq 0.0$ . Input up to 18 instantiations of this card. The next keyword (“\*”) card terminates this input if using fewer than 18 cards. The number of terms for the shear behavior may differ from that for the bulk behavior: insert zero to exclude a term.

Gi	BETAGi	Ki	BETAKi				
----	--------	----	--------	--	--	--	--

**Card 13b.** The keyword reader assumes the input deck includes this version of Card 13 if the value in the first entry is  $< 0.0$

VIOPT	NUE						
-------	-----	--	--	--	--	--	--

**Card 14a.** Include this card if VISOPT = -1 on Card 13b. Input up to 13 instantiations of this card. The next keyword (“\*”) card terminates this input if using fewer than 13 cards.

Ei	BETAi	Ej	BETAj				
----	-------	----	-------	--	--	--	--

**Card 14b.** Include this card if VISOPT = -2. Include up to 13 instantiations of this card. The next keyword (“\*”) card terminates this input if using fewer than 13 cards.

Gi	BETAi	Gj	BETAj				
----	-------	----	-------	--	--	--	--

# Visco-Elasticity

## Prony-Series input example

- Assume constant value  $\nu = 0.0 \rightarrow K_i = \frac{2}{3} G_i, E_i = 2 G_i$
- Following input is equivalent:

Standard Input

```
... (Cards 1 to 12)
$      Gi   beta_Gi          Ki   beta_Ki
3.000E-01 1.000E-01 2.000E-01 1.000E-01
6.000E+00 1.000E+00 4.000E+00 1.000E+00
9.000E+01 1.000E+02 6.000E+01 1.000E+02
1.500E+03 1.000E+04 1.000E+03 1.000E+04
```

VIOPT < 0

```
... (Cards 1 to 12)
$      VIOPT      nu
      -1      0.0
$      Ei   beta_Ei          Ej   beta_Ej
6.000E-01 1.000E-01 1.200E+01 1.000E+00
1.800E+02 1.000E+02 3.000E+03 1.000E+04
```

```
... (Cards 1 to 12)
$      VIOPT      nu
      -2      0.0
$      Gi   beta_Gi          Gj   beta_Gj
3.000E-01 1.000E-01 6.000E+00 1.000E+00
9.000E+01 1.000E+02 1.500E+03 1.000E+04
```

# Summary and Outlook

---

# Summary and Outlook

- New curing kinetics options
  - Chemical systems with two, three, four, or five species
  - Model-free kinetics approach with tabulated input for activation energies and logarithmic scaling function
  - Approaches validated with experimental and simulation data
- New input for Prony-series terms
  - Assume a frequency-independent Poisson's ratio
  - Only define series expansion of Young's or shear modulus
  - Higher number of Prony-series terms
- Need to look into the plasticity algorithm when material is used in a cohesive element

**Stay tuned: This could be the second part of a trilogy!**

# Thank You

---

DYNAmore GmbH,  
an Ansys Company  
Industriestr. 2  
70565 Stuttgart-Vaihingen  
Germany

Tel.: +49 - (0)711 - 459 600 0  
Fax: +49 - (0)711 - 459 600 29  
[info@dynamore.de](mailto:info@dynamore.de)

[www.dynamore.de](http://www.dynamore.de)  
[www.dynaexamples.com](http://www.dynaexamples.com)  
[www.dynasupport.com](http://www.dynasupport.com)  
[www.dynalook.com](http://www.dynalook.com)

© 2023 DYNAmore GmbH, an Ansys Company. All rights reserved.  
Reproduction, distribution, publication or display of the slides and content  
without prior written permission of the DYNAmore GmbH is strictly prohibited.

Find us on

